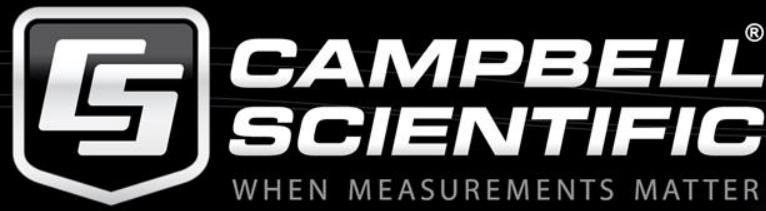


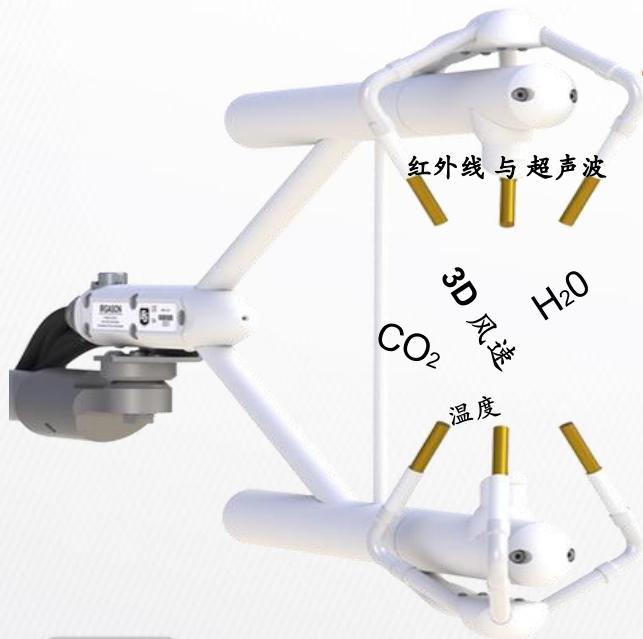
# 涡动相关技术的基本理论



理加联合科技有限公司

# 近地面层通量测定的理论要点与应用理解

周新华 Campbell Scientific, Inc



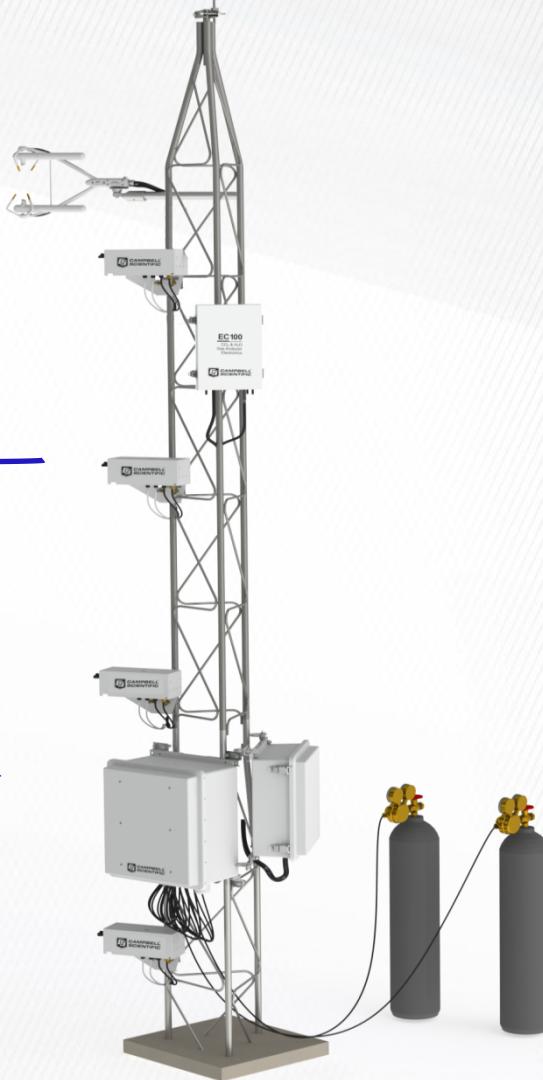
$$NEE_{CO_2} \approx \overline{C_d} \left( \overline{w'X'_{CO_2}}|_h + \int_0^h \frac{\partial X_{CO_2}}{\partial t} dz \right)$$

干空气  
密度       $CO_2$   
端流通量      通量测定高度下  
                   $CO_2$  存储变化

Gu et al./Ag For Meteorol (2012)



**IRGASON**  
(红外超声碳水热通量集成观测仪)



**AP200**  
(红外大气碳水热纵断面观测系统)

# Acknowledgement

(综述于以下专家的讲座)

## Campbell Scientific Inc.

Ryan Campbell, Benjamin Conrad, Sasha Ivans, Larry Jacobsen, Edward Swiatek, Bert Tanner

## University of Nebraska

Shashi Verma

## CSIRO Marine and Atmospheric Research

Ray Leuning



# 全球关注



多

少



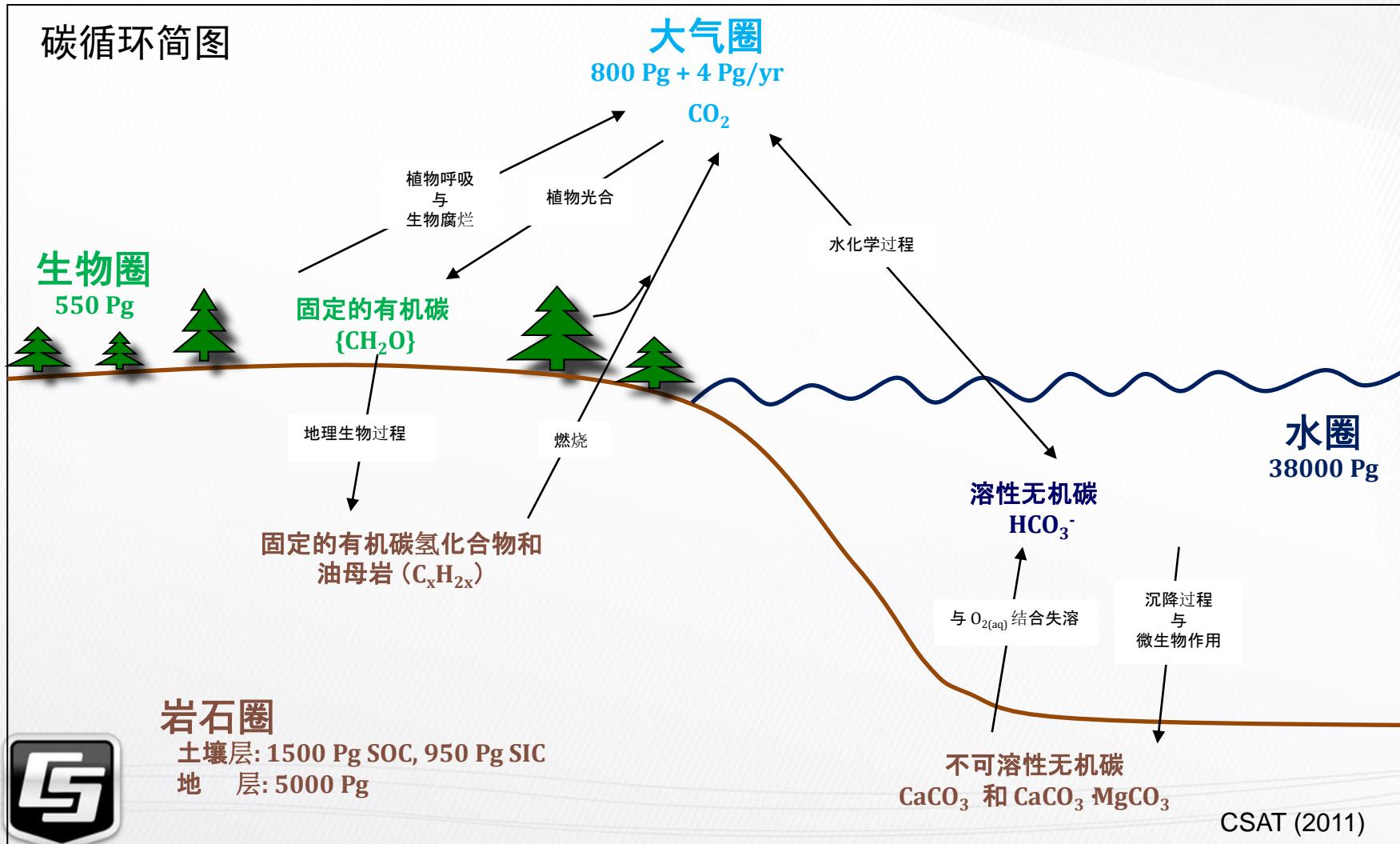
# 碳何从



# 碳何去



- 研究目的: 1) 更好地理解碳循环的自然机制  
 2) 人类活动对这一自然机制的干扰程度  
 3) 制定人类社会与经济发展策略使碳循环良性化



# 兴趣通量

$$Rn = LE + H + G \text{ (W m}^{-2} \text{s}^{-1}\text{)}$$

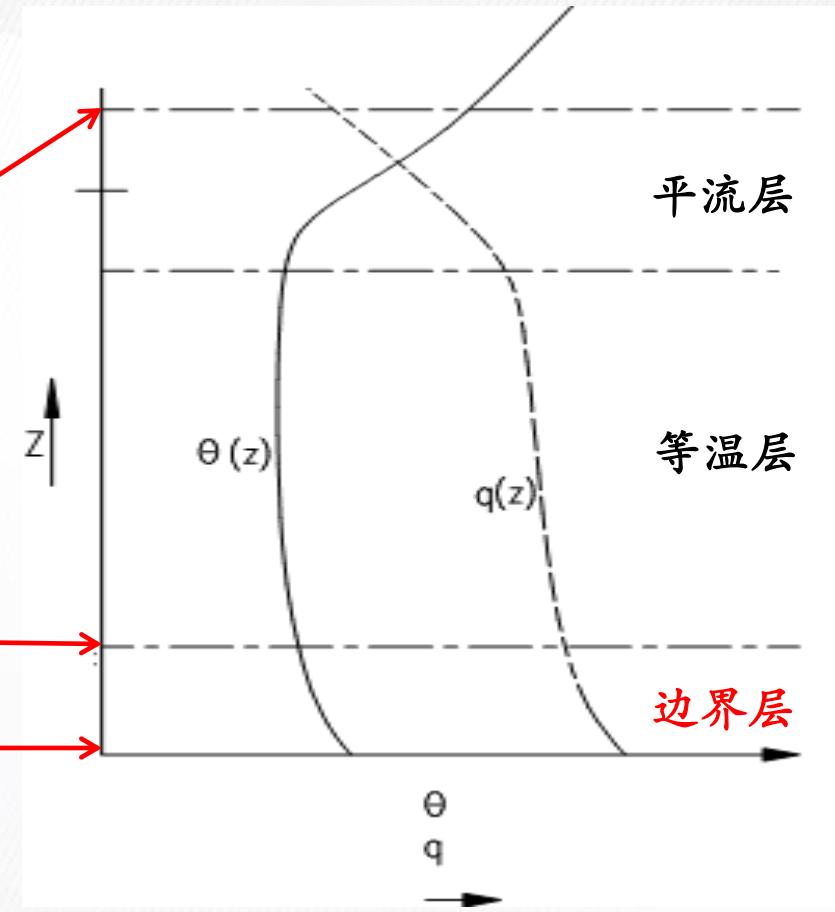
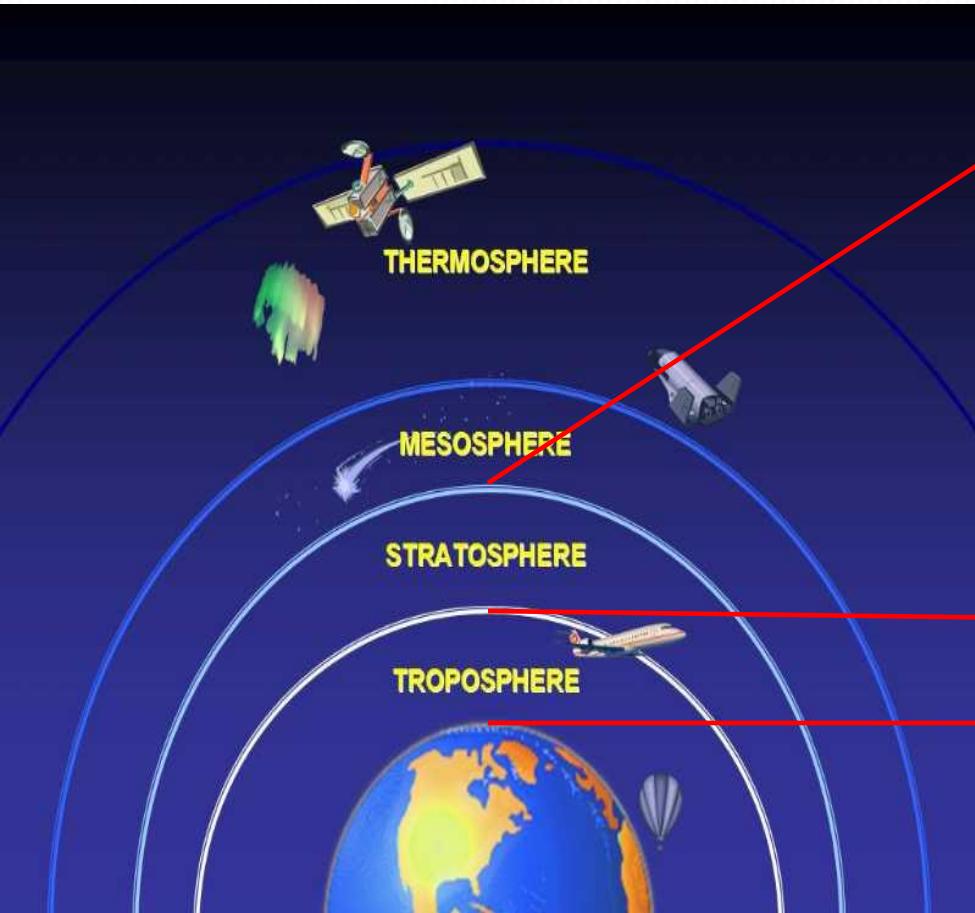
净辐射 潜热 感热 地表热  
通量 通量 通量 通量

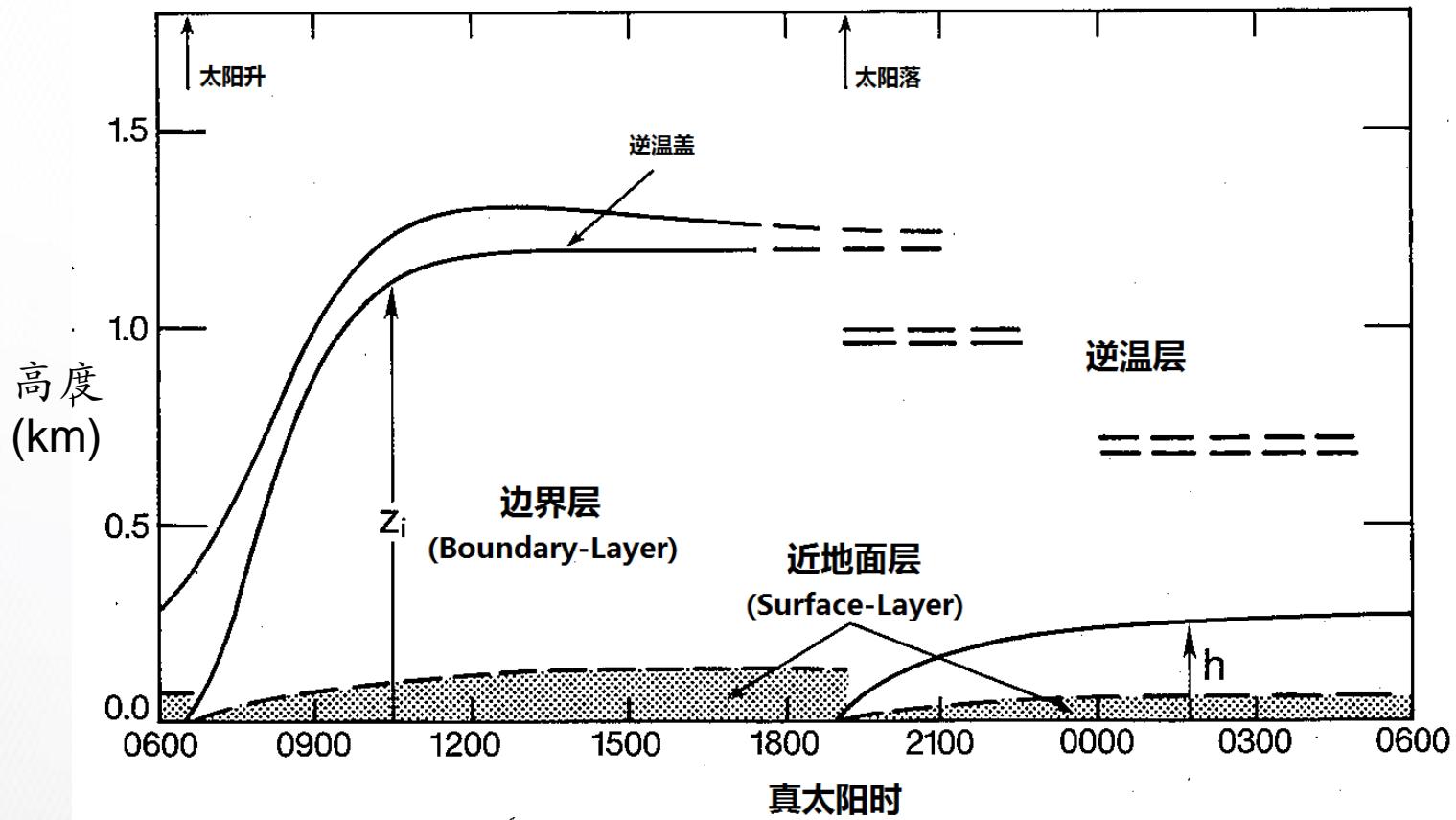
Fc

二氧化碳通量

(mg m<sup>-2</sup> s<sup>-1</sup>)



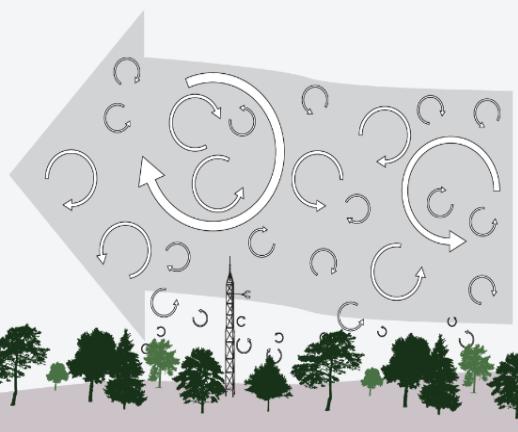
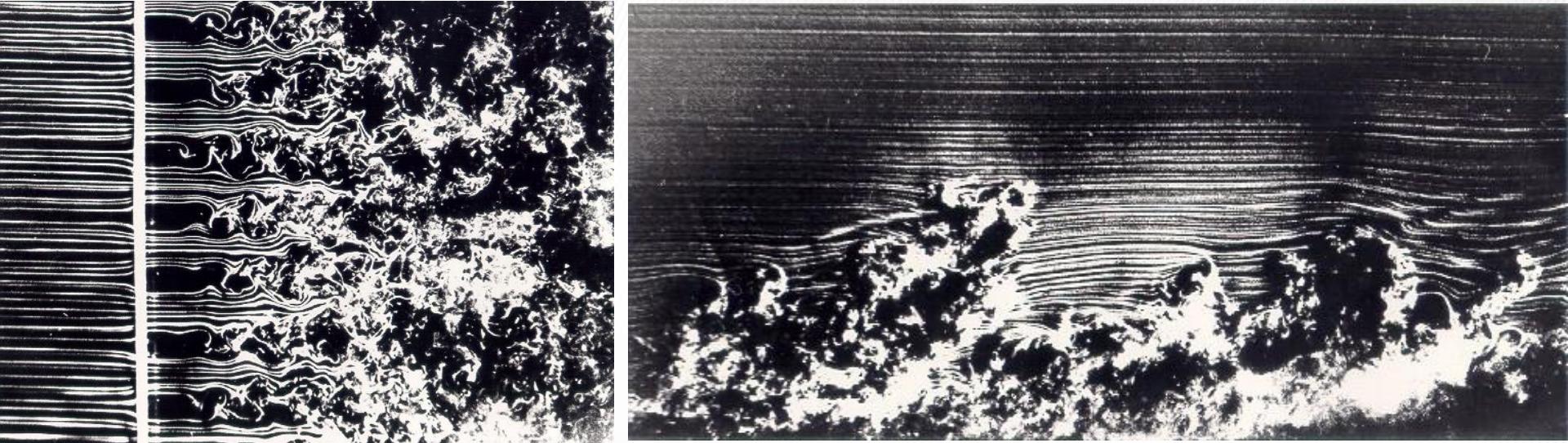




对流层：随太阳升起对地面加热而抬升活跃，随太阳降落与地面冷却而降低变稳 (Kaimal & Finnigan 1994)



# 近地面层的湍流



## 近地面层(Surface-Layer)

以水平流动为主的水气热空气湍流体。

其湍流产生于：

1. 与下垫面摩擦引发的水平风速梯度
2. 与下垫面热交换而改变密度所产生的空气浮力

## 内部特征

1. 无序
2. 三维无规则运动
3. 各气体组分充分混合



# 了解近地面层湍流

1. 流体运动的数学物理描述
2. 湍流的产生与耗散及其综合描述原理
3. 湍流的结构
4. 湍流传输动量，热量，质量的规律



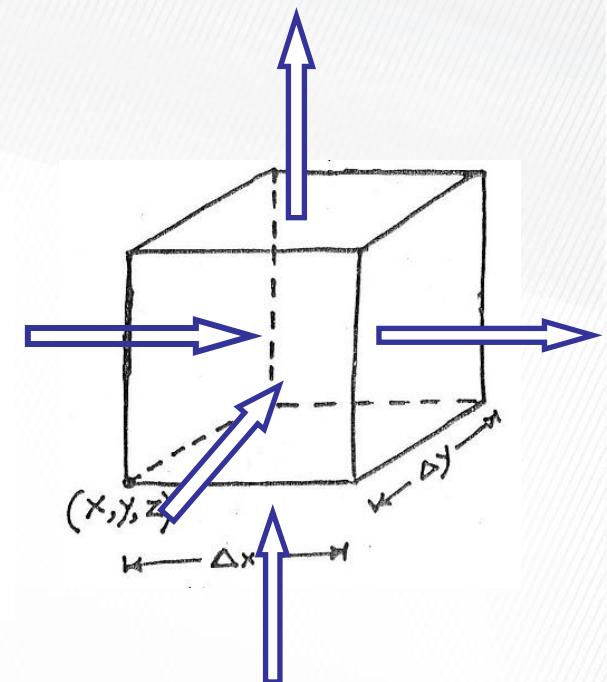
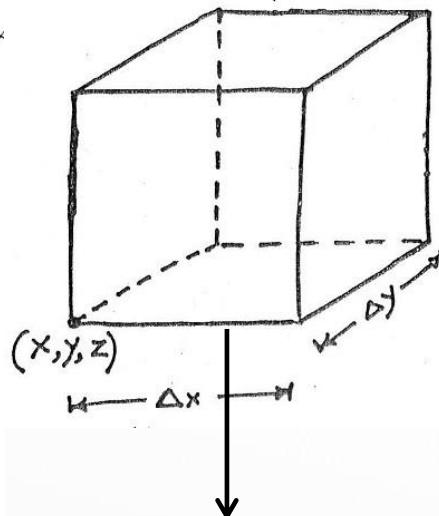
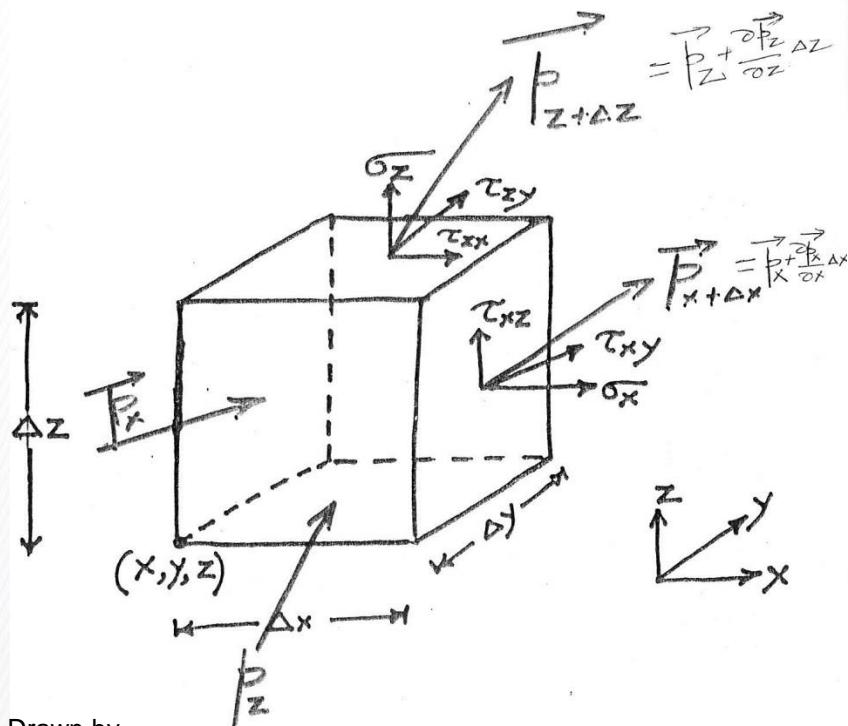
# 1. 流体运动的数学物理描述



## 压力 ( $P$ ) 与应力 ( $\tau, \sigma$ )

## 重力

## 物质守恒



Drawn by  
Dr. Shashi Verma

$$\text{Similarly } \vec{P}_y \neq \vec{P}_{y+\Delta y}$$

$$\rho g \Delta x \Delta y \Delta z$$

空气密度      重力加速度



# 描述流体的基本方程

## 运动方程 (Navier-Stokes Equations)

$$\rho \left( \frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} \right) = - \frac{\partial P}{\partial x_i} + \mu \frac{\partial^2 u_i}{\partial x_j \partial x_j} - \rho g \delta_{3i}$$

速度  
时间变量  
空间变量  
粘度系数  
Kronecker Delta

## 连续方程 (Continuity Equation)

$$\frac{\partial u_j}{\partial x_j} = 0$$

## 状态方程 (Equation of State)

$$P = \rho R T$$

压力  
空气密度  
气体常数  
温度



# 一般表达形式

## 运动方程

$$\rho \left( \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right) = - \frac{\partial p}{\partial x} + \mu \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right)$$

$$\rho \left( \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} \right) = - \frac{\partial p}{\partial y} + \mu \left( \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right)$$

$$\rho \left( \frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} \right) = - \frac{\partial p}{\partial z} + \mu \left( \frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) - \rho g$$

## 连续方程

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$



## 宝思内思克近似 (Boussinesq Approximation)

1. 空气粘度系数不变 ( $\mu=\text{constant}$ )

2. 空气为不可压气体

a. 在近地面层，压力( $P$ )，温度( $T$ ) 和密度( $\rho$ )与其各自基值( $P_0, T_0, \rho_0$ )的差( $P_1, T_1, \rho_1$ )与其基值比很小

$$\left| \frac{P_1}{P_0} \right| \ll 1 \quad \left| \frac{T_1}{T_0} \right| \approx \left| \frac{\rho_1}{\rho_0} \right| \ll 1$$

b. 压力波动更小，空气密度波动主要由温度波动引起。

$$\left| \frac{P_1}{P_0} \right| \ll \left| \frac{T_1}{T_0} \right| \approx \left| \frac{\rho_1}{\rho_0} \right|$$

$$\rho \left( \frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} \right) = - \frac{\partial P}{\partial x_i} + \mu \frac{\partial^2 u_i}{\partial x_j \partial x_j} - \rho g \delta_{3i}$$



$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = - \frac{\partial P_1}{\rho_0 \partial x_i} + \frac{\mu}{\rho_0} \frac{\partial^2 u_i}{\partial x_j \partial x_j} + \frac{T_1}{T_0} g \delta_{3i}$$

温度波动与重力偶联  
可有效地绕动气流

运动方程的宝思内思克近似



# 雷诺(Reynolds)变量分解与平均规则

分解规则

$$u = \bar{u} + u'$$

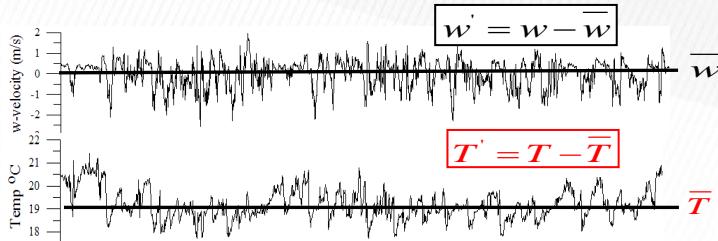
平均规则

$$\bar{u}' = 0$$

$$\overline{\bar{u} + u'} = \bar{\bar{u}} + \bar{u}' = \bar{u}$$

$$\begin{aligned}\overline{uw} &= \overline{(\bar{u} + u')(w + w')} \\ &= \bar{u}\bar{w} + \overline{u'w'}\end{aligned}$$

$$\frac{\partial \bar{u}}{\partial x} = \frac{\partial \bar{u}}{\partial x} \quad \frac{\partial \bar{u}}{\partial t} = \frac{\partial \bar{u}}{\partial t}$$



宝思内思克近似运动方程

$$\frac{\partial u_i}{\partial t} + u_J \frac{\partial u_i}{\partial x_J} = - \frac{\partial p_1}{\rho_0 \partial x_i} + \frac{\mu}{\rho_0} \frac{\partial^2 u_i}{\partial x_J \partial x_J} + \frac{T_1}{T_0} g \delta_{3i}$$



雷诺平均运动方程

$$\frac{\partial \bar{u}_i}{\partial t} + \bar{u}_J \frac{\partial \bar{u}_i}{\partial x_J} = - \frac{\partial \bar{p}_1}{\rho_0 \partial x_i} + \frac{1}{\rho_0} \frac{\partial}{\partial x_J} \left( \mu \frac{\partial \bar{u}_i}{\partial x_J} - \rho_0 \overline{u'_i u'_J} \right) + \frac{\bar{T}_1}{T_0} g \delta_{3i}$$



## 2. 端流的产生与耗散及其综合描述原理



# 湍流动能变化

$$\frac{\rho}{2} \frac{D \left( \overline{u'^2 + v'^2 + w'^2} \right)}{Dt} = -\rho \overline{(u'w')} \frac{\partial \bar{u}}{\partial z} + \rho \frac{g}{\bar{\theta}} \overline{(\theta'w')} + \frac{\partial \overline{(p'w')}}{\partial z} - \frac{\rho}{2} \frac{\partial \overline{(u'^2 + v'^2 + w'^2)w'}}{\partial z} - \rho \epsilon$$

↑ 动能变化      ↑ 下垫面摩擦      ↑ 气团沉浮      ↑ 压力运输      ↑ 湍流运输      ↑ 粘度扩散

瑞查德数  
Richard number

$$R_f = \frac{(g/\bar{T})\bar{T}'w'}{\overline{u'w'}(\partial \bar{u}/\partial z)}$$

气团浮力  
下垫面摩擦



奥布克瓦长度  
Obukhov length

$$L = - \frac{u_*^3/k}{(g/\bar{T})\overline{(T'w')}_0}$$

描述整个大气近地面

近地面层  
大气稳定性

$$\frac{z}{L} = - \frac{(g/\bar{\theta})\overline{\theta'w'}}{u_*^3/kz}$$

无量纲

## 近地面层稳定性

$$\frac{z}{L} = - \frac{g_0 / \bar{\theta}(\bar{w}'\bar{\theta}')_S}{u_*^3 / kz}$$

$u_*$  摩擦速度 ( $\text{m s}^{-1}$ )

$k$  von Karman 常数 (0.41)

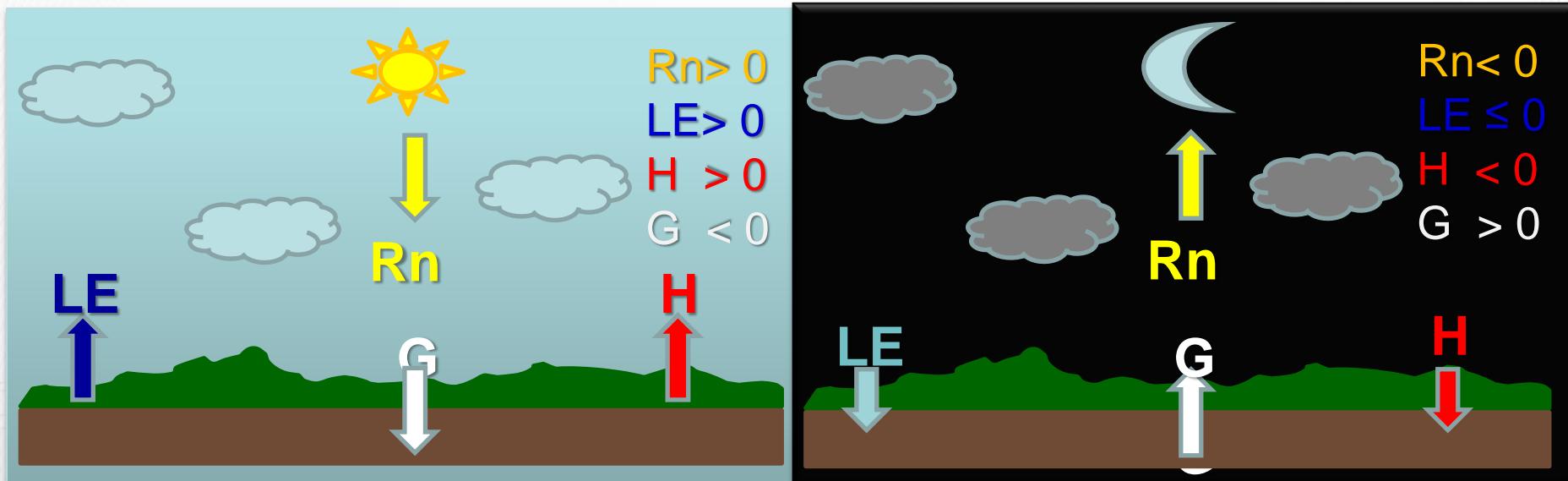
$g_0$  海平面重力加速度 ( $9.81 \text{ m s}^{-2}$ )

$\theta$  潜温 (K)

$z$  高度 (m)

$\frac{z}{L} < 0$  非稳定近地面层

$\frac{z}{L} > 0$  稳定近地面层



$$u_* = [-(\overline{u'w'})_0]^{1/2} \quad (1.25a)$$

$$T_* = \frac{-(\overline{w'\theta'})_0}{u_*} \quad (1.25b)$$

Although defined strictly in terms of fluxes at the surface,  $u_*$  and  $T_*$  are evaluated, in practice, from measurements of the fluxes at some convenient height within the surface layer where their vertical variations can be assumed negligible with height, a reasonable assumption for  $z \lesssim |L|$  (Haugen et al., 1971). The important nondimensional forms to emerge in the surface layer are

$$\phi_m = (kz/u_*)(\partial \bar{u}/\partial z) \text{ wind shear,} \quad (1.26)$$

$$\phi_h = (kz/T_*)(\partial \bar{\theta}/\partial z) \text{ thermal stratification,} \quad (1.27)$$

$$\phi_w = \sigma_w/u_* \text{ variability in } w, \quad (1.28)$$

$$\phi_\theta = \sigma_\theta/|T_*| \text{ variability in } \theta, \quad (1.29)$$

$$\phi_\epsilon = kze/\epsilon u_*^3 \text{ dissipation of turbulent kinetic energy,} \quad (1.30)$$

where  $\sigma_w$  and  $\sigma_\theta$  are the standard deviations of  $w$  and  $\theta$ , and  $\epsilon$  is the rate of dissipation of turbulent kinetic energy. We introduce  $\epsilon$  here because of its relevance to discussions of the turbulent kinetic energy budget later in this chapter. Its relationship to velocity spectra will be discussed in Chapter 2.

All the above functions follow M-O scaling with surprisingly small scatter, as evident in the plots of the Kansas data (Businger et al., 1971; Wyngaard and Coté, 1971). The following formulations are essentially the Kansas results, reexamined and refined through comparison with other observations (Dyer, 1974; Högström, 1988):

$$\phi_m = \begin{cases} (1 + 16|z/L|)^{-1/4}, & -2 \leq z/L \leq 0 \\ (1 + 5z/L), & 0 \leq z/L \leq 1 \end{cases} \quad (1.31)$$

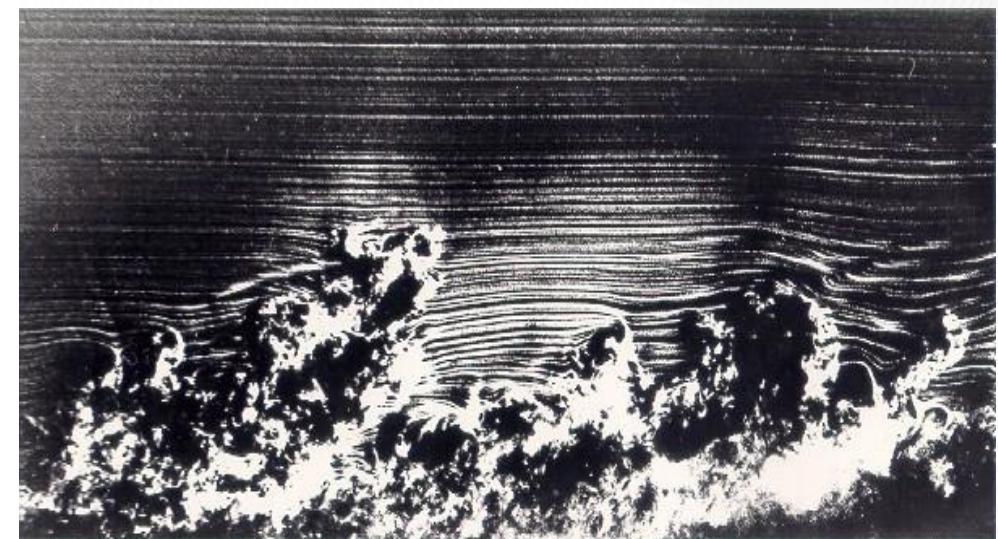
$$\phi_h = \begin{cases} (1 + 16|z/L|)^{-1/2}, & -2 \leq z/L \leq 0 \\ (1 + 5z/L), & 0 \leq z/L \leq 1 \end{cases} \quad (1.32)$$

$$\phi_w = \begin{cases} 1.25(1 + 3|z/L|)^{1/3}, & -2 \leq z/L \leq 0 \\ 1.25(1 + 0.2z/L), & 0 \leq z/L \leq 1 \end{cases} \quad (1.33)$$

$$\phi_\theta = \begin{cases} 2(1 + 9.5|z/L|)^{-1/3}, & -2 \leq z/L \leq 0 \\ 2(1 + 0.5z/L)^{-1}, & 0 \leq z/L \leq 1 \end{cases} \quad (1.34)$$

$$\phi_\epsilon = \begin{cases} (1 + 0.5|z/L|^{2/3})^{3/2}, & -2 \leq z/L \leq 0 \\ (1 + 5z/L), & 0 \leq z/L \leq 1. \end{cases} \quad (1.35)$$

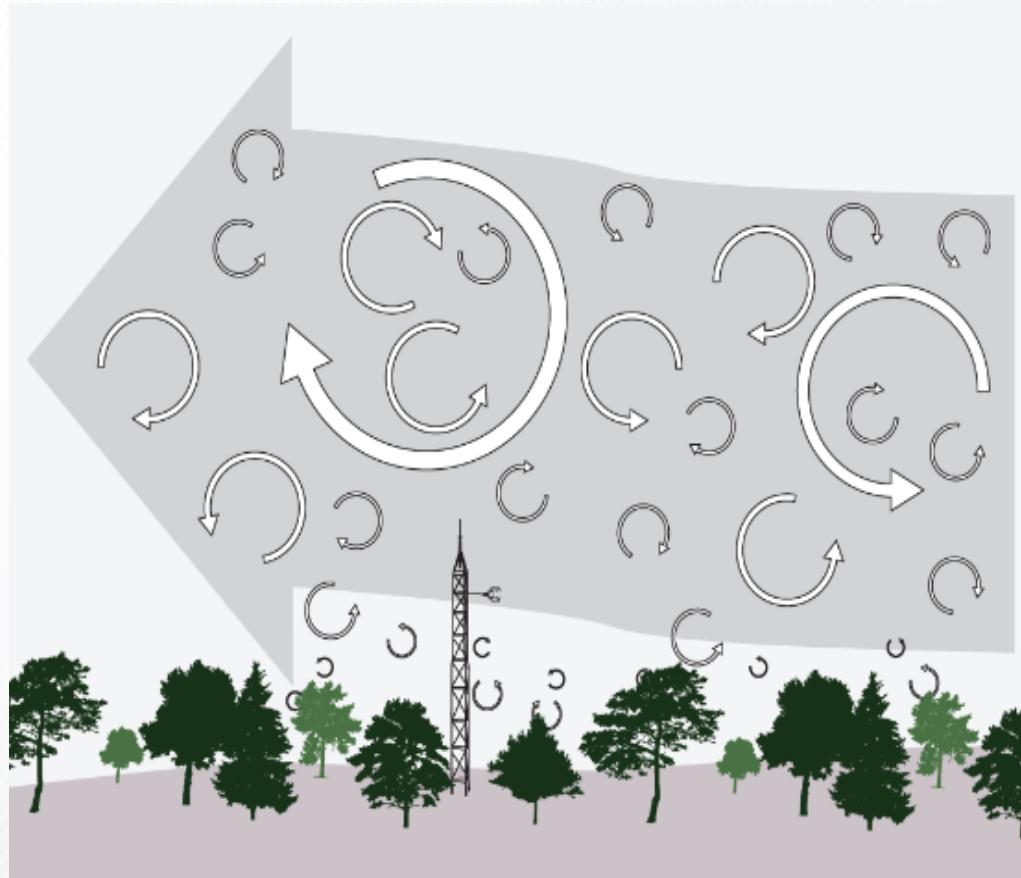
The forms of these functions, plotted in Fig. 1.7, cannot be predicted from



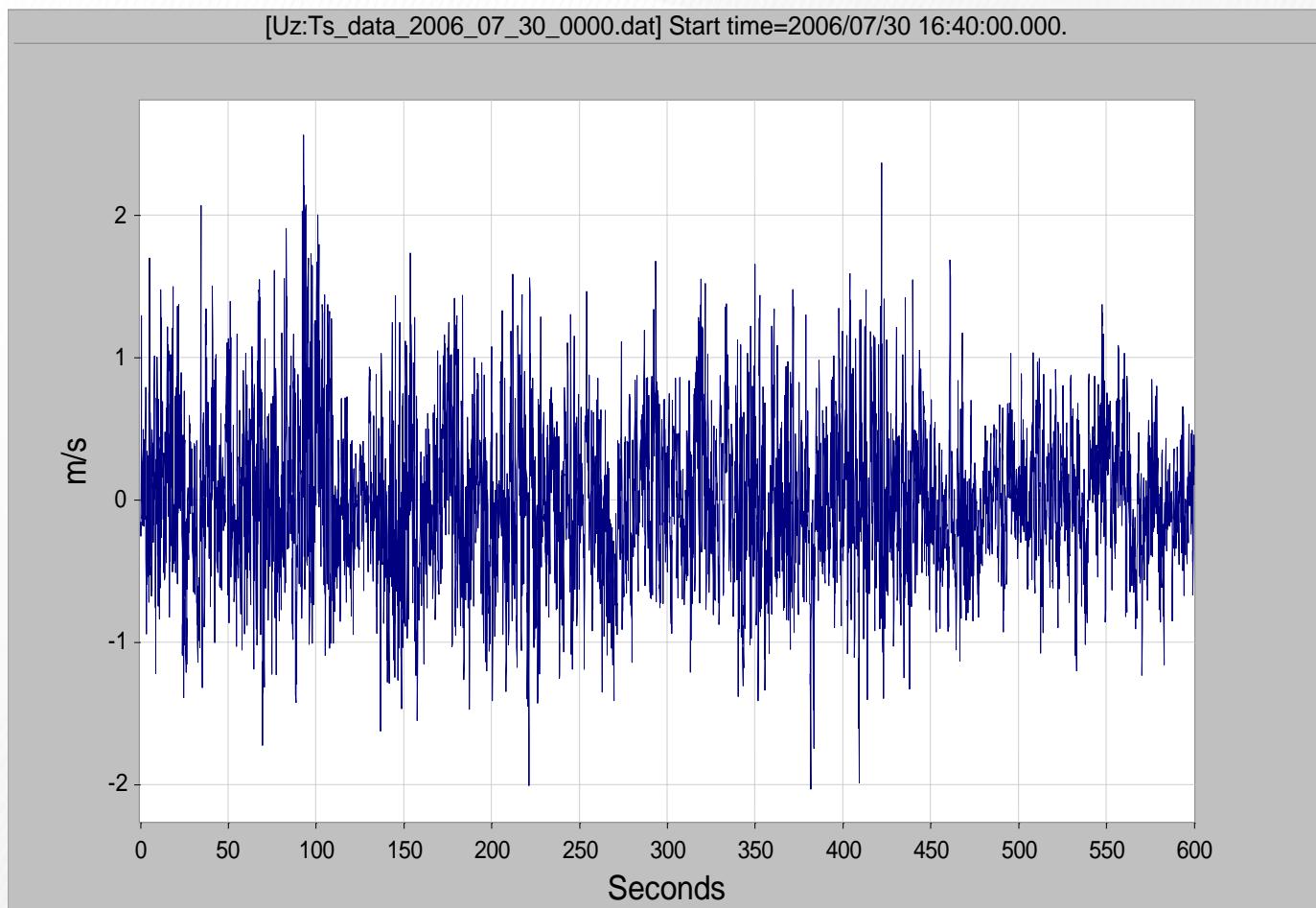
(Kaimal & Finnigan 1994)

### 3. 湍流的结构





# 时域上垂直风速



# 垂直风速的湍流谱

$\omega$  – 角频率  
 $t$  – 时间

$$w(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} w(t) e^{i\omega t} dt$$

$$w(t) = \int_{-\infty}^{\infty} w(\omega) e^{-i\omega t} d\omega$$



# 湍流谱的分解

任何信号均可以表达为三角玄函数级数之和，  
即傅立叶级数（Fourier series）。

$$s_a(t) = k_a + A_{a1} \cos(\omega_{a1}t + \phi_{a1}) + A_{a2} \cos(\omega_{a2}t + \phi_{a2}) + A_{a3} \cos(\omega_{a3}t + \phi_{a3}) + \dots$$

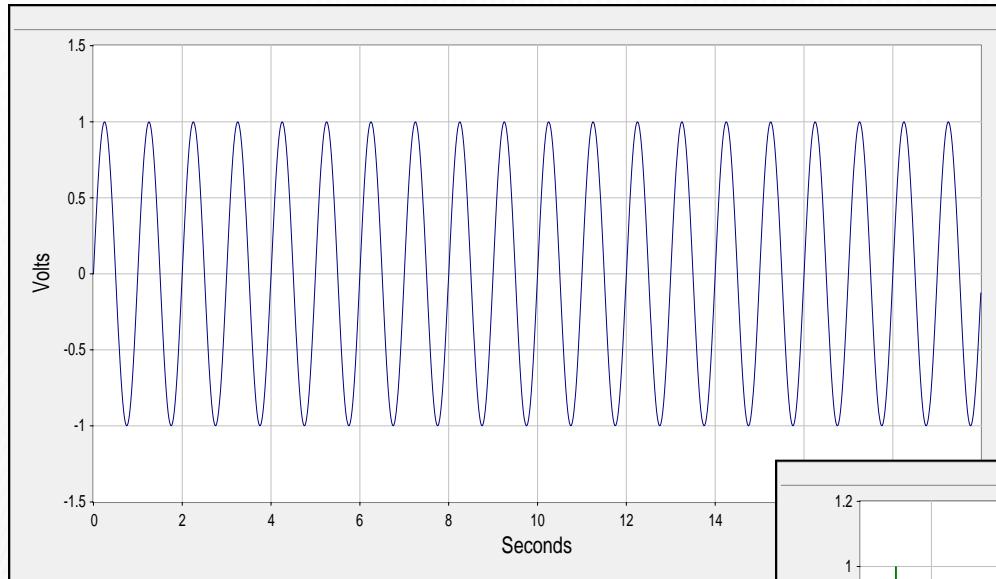
信号谱是将振幅( $A_{ai}$ ) 和相位( $\phi_{ai}$ ) 表达为这些角频率( $\omega_{ai}$ ) 的函数



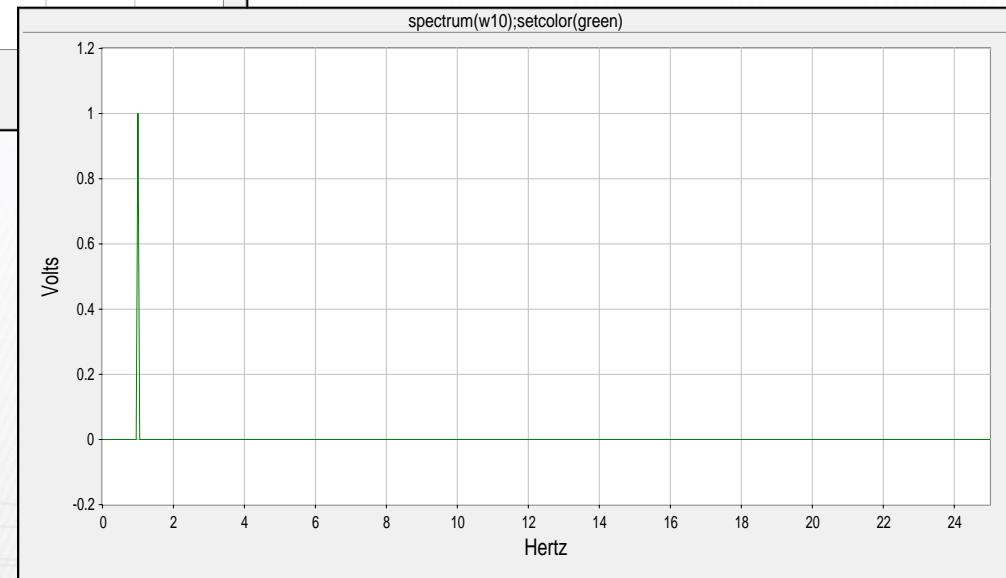
# 正弦波从时域到频域

$$s_a(t) = k_a + A_{a1} \cos(\omega_{a1} t + \phi_{a1}) + A_{a2} \cos(\omega_{a2} t + \phi_{a2}) + A_{a3} \cos(\omega_{a3} t + \phi_{a3}) + \dots$$

## 1-Hz 正弦时间函数



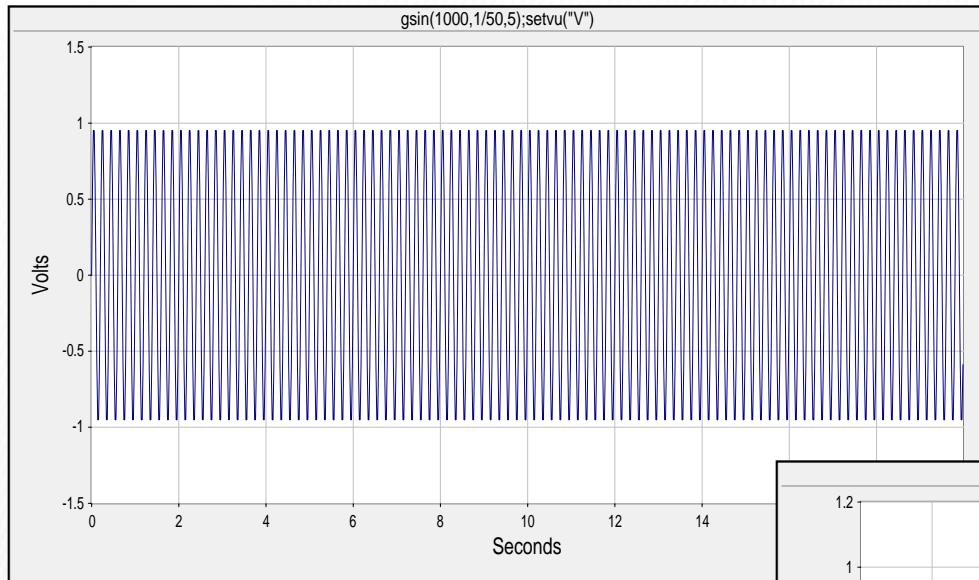
1-Hz 正弦时间函数  
在频域上的表达



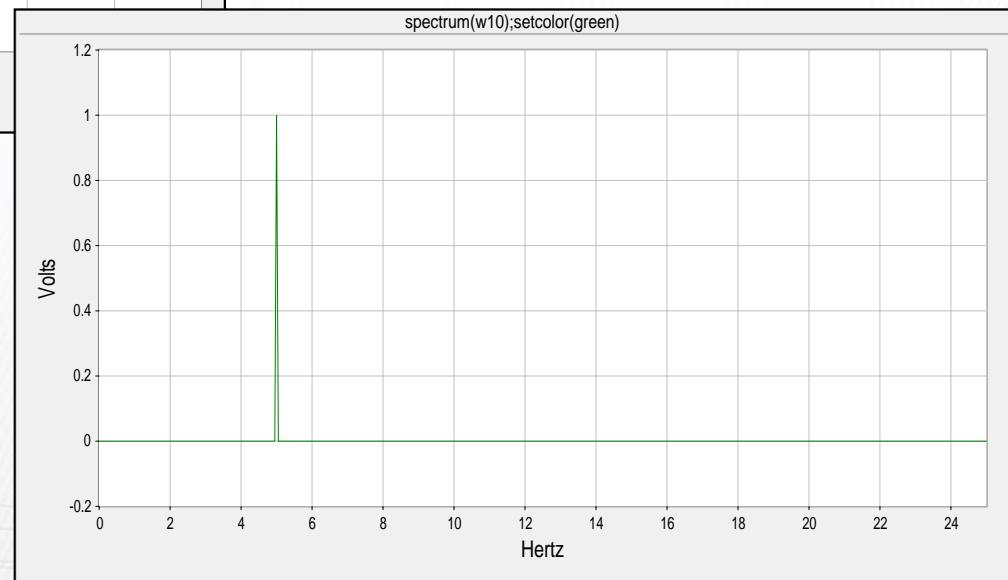
# 正弦波从时域到频域

$$s_a(t) = k_a + A_{a1} \cos(\omega_{a1} t + \phi_{a1}) + A_{a2} \cos(\omega_{a2} t + \phi_{a2}) + A_{a3} \cos(\omega_{a3} t + \phi_{a3}) + \dots$$

## 5-Hz 正弦时间函数

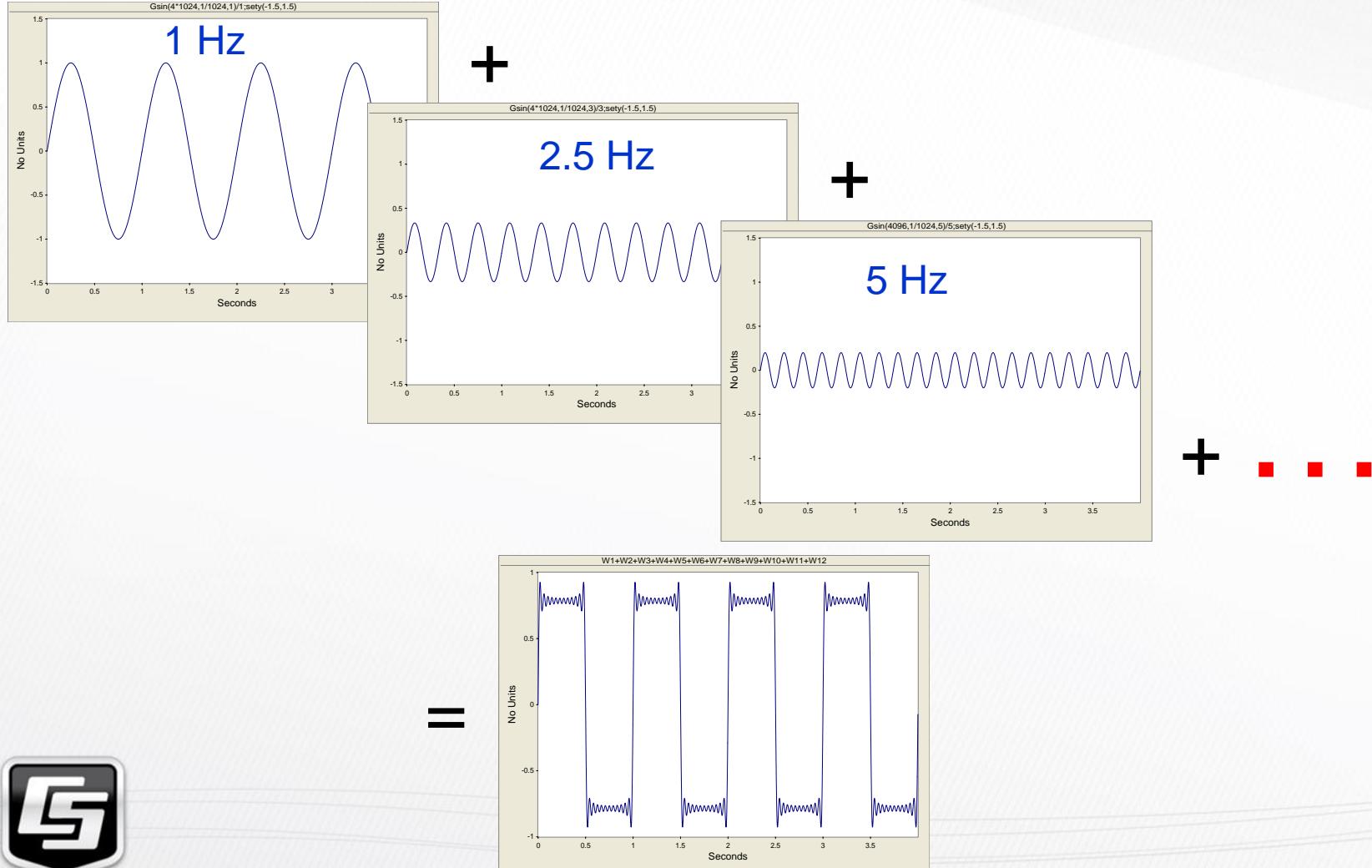


5-Hz 正弦时间函数  
在频域上的表达

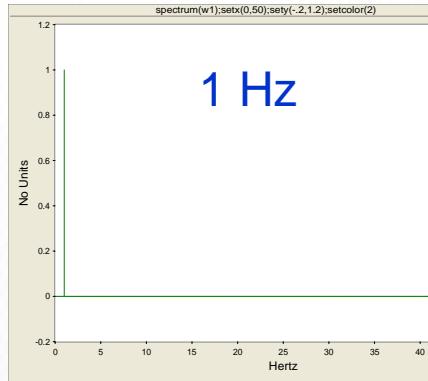


# 多个正弦时间函数的叠加

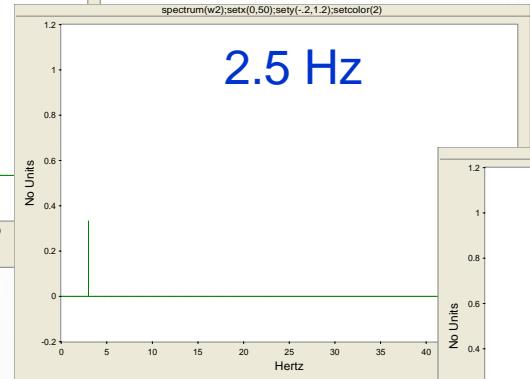
$$s_a(t) = k_a + A_{a1} \cos(\omega_{a1} t + \phi_{a1}) + A_{a2} \cos(\omega_{a2} t + \phi_{a2}) + A_{a3} \cos(\omega_{a3} t + \phi_{a3}) + \dots$$



# 多个正弦时间函数叠加后 在频域上的表达

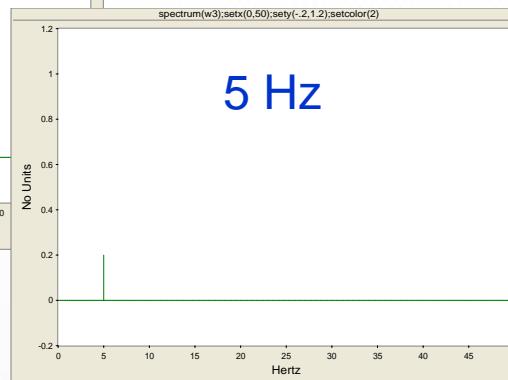


+



2.5 Hz

+

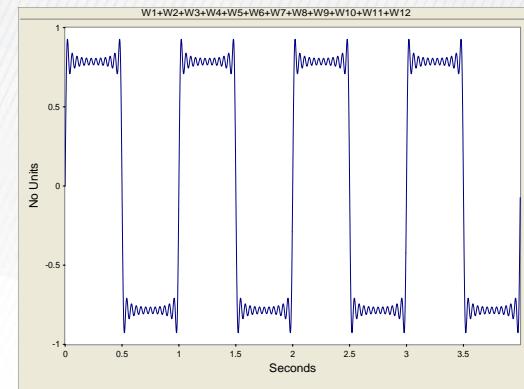
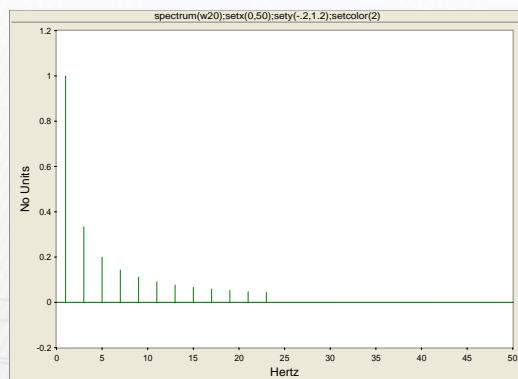


5 Hz

+



=



# 方差谱的分解

方差既可表达在时域上，也可表达在频域上（Parseval 定理）。

$$s_a(t) = k_a + A_{a_1} \cos(\omega_{a_1} t + \phi_{a_1}) + A_{a_2} \cos(\omega_{a_2} t + \phi_{a_2}) + A_{a_3} \cos(\omega_{a_3} t + \phi_{a_3}) + \dots$$

$$\text{var}(s_a) = \frac{A_{a_1}^2}{2} + \frac{A_{a_2}^2}{2} + \frac{A_{a_3}^2}{2} + \dots$$

方差是对能量谱密度函数在频域上的积分



# 方差是对能量谱密度函数在频域上的积分

自相关定义

$$R_{ww}(\tau) = \overline{w'(\textcolor{teal}{t})w'(\textcolor{teal}{t} + \tau)} = \lim_{T_p \rightarrow \infty} \frac{1}{2T_p} \int_{-T_p}^{T_p} w'(\textcolor{teal}{t})w'(\textcolor{teal}{t} + \tau) d\tau$$

傅立叶变换对

$$S_{ww}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} R_{ww}(\tau) e^{i\omega\tau} d\tau$$

$$R_{ww}(\tau) = \int_{-\infty}^{\infty} S_{ww}(\omega) e^{-i\omega\tau} d\omega = \int_{-\infty}^{\infty} S_{ww}(\omega) d\omega = \overline{w'(\textcolor{teal}{t})w'(\textcolor{teal}{t} + \tau)}$$

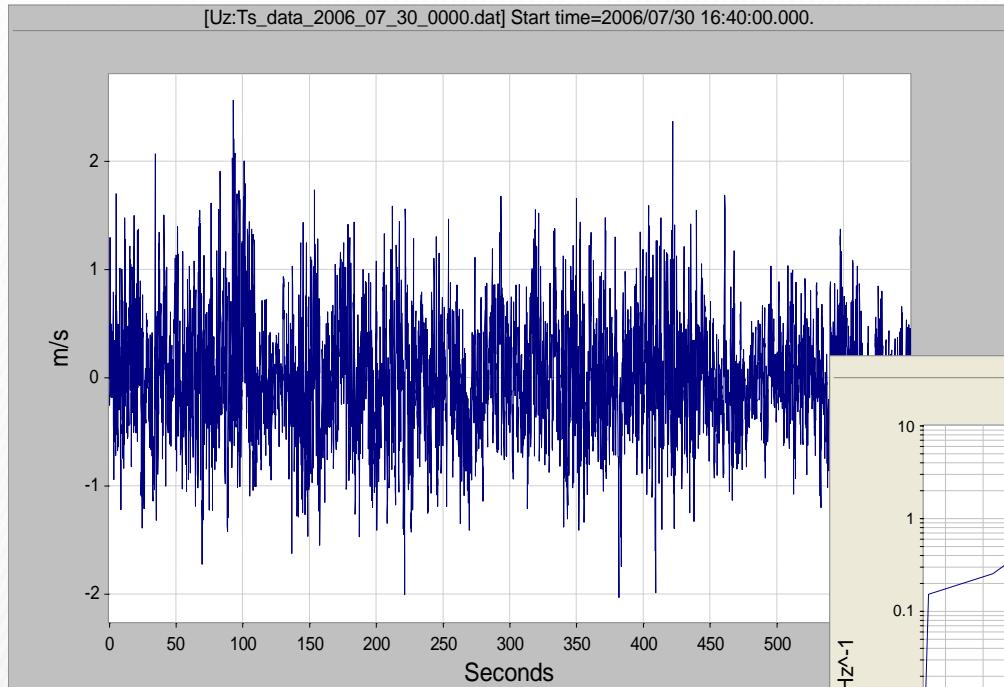
$$R_{ww}(0) = \int_{-\infty}^{\infty} S_{ww}(\omega) e^{-i\omega 0} d\omega = \int_{-\infty}^{\infty} S_{ww}(\omega) d\omega = \overline{w'(\textcolor{teal}{t})w'(\textcolor{teal}{t} + 0)} = \overline{\textcolor{blue}{w'}^2}$$

$$\overline{\textcolor{blue}{w'}^2} = \int_{-\infty}^{\infty} S_{ww}(\omega) d\omega$$

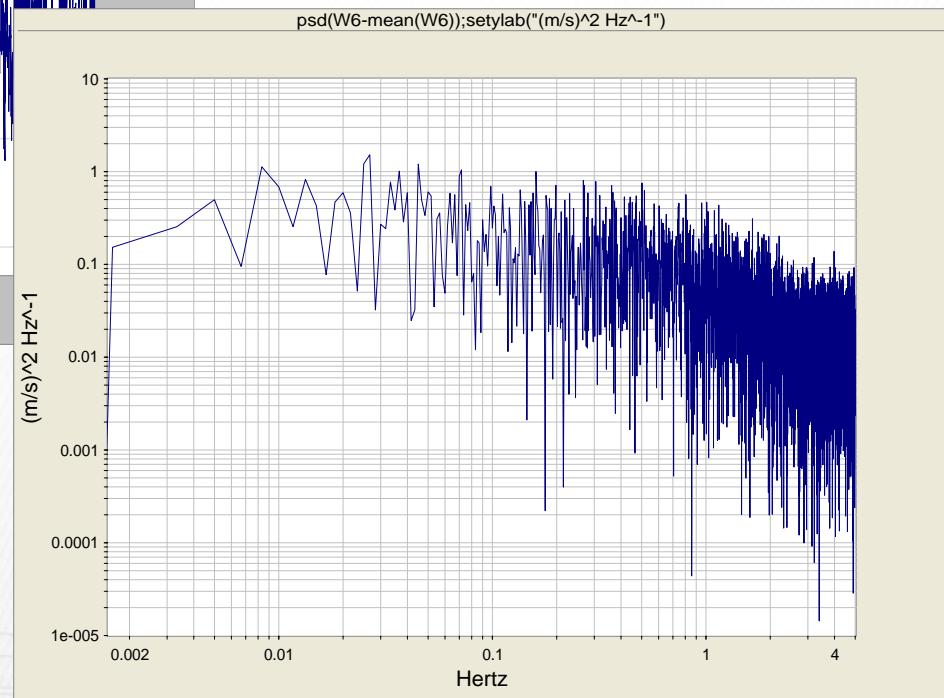


# 垂直风速

## 时域函数

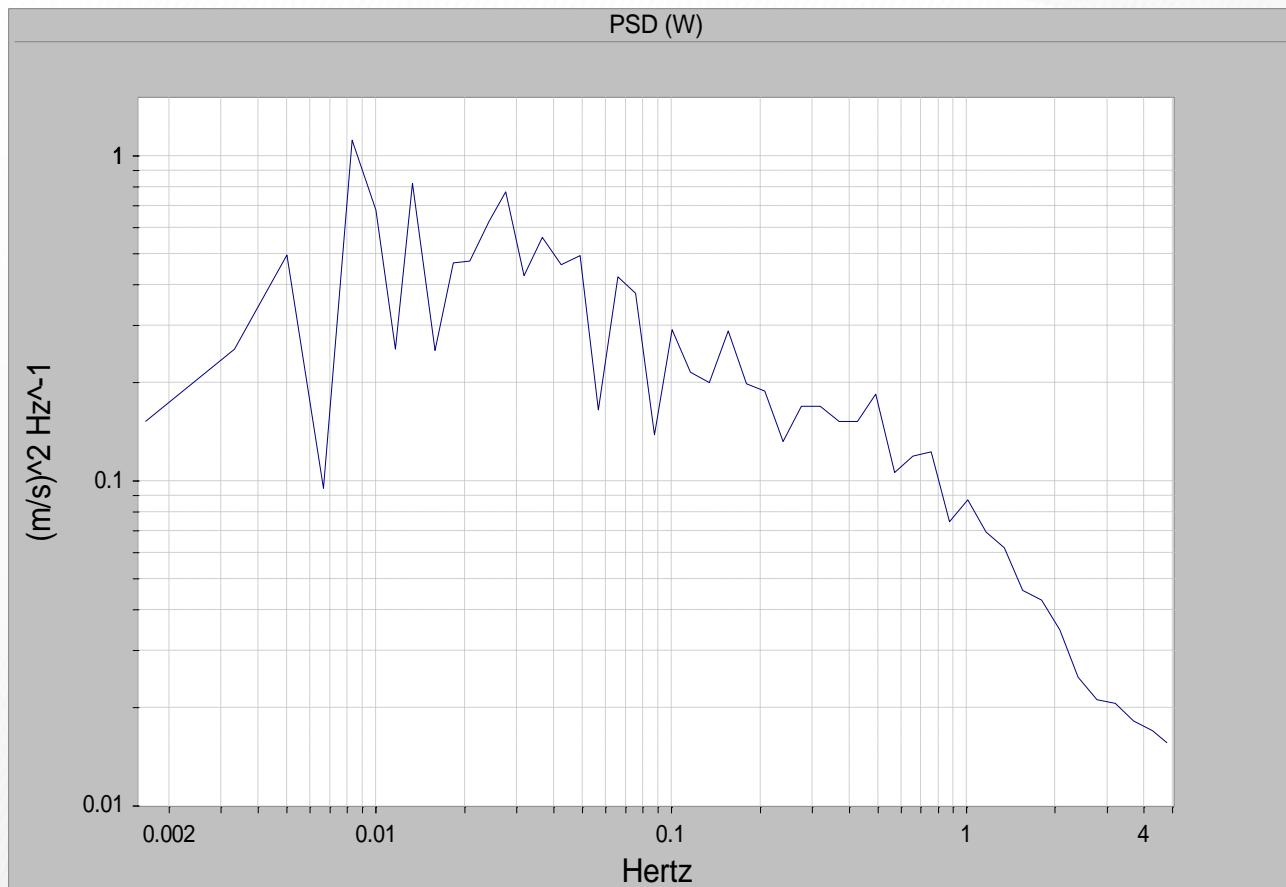


频域函数  
(phase not shown)



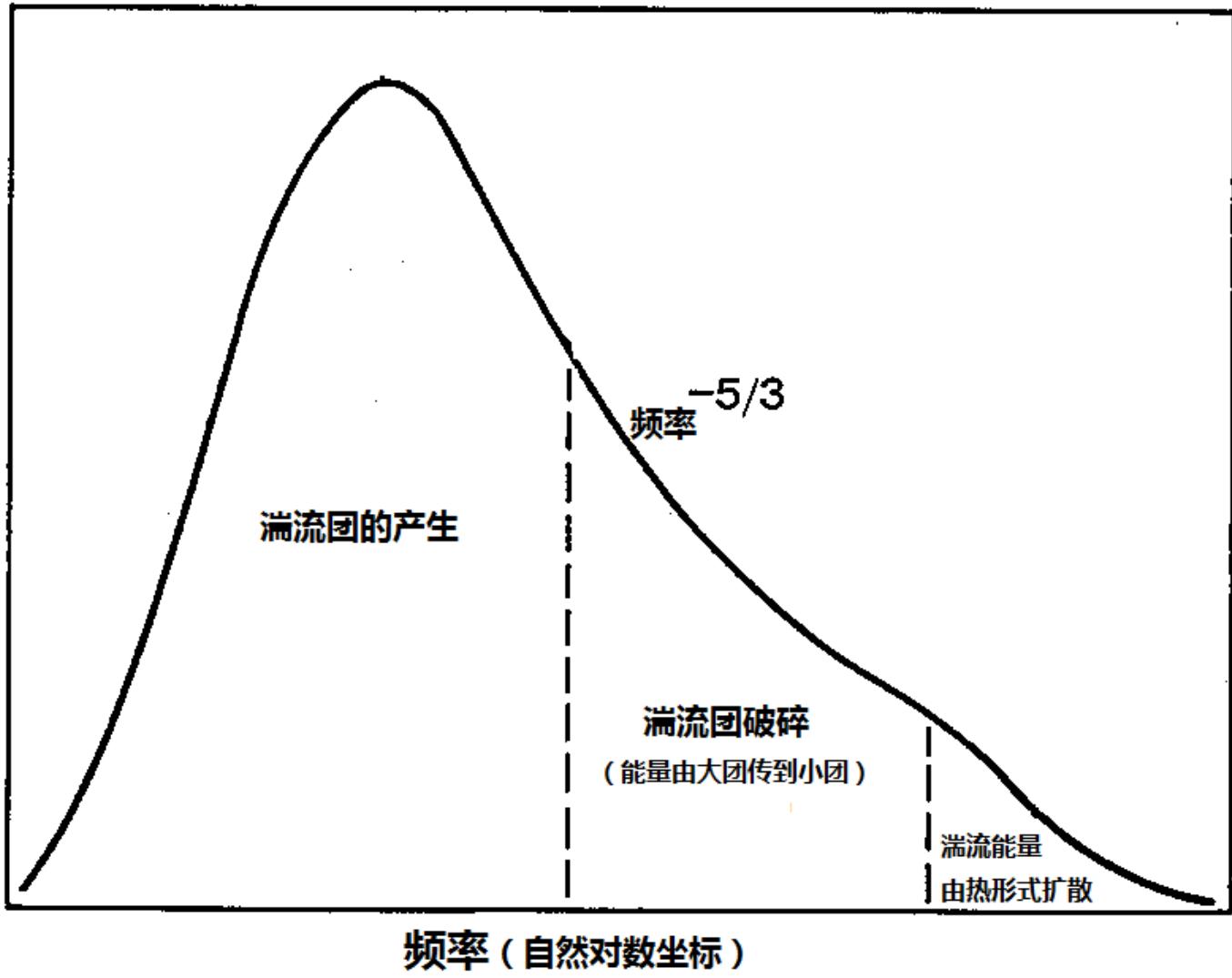
# 平滑的垂直风速能量谱

一般谱函数形状  
Kaimal 谱



## 湍流能量谱的一般形式

频率 x 能量谱



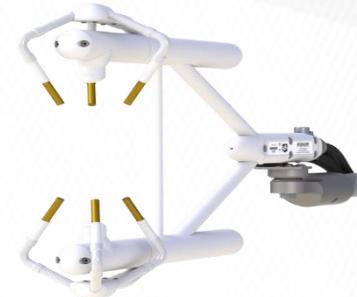
# 协方差也是对能量谱密度函数在频域上的积分

用自相关定义两个不同变量的相关

$$R_{\alpha w}(\mathbf{r}) = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + \mathbf{r})} = \lim_{T_p \rightarrow \infty} \frac{1}{2T_p} \int_{-T_p}^{T_p} \alpha'(\mathbf{x})w'(\mathbf{x} + \mathbf{r}) d\mathbf{r}$$

傅立叶变换对

$$S_{\alpha w}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} R_{\alpha w}(r) e^{i\omega r} dr$$



$$R_{\alpha w}(\tau) = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) e^{-i\omega\tau} d\omega = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + \tau)}$$

$$R_{\alpha w}(0) = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) e^{-i\omega 0} d\omega = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + 0)} = \overline{\alpha' w'}$$

$$\overline{\alpha' w'} = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega$$

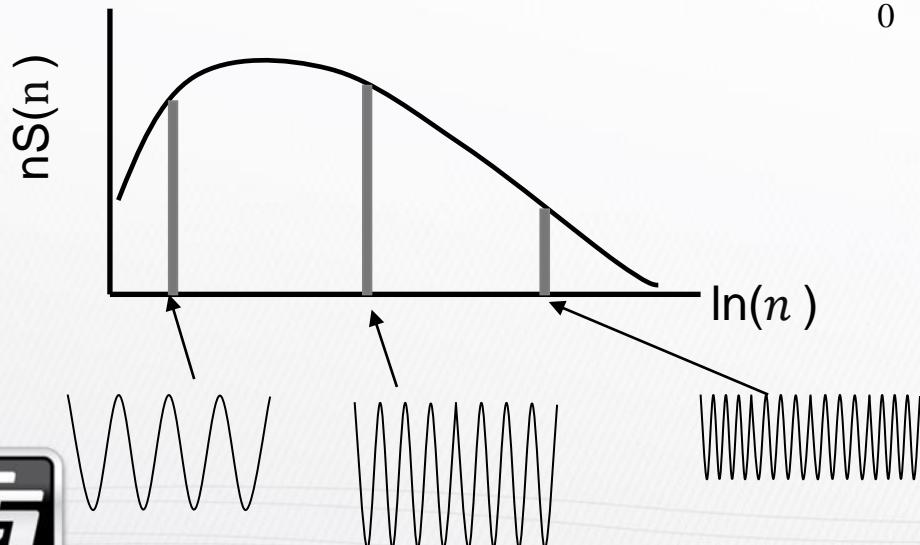


# 湍流谱和协湍流谱的一般形状

$$n = \frac{fz}{\bar{u}}, \quad f = \frac{\omega}{2\pi}$$

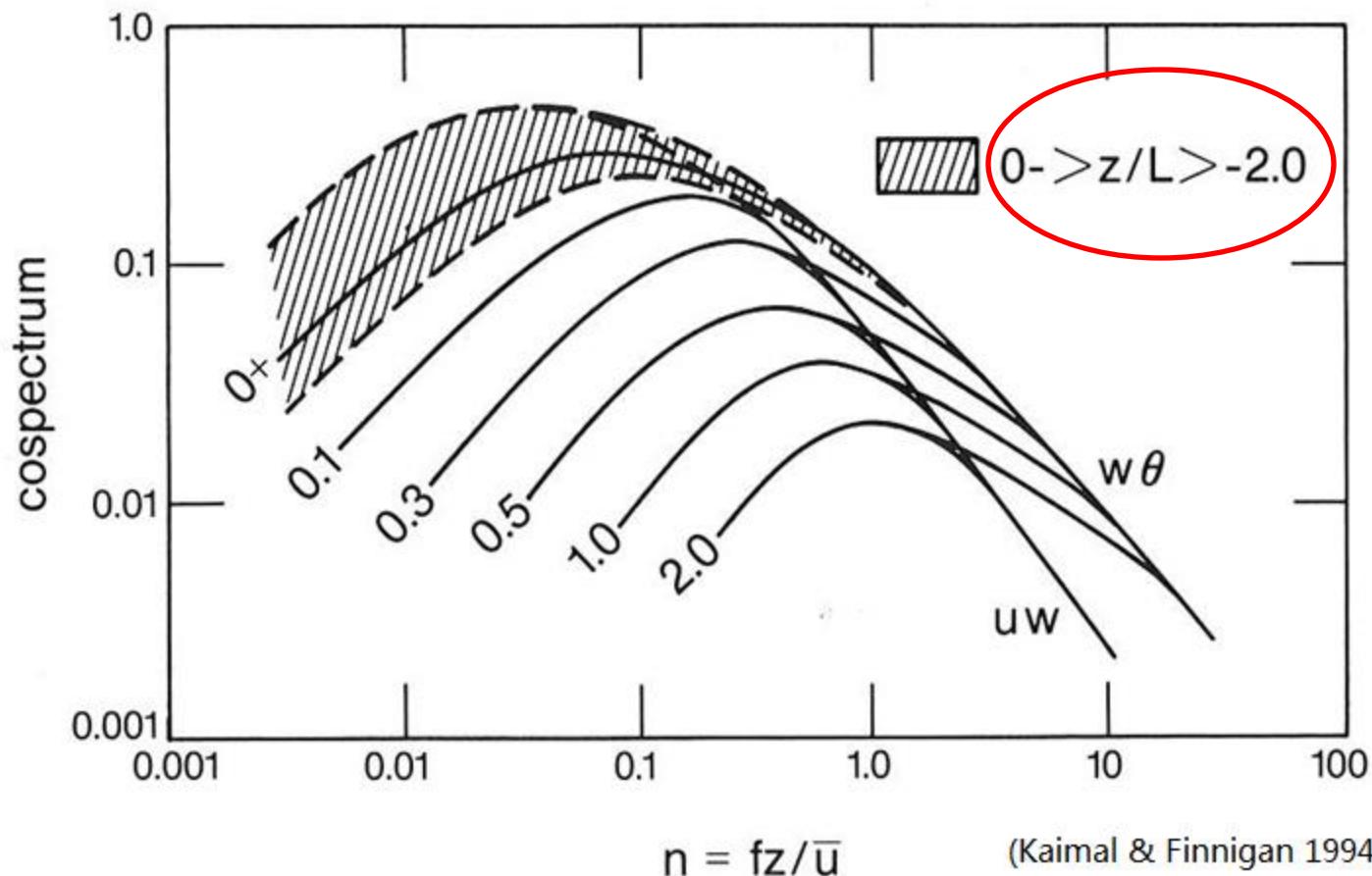
$$\text{variance} = \overline{T'^2} = \int_0^{\infty} nS_T(n) d\ln(n)$$

$$\text{covariance} = \overline{w'T'} = \int_0^{\infty} nC_{wT}(n) d\ln(n)$$



Larry Jacobsen, CSI

## 垂直风速与水平风速或温度 在近地面层不同稳定性下的协湍流谱



$$n = fz/\bar{u}$$

(Kaimal & Finnigan 1994)



# 协湍流谱

$$\frac{Z}{L} > 0$$

水平风速与垂直风速

$$fS_{uw}(f) = \frac{fz/\bar{u}}{A_{uw} + B_{uw}\left(\frac{fz}{\bar{u}}\right)^{2.1}}$$

$$A_{uw} = 0.124\left(1 + 7.9\frac{z}{L}\right)^{0.75}$$

$$B_{uw} = 23.252\left(1 + 7.9\frac{z}{L}\right)^{-0.825}$$

气温与垂直风速

$$fS_{Tw}(f) = \frac{fz/\bar{u}}{A_{Tw} + B_{Tw}\left(\frac{fz}{\bar{u}}\right)^{2.1}}$$

$$A_{Tw} = 0.284\left(1 + 6.4\frac{z}{L}\right)^{0.75}$$

$$B_{Tw} = 9.3447\left(1 + 6.4\frac{z}{L}\right)^{-0.825}$$



## 4. 湍流传输动量，热量及质量的规律



# 三个假设

## 雷诺平均运动方程 ( $u_1$ 方向)

1. 等高空间上的一致性

$$\frac{\partial}{\partial x_1} = 0 \quad \frac{\partial}{\partial x_2} = 0$$

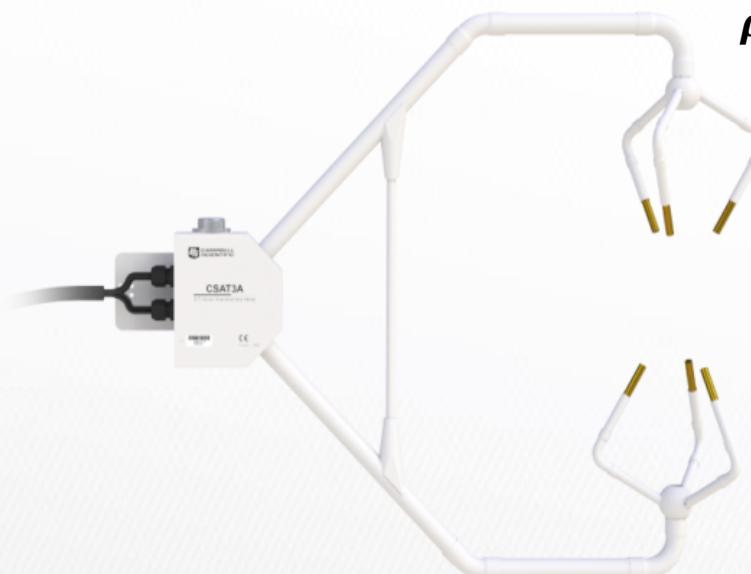
$$\frac{\partial \bar{u}_1}{\partial t} + \bar{u}_J \frac{\partial \bar{u}_1}{\partial x_J} = - \frac{\partial \bar{P}_1}{\rho_0 \partial x_1} + \frac{1}{\rho_0} \frac{\partial}{\partial x_J} \left( \mu \frac{\partial \bar{u}_1}{\partial x_J} - \rho_0 \bar{u}'_1 \bar{u}'_J \right) + \frac{\bar{T}_1}{T_0} g \delta_{31}$$

2. 时域上的稳定性

$$\frac{\partial}{\partial t} = 0$$

3. 干空气物质守恒

$$\bar{u}_3 = 0$$



$$\frac{1}{\rho_0} \frac{\partial}{\partial x_3} \left( \mu \frac{\partial \bar{u}_1}{\partial x_3} - \rho_0 \bar{u}'_1 \bar{u}'_3 \right) = 0$$

$$\mu \frac{\partial \bar{u}_1}{\partial x_3} - \rho_0 \bar{u}'_1 \bar{u}'_3 = \text{Constant}$$

$$\rho_0 \bar{u}'_1 \bar{u}'_3 = \text{Constant}$$

$$\frac{\text{kg}}{\text{m}^3} \quad \frac{\text{m}}{\text{s}} \quad \frac{\text{m}}{\text{s}}$$

$$\frac{\text{kg m/s}}{\text{m}^2 \text{s}}$$



# 常通量结论

纵向CO<sub>2</sub>, 水, 热通量是常量

$$\frac{\partial}{\partial w} \left( K_T \frac{\partial \bar{T}_1}{\partial w} - C_p \rho_0 \overline{w' T'}_1 \right) = 0$$

$$\frac{J}{^oC \text{kg}} \frac{\text{kg}}{\text{m}^3} \frac{m}{s} 0 C = \frac{J}{\text{m}^2 \text{s}}$$

$$\frac{\partial}{\partial w} \left( K_{co2} \frac{\partial \bar{\rho}_{co2}}{\partial w} - \overline{w' \rho'}_{co2} \right) = 0$$

$$\frac{m}{s} \frac{mg}{m^3} = \frac{mg}{m^2 s}$$

$$\frac{\partial}{\partial w} \left( K_{h2o} \frac{\partial \bar{\rho}_{h2o}}{\partial w} - \overline{w' \rho'}_{h2o} \right) = 0$$

$$\frac{m}{s} \frac{g}{m^3} = \frac{g}{m^2 s}$$



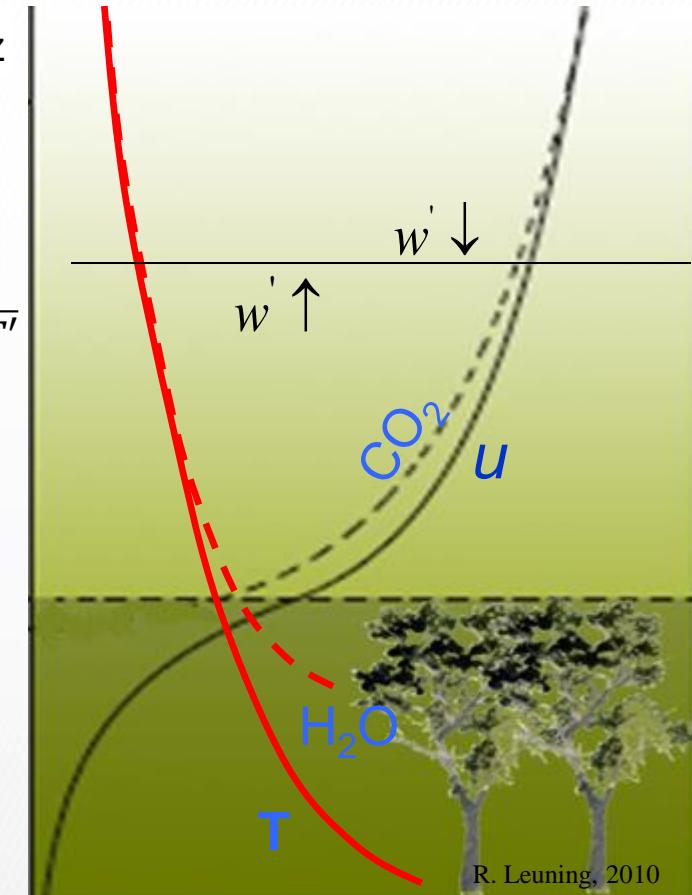
# Examples

$$\tau = \rho_0 \overline{w' u'}$$

$$H = C_p \rho_0 \overline{w' T'}$$

$$F_C = \overline{w' \rho'_{CO_2}}$$

$$E = \overline{w' \rho'_{H_2O}}$$



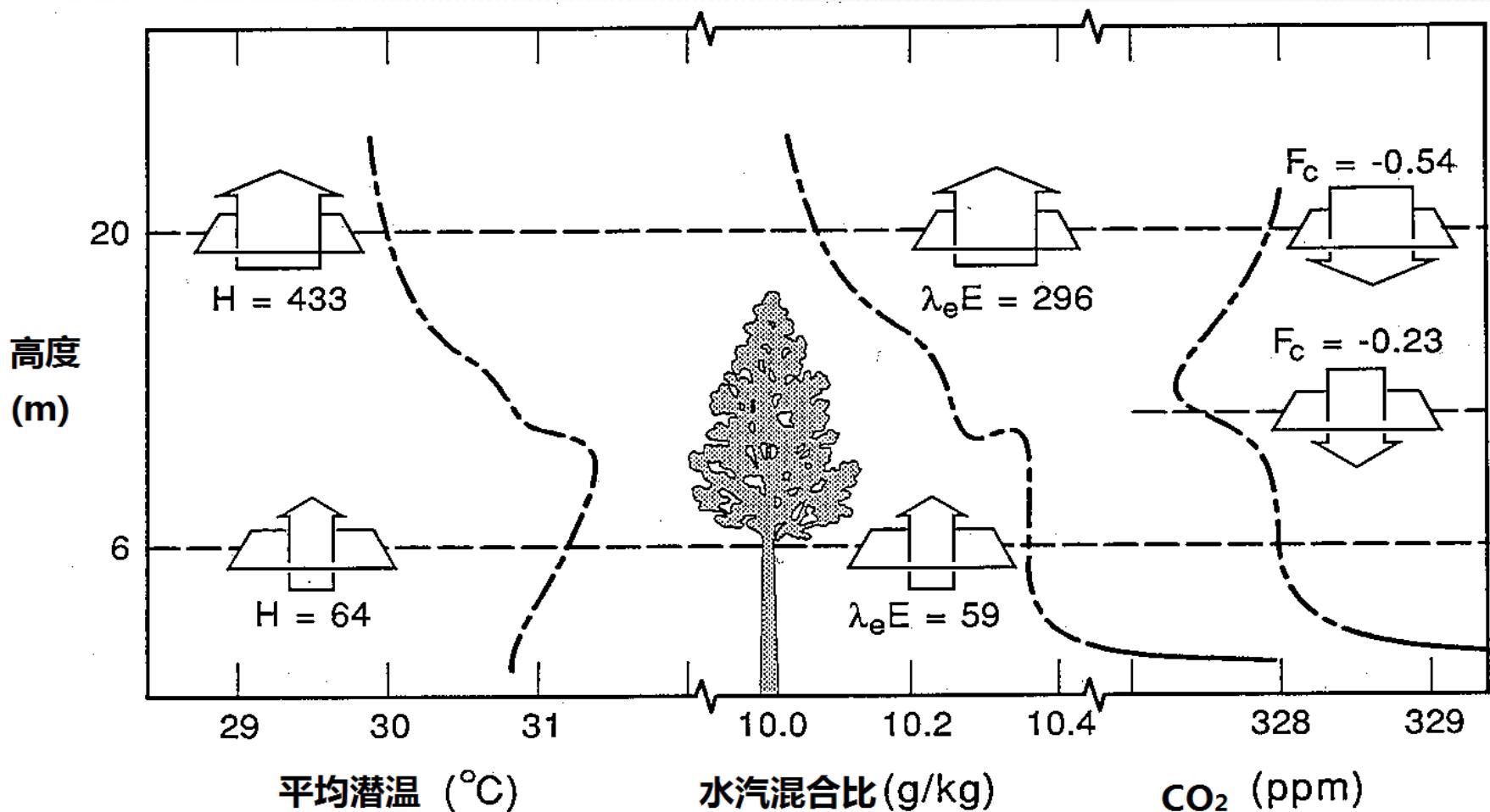
竖直风 m/s	$U'$ m/s	$T'$ °C	$\rho'_{CO_2}$ mg/m³	$\rho'_{H_2O}$ g/m³
上 $w'=0.1$	-1	1	-1	1
下 $w'=-0.1$	1	-1	1	-1
通量	$-0.2 \frac{kg\ m/s}{m^2\ s}$	$200 \frac{W}{m^2}$	$-0.2 \frac{mg}{m^2\ s}$	$0.2 \frac{g}{m^2\ s}$
	动量	热	CO <sub>2</sub>	H <sub>2</sub> O

$$\rho_0 \approx 1 \frac{kg}{m^3}, \quad C_p \approx 1000 \frac{J}{^oC\ kg}$$

e.g.  $\Delta t = 0.5$  s

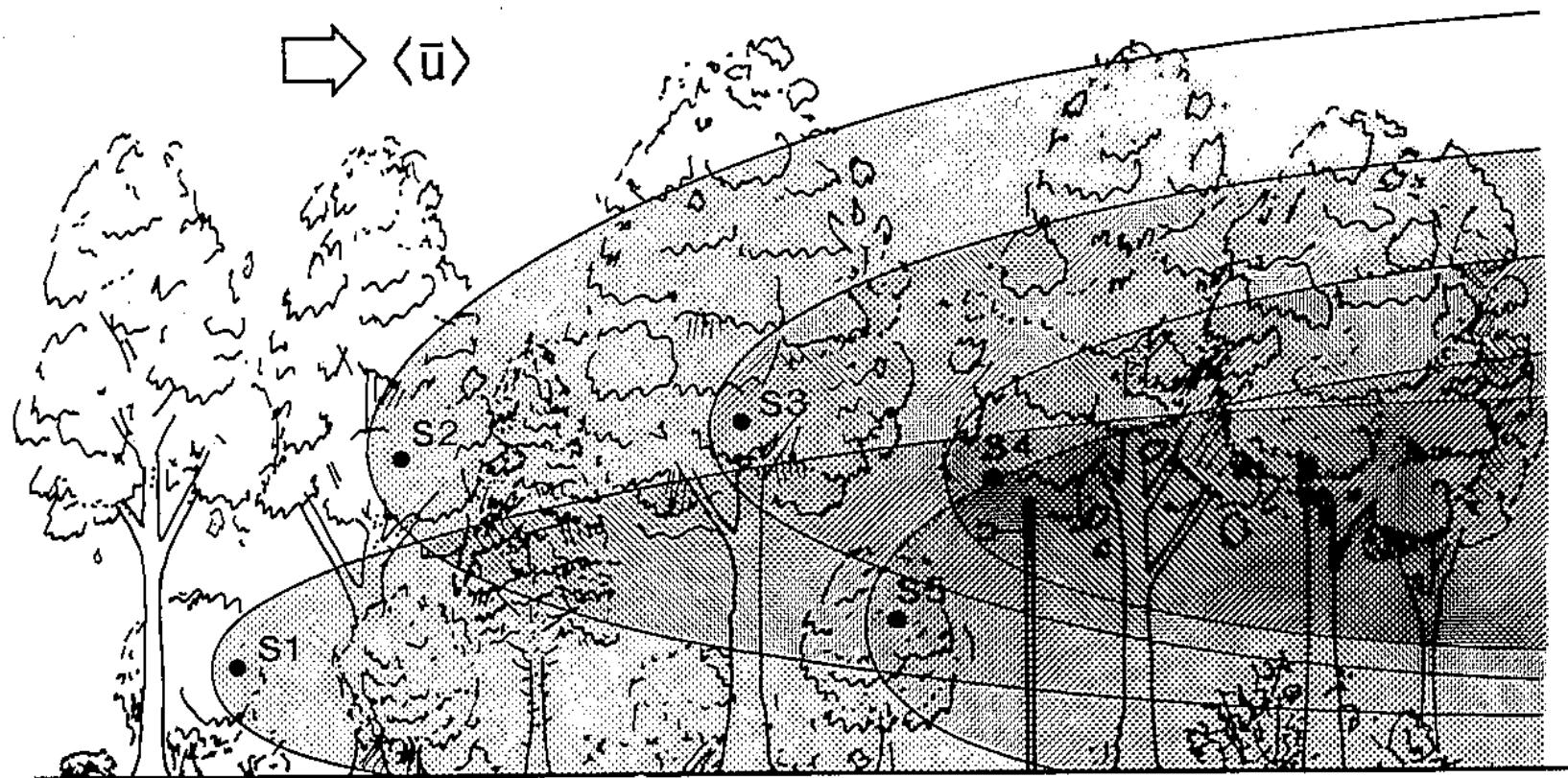


# 林下通量可逆梯度而行



Denmead & Bradley 1985

# 林内的质能源汇使林内通量复杂化



$$H = C_p \rho_0 \overline{w' T'}$$

$$F_{co2} = \overline{w' \rho'}_{co2}$$

$$E = \overline{w' \rho'}_{h2o}$$

## 严谨测定方法

### 依据：边界层流体物理学理论

#### 1. 传感器的野外安装

- a. 开阔域湍流场 (Fetch)
- b. 传感器的感源分布 (Footprint)
- c. 同时空测定
- d. 坐标旋转

#### 2. 传感器反应

- a. 传感器的敏感度
- b. 时间常数 (Time constant)
- c. 传输函数 (Transfer function)
- d. 测定路径和体积平均 (path length/volume averaging)
- e. 平均时长 (Low frequency issue)

#### 3. 测定频率 (Sampling frequency)

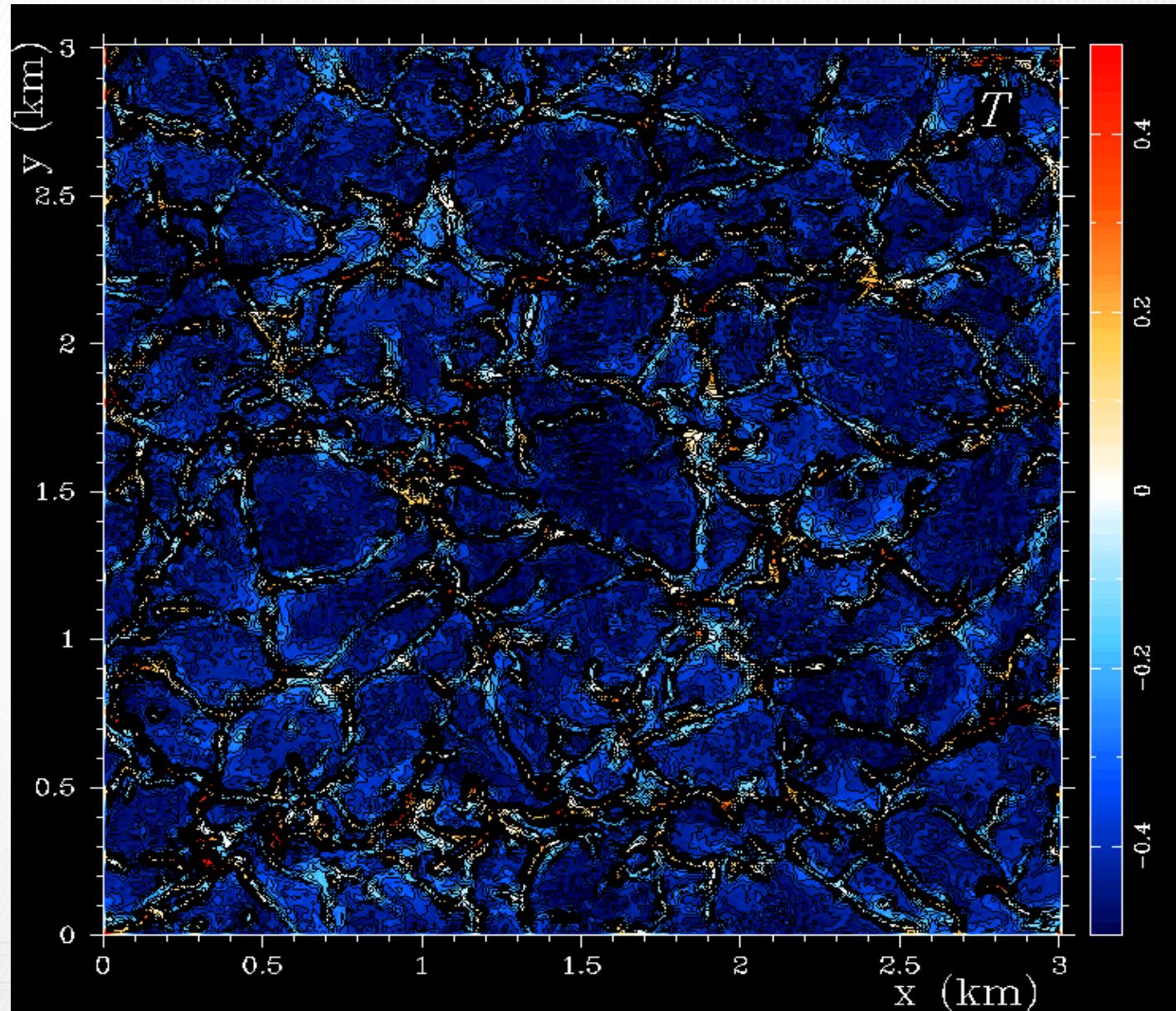
- 4. 高叠 (“杂”) 低现象 (Aliasing)
- 5. 超声感热通量订正 (SND correction)
- 6. 氧订正 (Oxygen correction)
- 7. 订正测定过程中空气密度的变化影响 (WPL correction)



# 1. 传感器的野外安装



# 空间异质性 (Spatial Heterogeneity)



# 协方差与其能量谱

协方差定义

$$R_{\alpha w}(\mathbf{r}) = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + \mathbf{r})}$$

傅立叶变换对

$$S_{\alpha w}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} R_{\alpha w}(\mathbf{r}) e^{i\omega \mathbf{r}} d\mathbf{r}$$

$$R_{\alpha w}(0) = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) e^{-i\omega 0} d\omega = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega$$

$$R_{\alpha w}(0) = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + 0)} = \overline{\alpha' w'}$$

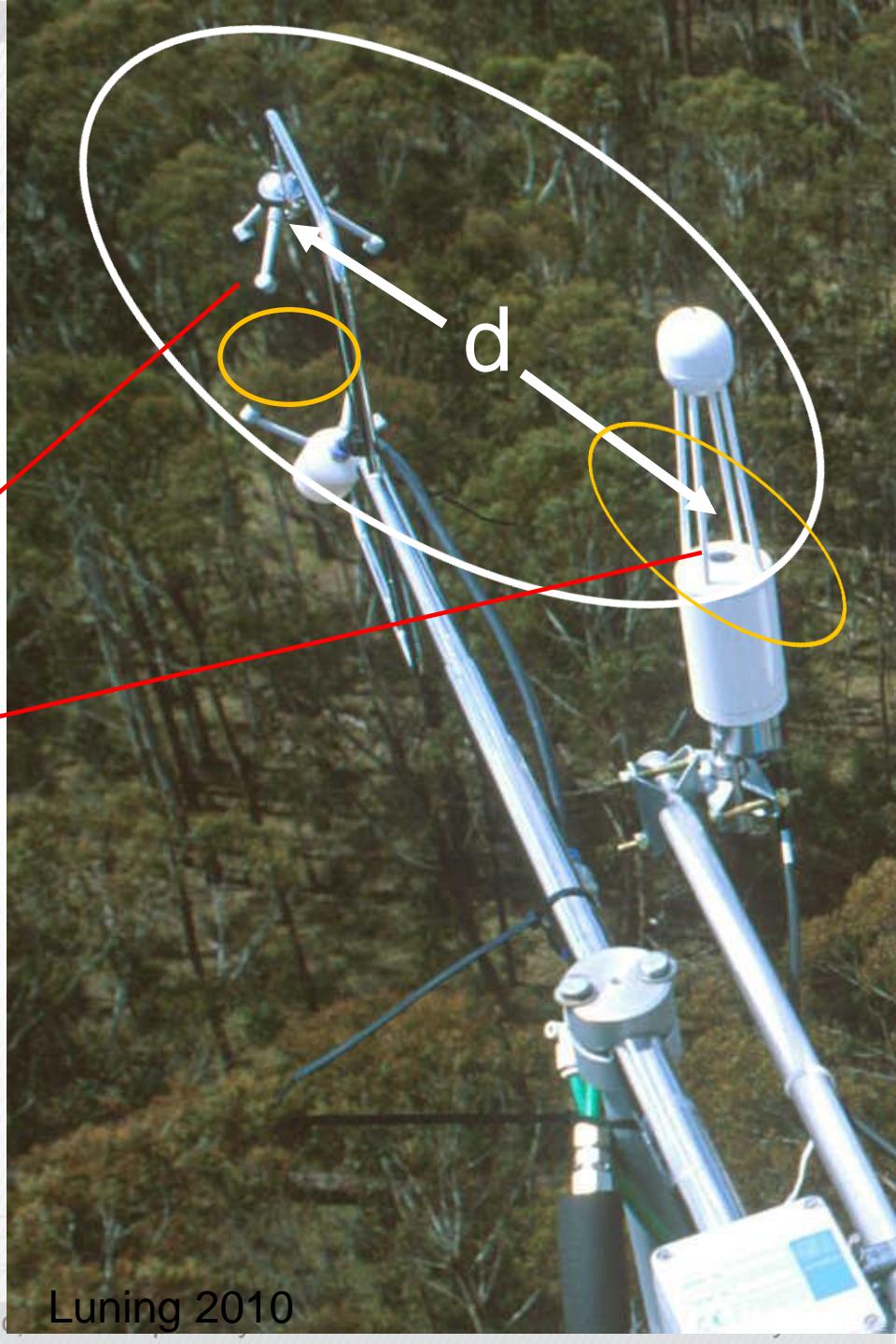
$$\overline{\alpha' w'} = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega$$



# 同时空测定

## 异空测定

- *loss of covariance*
- Samples eddies  $> \sim 2d$



# 协方差与其能量谱

协方差定义

$$R_{\alpha w}(\mathbf{r}) = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + \mathbf{r})}$$

傅立叶变换对

$$S_{\alpha w}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} R_{\alpha w}(\mathbf{r}) e^{i\omega \mathbf{r}} d\mathbf{r}$$

$$R_{\alpha w}(0) = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) e^{-i\omega 0} d\omega = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega$$

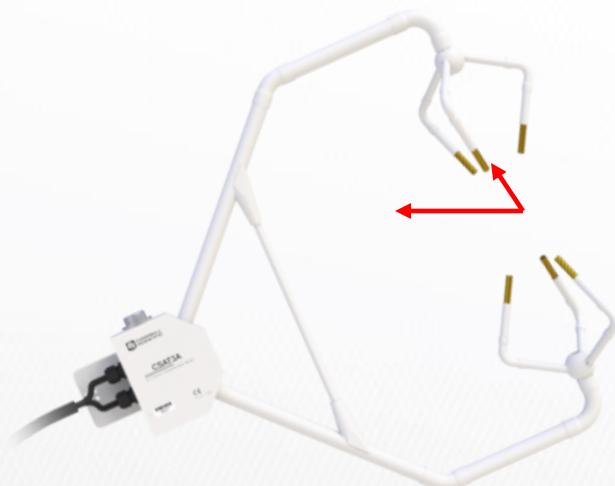
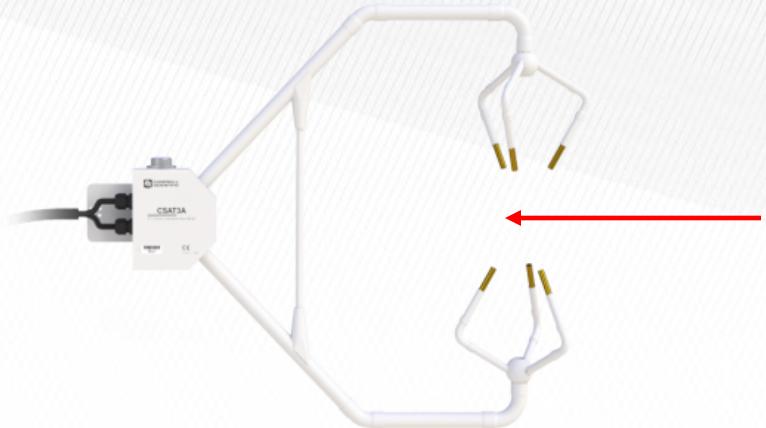
$$R_{\alpha w}(0) = \overline{\alpha'(\mathbf{x})w'(\mathbf{x} + \mathbf{0})} = \overline{\alpha' w'}$$

$$\overline{\alpha' w'} = \int_{-\infty}^{\infty} S_{\alpha w}(\omega) d\omega$$

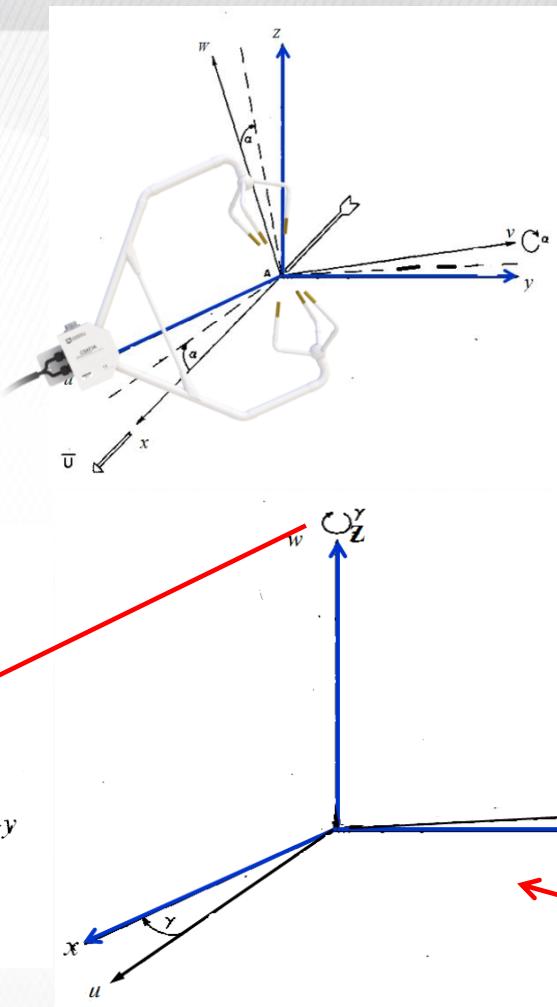


坐标旋转修正  
为什么?





# 仪器与风场坐标系

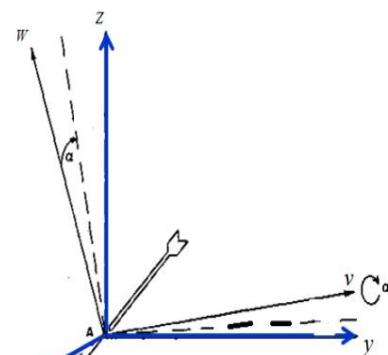
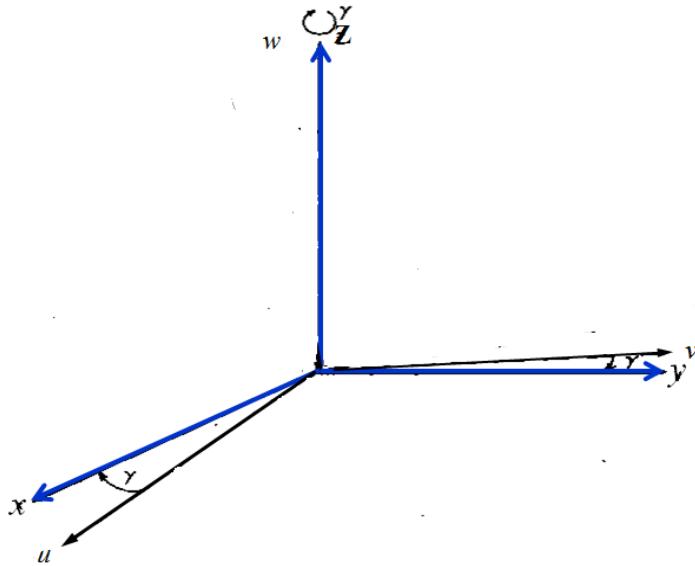


$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} \cos\gamma & -\sin\gamma & 0 \\ \sin\gamma & \cos\gamma & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\beta & -\sin\beta \\ 0 & \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} \cos\alpha & 0 & \sin\alpha \\ 0 & 1 & 0 \\ -\sin\alpha & 0 & \cos\alpha \end{bmatrix} \begin{bmatrix} u_m \\ v_m \\ w_m \end{bmatrix}$$



# 角度的计算

$$\gamma = \arctan\left(\frac{\bar{v}_m}{\bar{u}_m}\right)$$

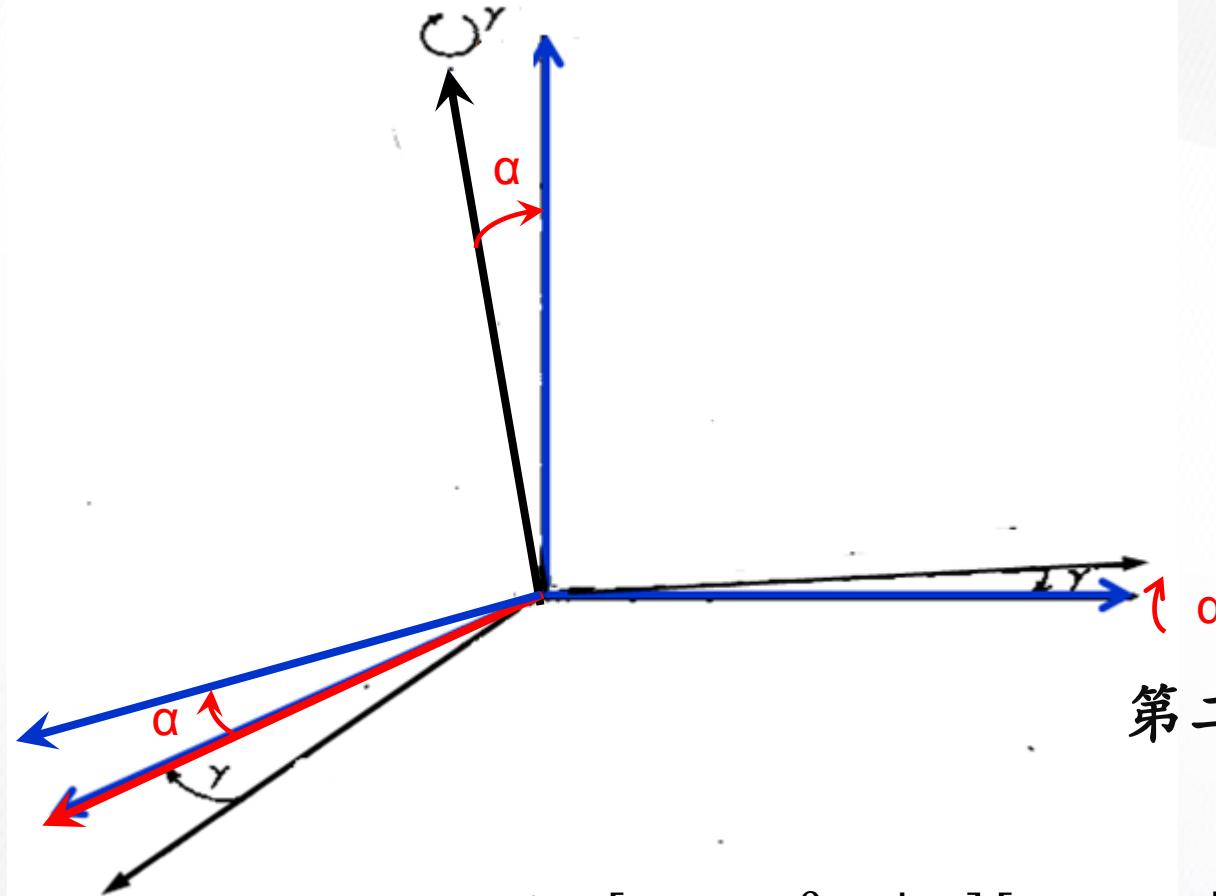


$$\alpha = -\arctan \frac{\bar{w}_1}{\bar{u}_1} = -\arctan \frac{\bar{w}_m}{\bar{u}_m \cos \gamma + \bar{v}_m \sin \gamma}$$



# 两次旋转

第一次旋转

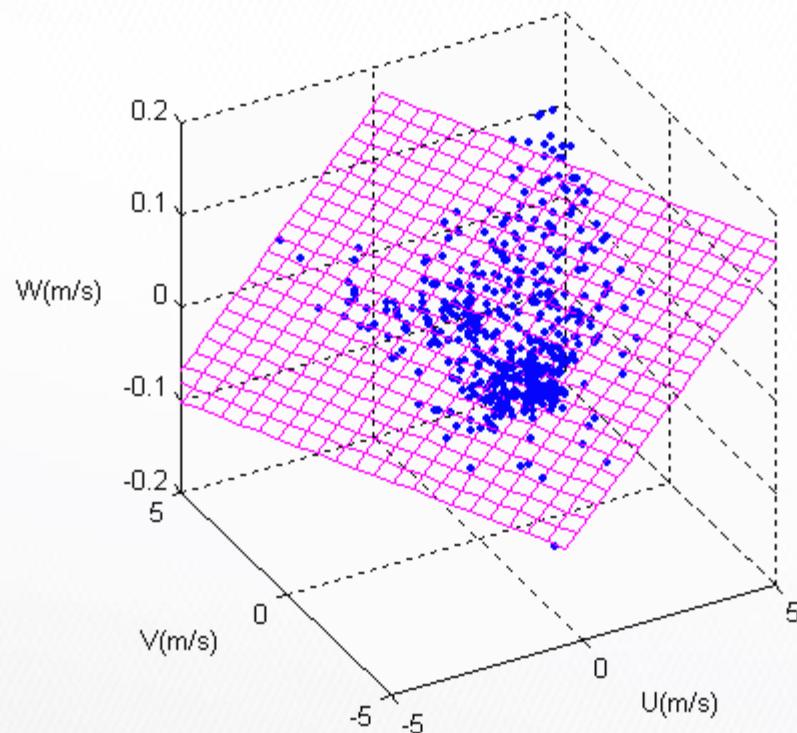


第二次旋转

$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} \cos\alpha & 0 & \sin\alpha \\ 0 & 1 & 0 \\ -\sin\alpha & 0 & \cos\alpha \end{bmatrix} \begin{bmatrix} \cos\gamma & -\sin\gamma & 0 \\ \sin\gamma & \cos\gamma & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u_m \\ v_m \\ w_m \end{bmatrix}$$



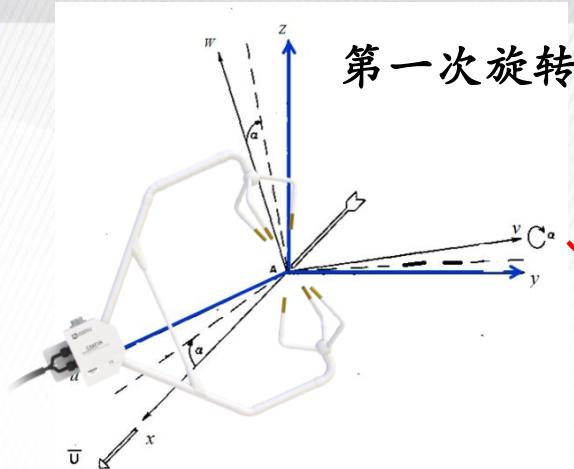
# 平面拟合坐标旋转角度计算



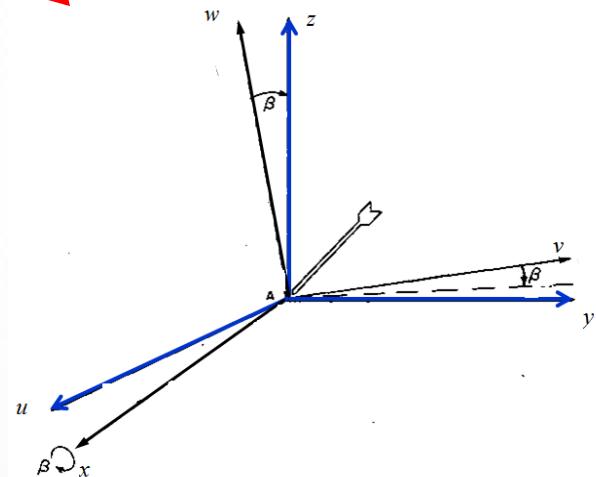
COORDINATE SYSTEM ROTATED ABOUT THIS PLANE



# 平面拟合 坐标旋转

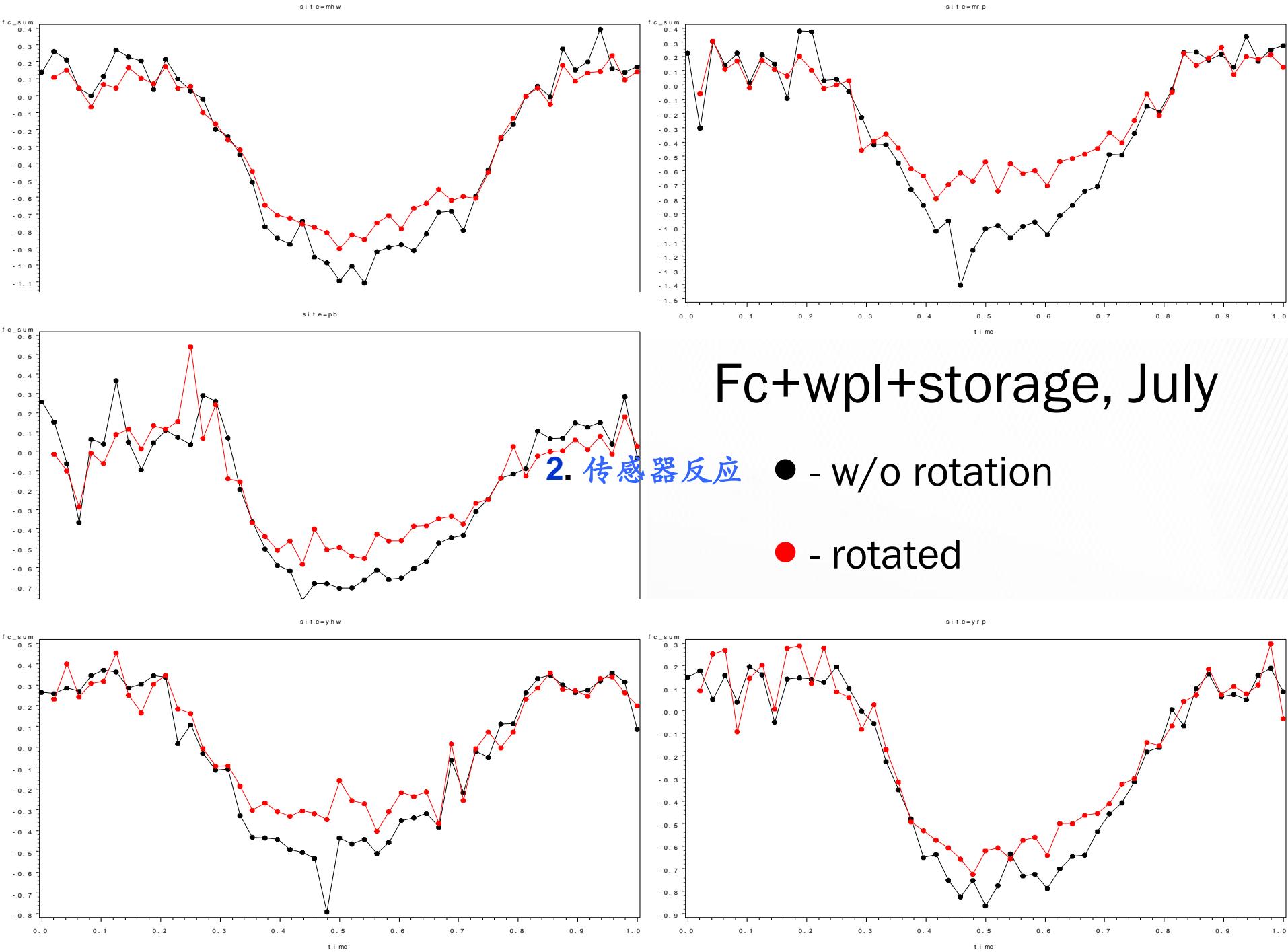


第一次旋转



$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\beta & -\sin\beta \\ 0 & \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} \cos\alpha & 0 & \sin\alpha \\ 0 & 1 & 0 \\ -\sin\alpha & 0 & \cos\alpha \end{bmatrix} \begin{bmatrix} u_m \\ v_m \\ w_m \end{bmatrix}$$

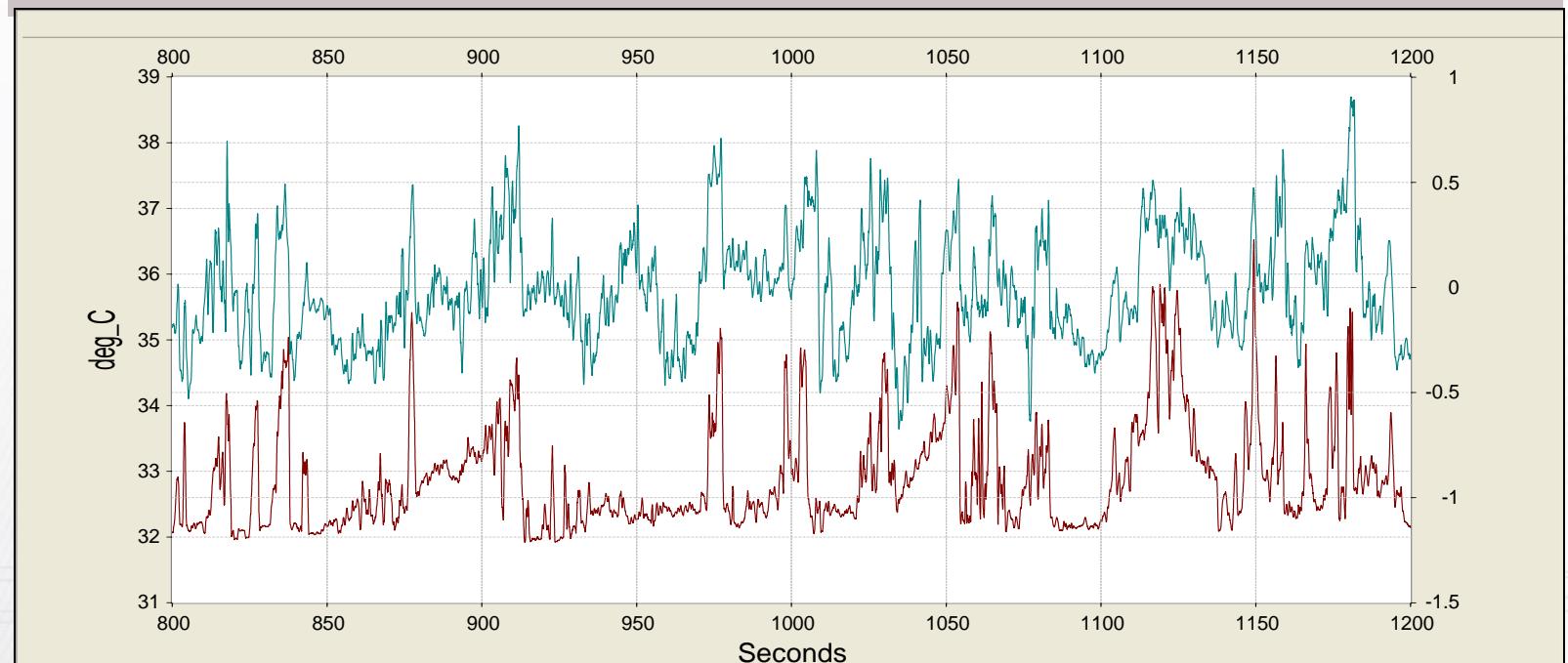
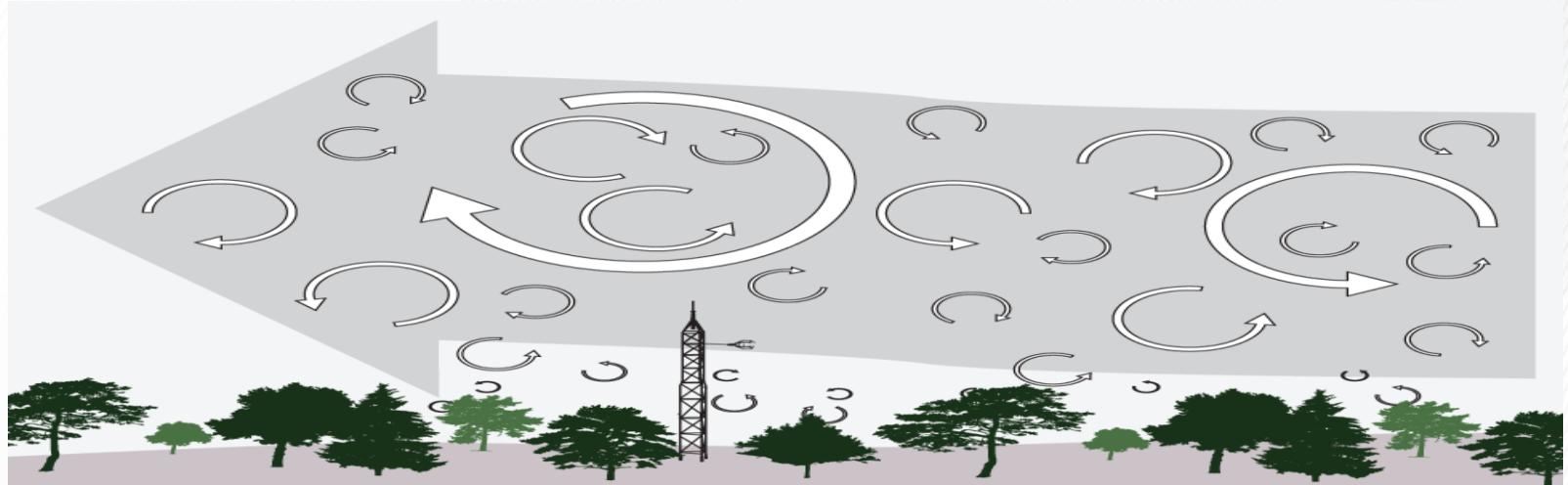




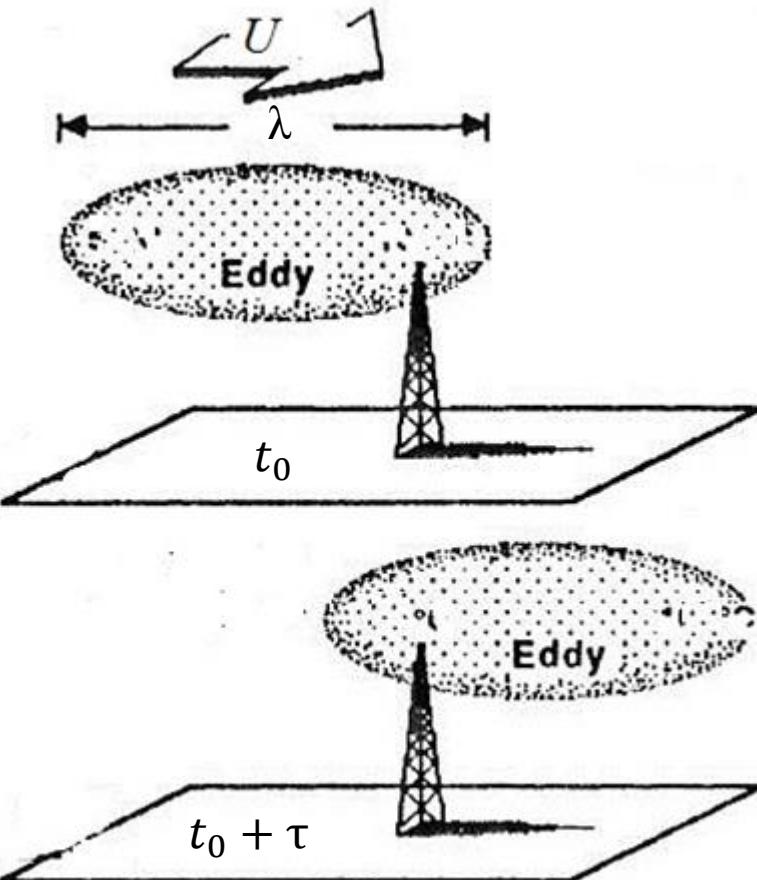
## 2. 传感器反应



# 订正测定中高频遗漏通量



## 湍流团的大小与频率



$$\text{周期 } (\tau) = \frac{\text{波长 } (\lambda)}{\text{风速 } (U)} = \frac{1}{\text{频率 } (f)}$$

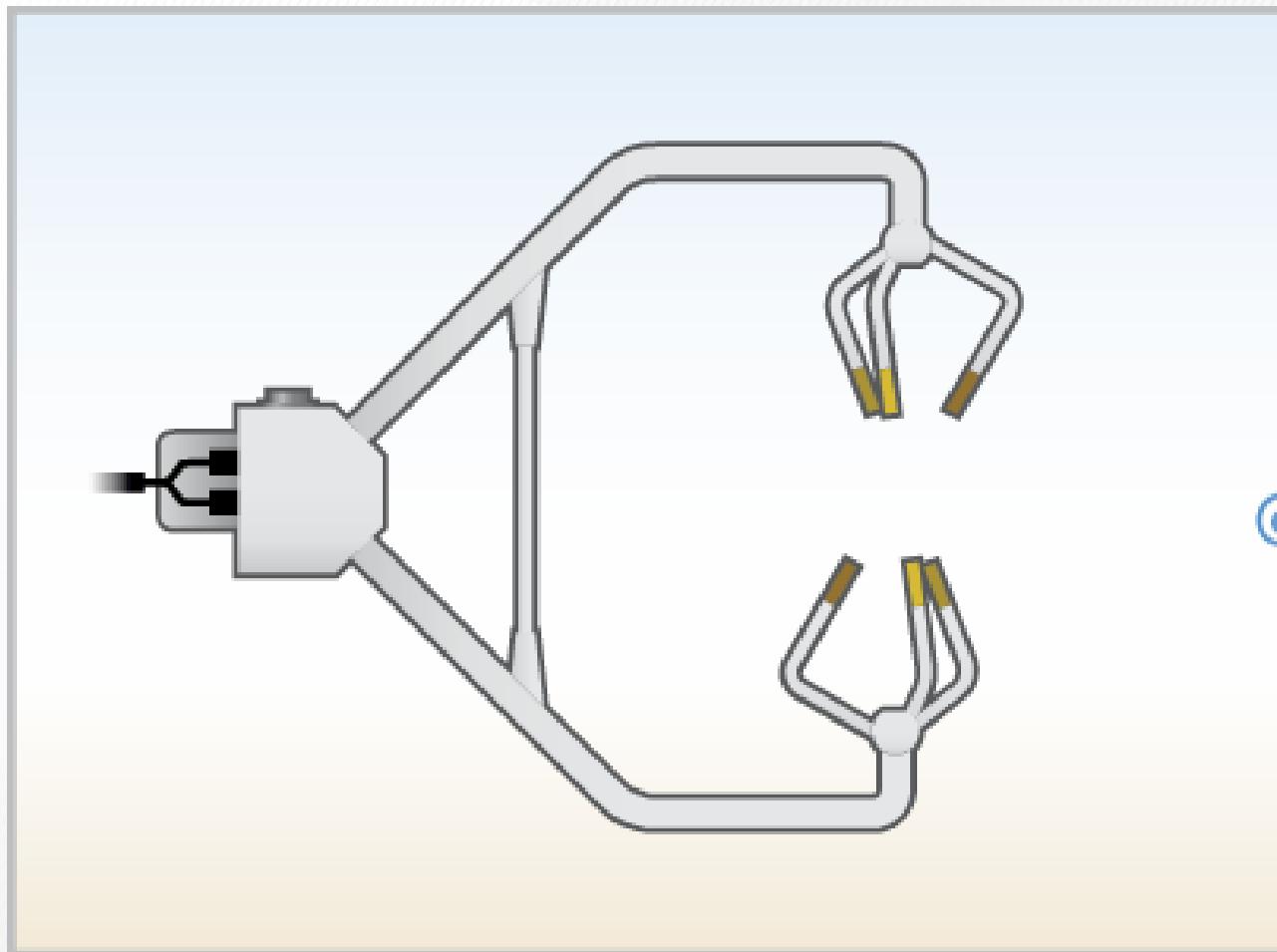
$f$  - 转动频率 ( $\frac{\text{圈}}{\text{秒}}$ )

$$k = \frac{2\pi f}{\bar{u}} \quad \text{波数 } (\frac{\text{圈}}{\text{米}})$$

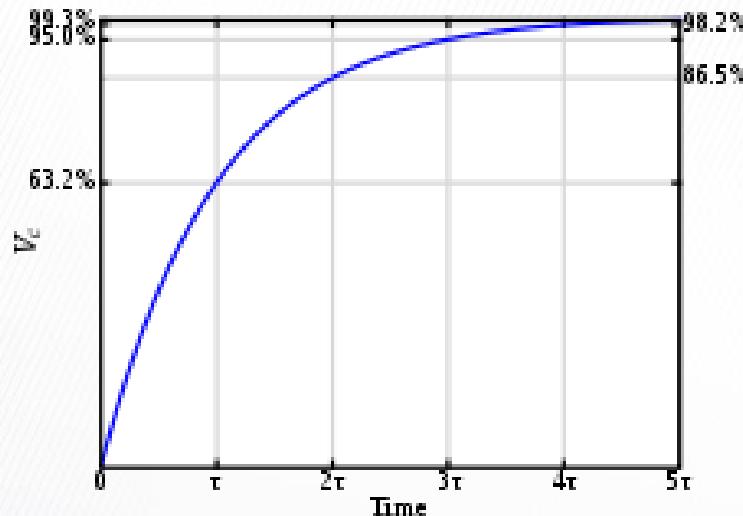
$$\omega = 2\pi f \quad \text{角频率 } \left( \frac{\text{弧度}}{\text{秒}} \right)$$



# 传感器结构与高频湍流团



# 时间常数 ( $\tau$ ) 的定义



时间常数( $\tau_{FW}$ )

传感器感应到63.2%被测物理量所需的时间。

$$\frac{dT_m(t)}{dt} = \frac{T(t) - T_m(t)}{\tau}$$

$T(t)$  时间  $t$  时的被测温度

$T_m(t)$  时间  $t$  时传感器测得的温度



# 传感器反应速度与湍流团频率

$$\tau = 0.167 D^2 \frac{\rho_a C}{k_a \text{Nu}}$$

$D$  dimension

$\rho_a$  material density of thermocouple

$C$  specific heat of thermocouple materials

$k_a$  thermal conductivity of air

$\text{Nu}$  Nusselt number



# 传输函数 (Transfer function)

—具有时间常数  $\tau$  的传感器对不同频率信号（如温度）的相对反应。  
是频率的函数。  
函数值从 1 到 0。1 是完全反映，0 没反应



$$\frac{dT_m(t)}{dt} = \frac{T(t) - T_m(t)}{\tau}$$

$T(t)$  时间 $t$ 时的被测温度

$T_m(t)$  时间 $t$ 时传感器测得的温度



# 基本例子：传输函数

对时间常数定义方程两端做傅立叶变换

$$\mathcal{F}\left(\frac{dT_m(\textcolor{teal}{t})}{dt}\right) = \mathcal{F}\left(\frac{T(\textcolor{teal}{t}) - T_m(\textcolor{teal}{t})}{\tau}\right)$$

即

$$-j\omega T_m(\omega) = \frac{1}{\tau} [T(\omega) - T_m(\omega)]$$

$\omega$  - 频率,  $j = \sqrt{-1}$ .

整理得

$$\frac{T_m(\omega)}{T(\omega)} = \frac{1}{1 - j\tau\omega}$$



1.1

1

0.9

0.8

0.7

0.6

0.5

0.4

0.3

0.2

0.1



0

0.000001

0.00001

0.0001

0.001

0.01

0.1

1

10

100

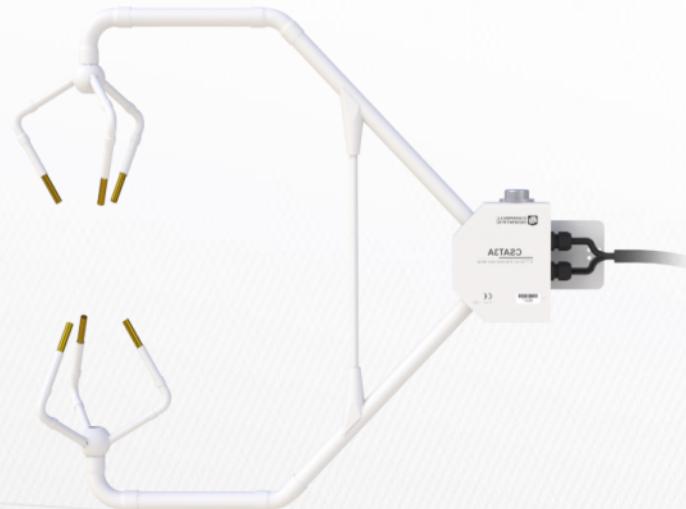
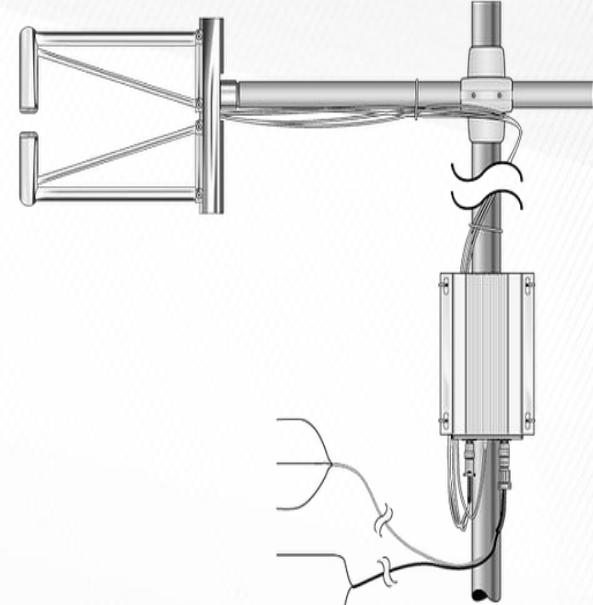
1000

10000

$$T_{TT\_TC}(f, \tau_{FW}) = \frac{1}{1 + (2\pi f \tau_{FW})^2}$$

# 测定路径/体积平均

(path length/volume averaging)



# 垂直风速路径平均频率反应近似函数

1.1

1

0.9

0.8

0.7

0.6

0.5

0.4

0.3

0.2

0.1

0



0.000001 0.00001 0.0001 0.001 0.01 0.1 1 10 100 1000 10000

$$T_{ww\_LA}(f, p, u) = \frac{2}{\pi f p / u} \left( 1 + \frac{\exp(-2\pi \frac{p}{u} f)}{2} - \frac{3 \left[ 1 - \exp(-2\pi \frac{p}{u} f) \right]}{4\pi f p / u} \right)$$

# 标量路径平均频率反应近似函数

$$T_{ss-LA}^{0.6}(n, p, u) = \frac{1}{2\pi fp/u} \left( 3 + \exp(-2\pi \frac{p}{u} f) - \frac{4 \left[ 1 - \exp(-2\pi \frac{p}{u} f) \right]}{2\pi fp/u} \right)$$



# CSAT超声热通量路径平均频率反应函数 Dijk (2002)

1.1

1

0.9

0.8

0.7

0.5

0.4

0.3

0.2

0.1

0

0.000001

0.00001

0.001

0.01

0.1

1

10

100

1000

10000



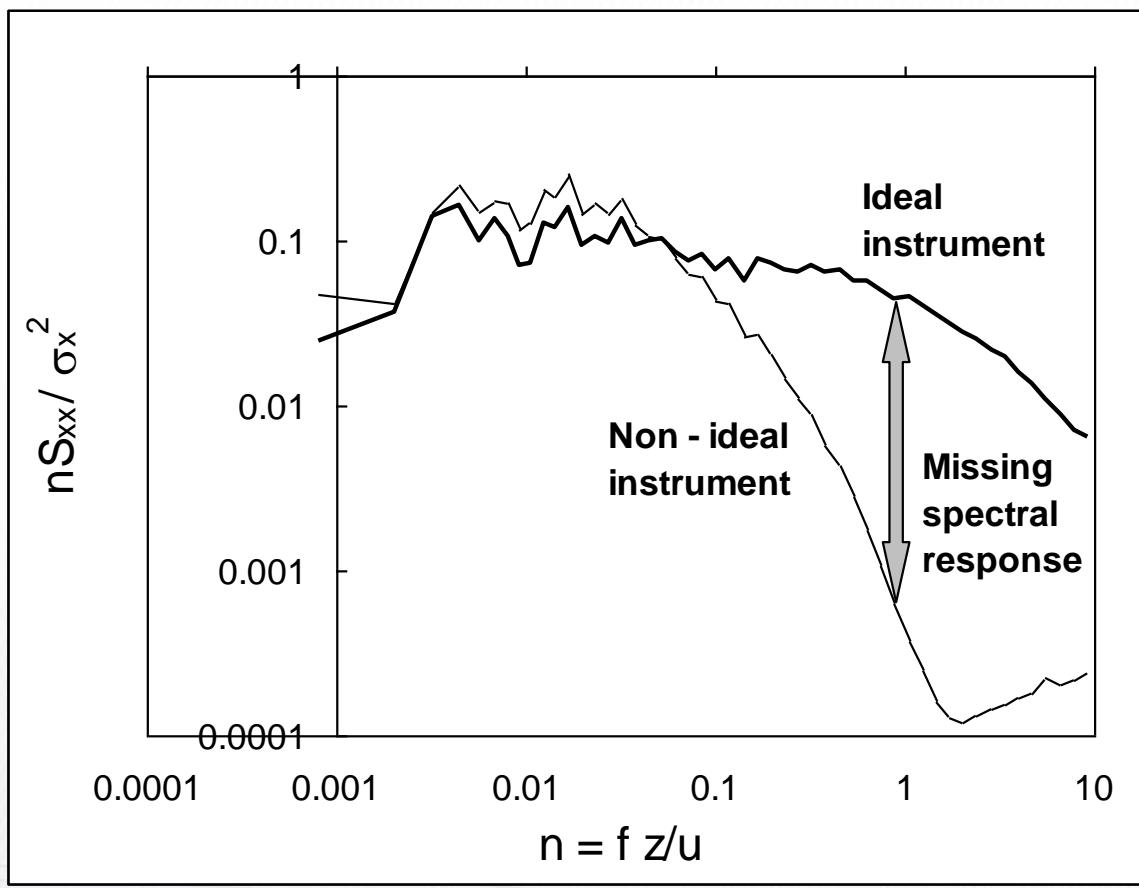
$$T(k) = \frac{1}{\beta z w S(|k|z)^{-7/3}} \int_0^\infty \int_0^{2\pi} KA \frac{k^2 + K^2 \sin^2 \theta}{\sqrt{k^2 + K^2}} \times \frac{1}{3} \left[ \sin c\left(\frac{\mathbf{k} \cdot \mathbf{I}_a}{2}\right) + \sin c\left(\frac{\mathbf{k} \cdot \mathbf{I}_b}{2}\right) + \sin c\left(\frac{\mathbf{k} \cdot \mathbf{I}_c}{2}\right) \right] d\theta dK$$

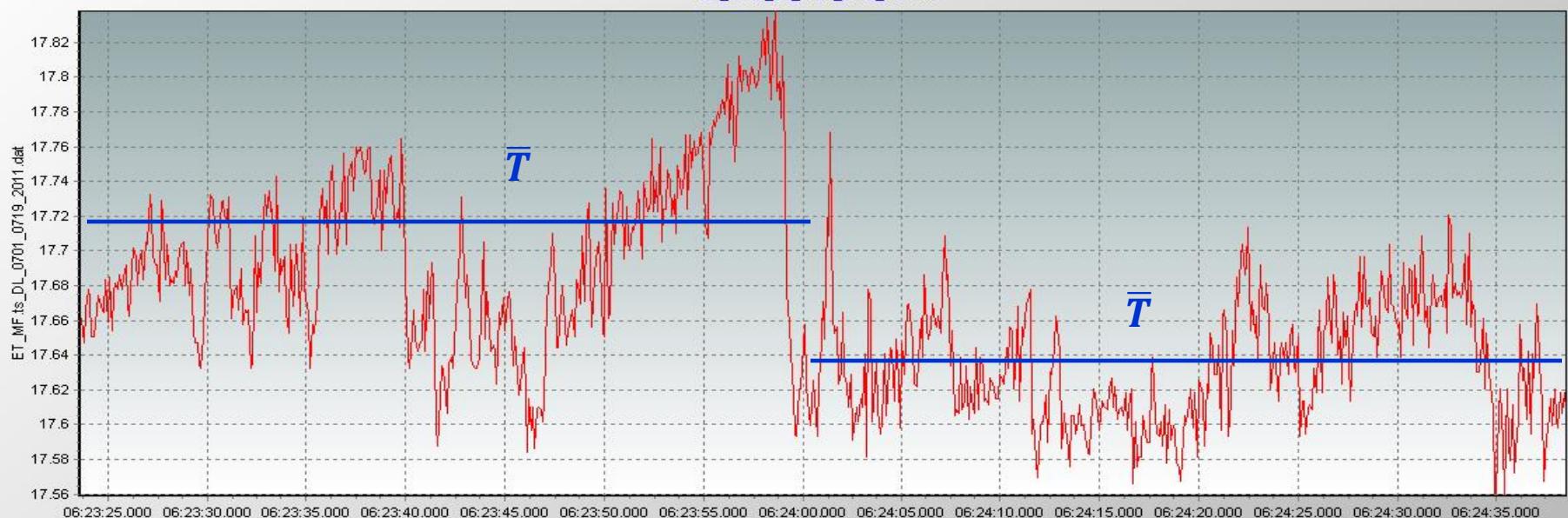
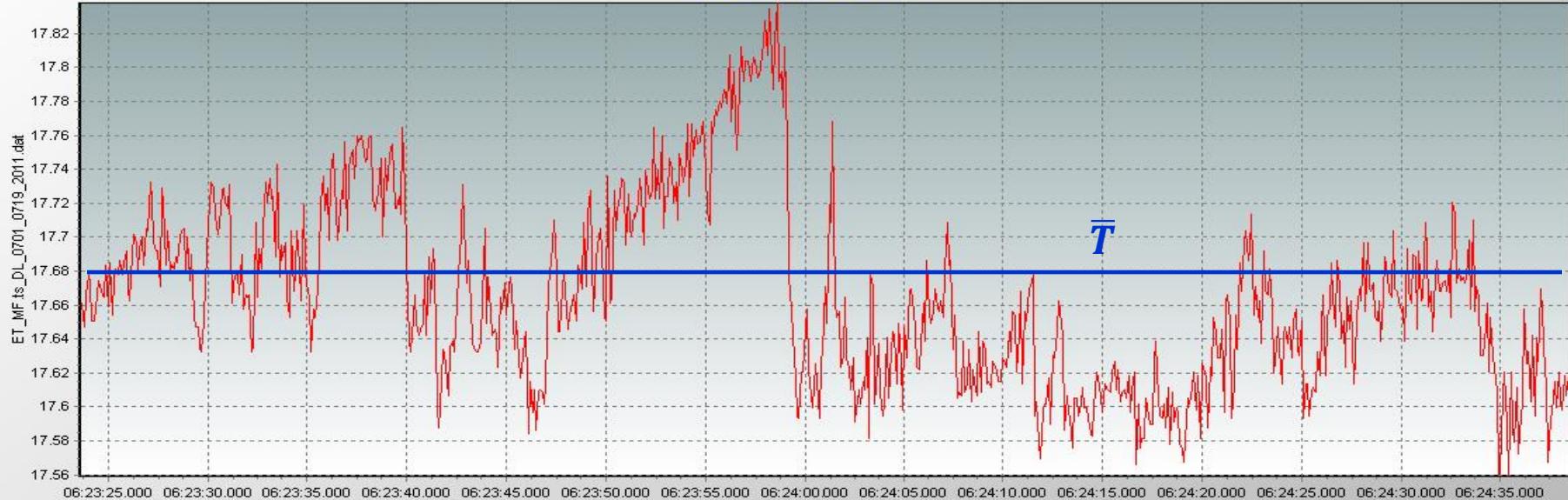
# 传感器分离频率反应函数

$$T_{Tw\_s}(f, s, u) = \exp\left[-9.9\left(\frac{f \times \text{Separation distance}}{u}\right)^{1.5}\right]$$



# 高频被濾(high-cut filter)的湍流譜

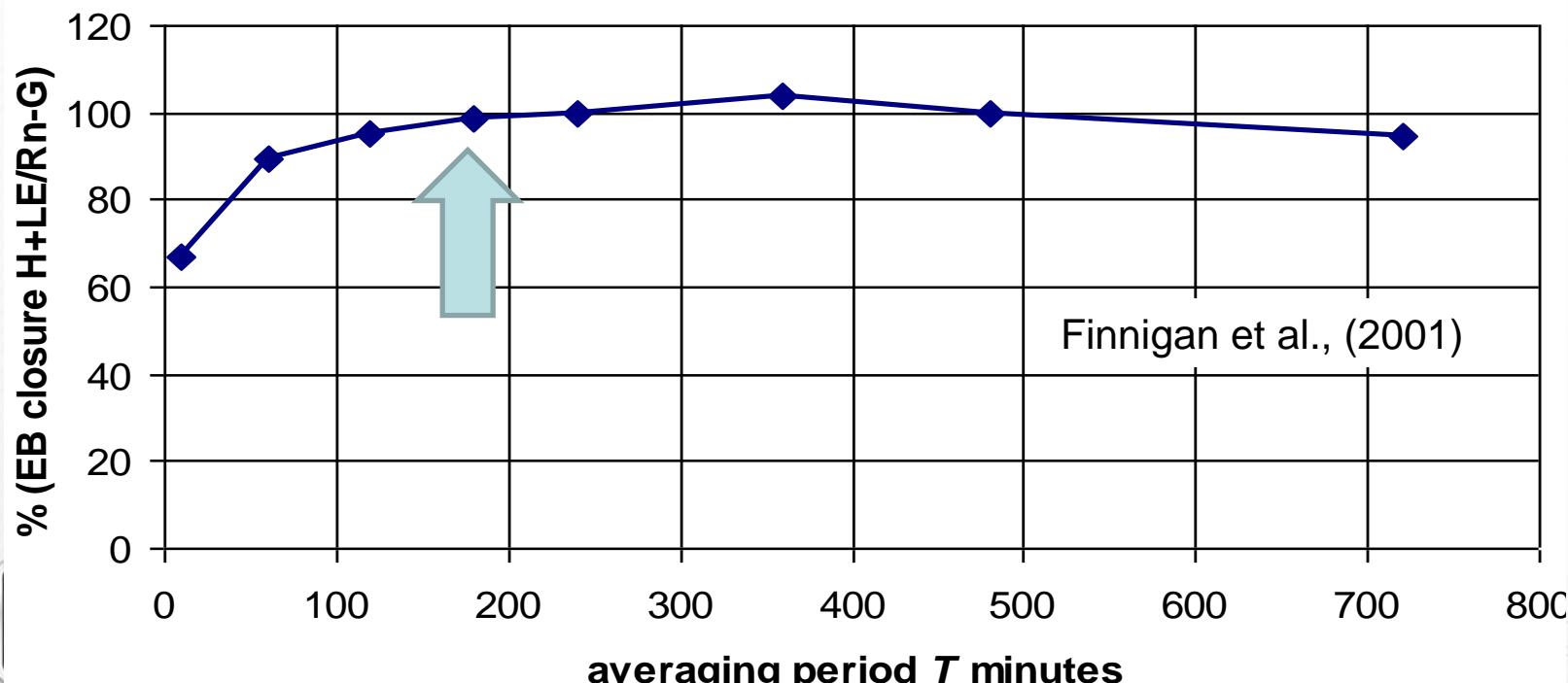




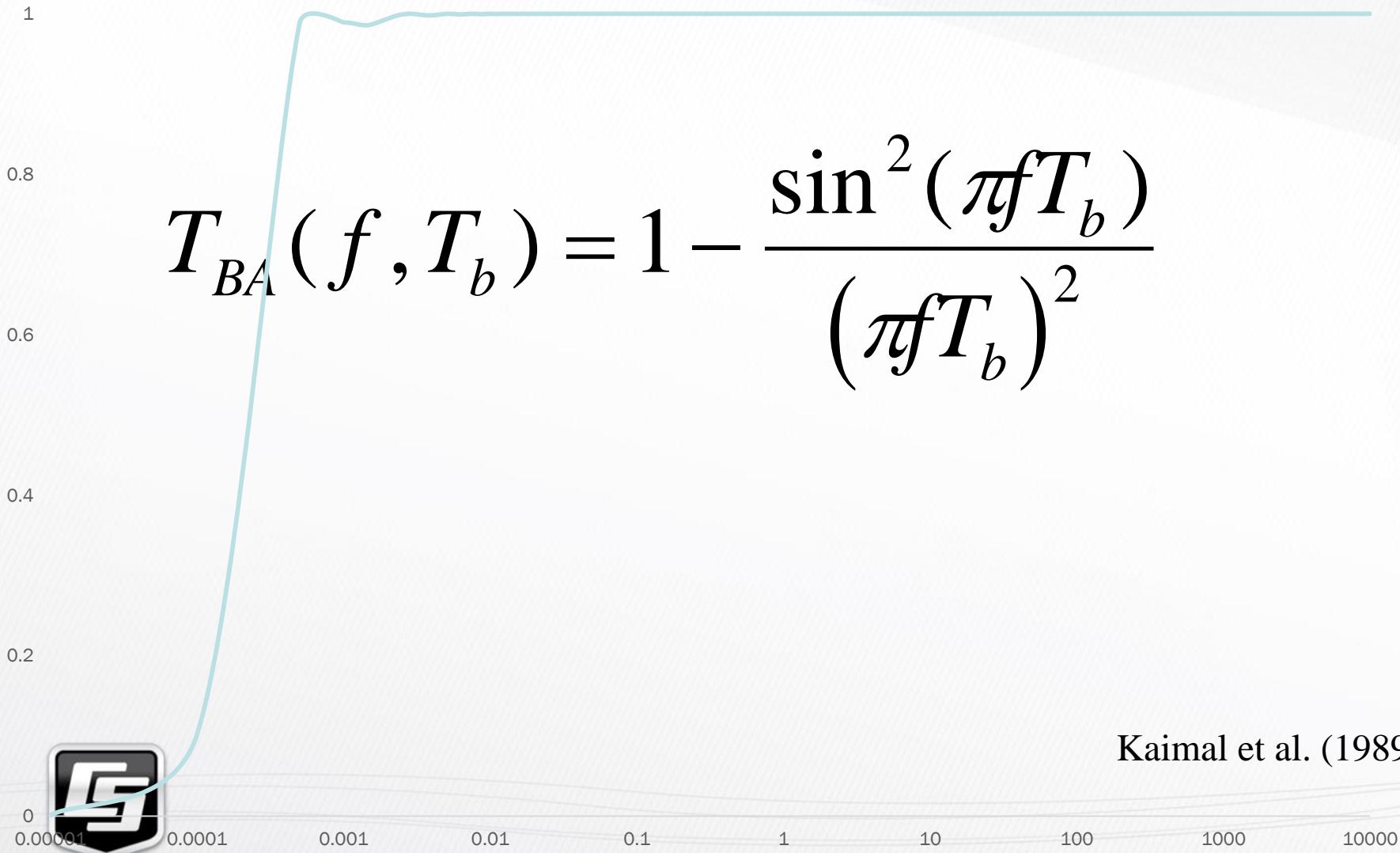
一般平均时长是30分钟

这个时长在一些情况下较短，可能丢失通量

- 在Manaus 热带雨林，平均时长短于180 分钟有通量丢失.



# 平均方法 (平均时长)



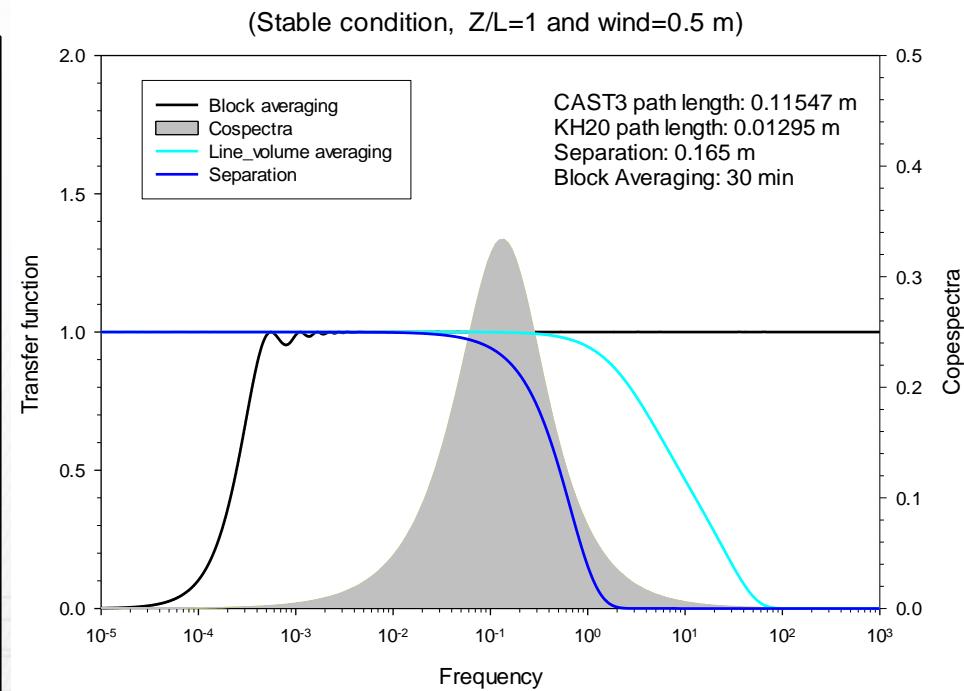
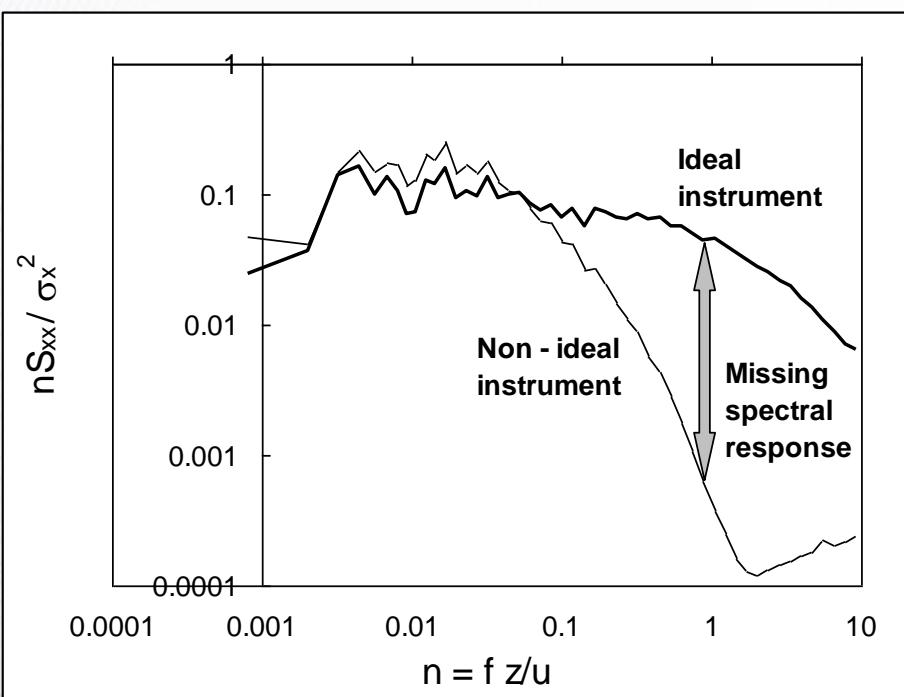
# 频率修正

$$\overline{\alpha' w'} = \left( \overline{\alpha' w'} \right)_m \left\{ \frac{\int_0^{\infty} S_{\alpha w}(f) df}{\int_0^{\infty} T_{\alpha w}(f) S_{\alpha w}(f) df} \right\}$$

‘真’ 协谱

测得的  
协方差

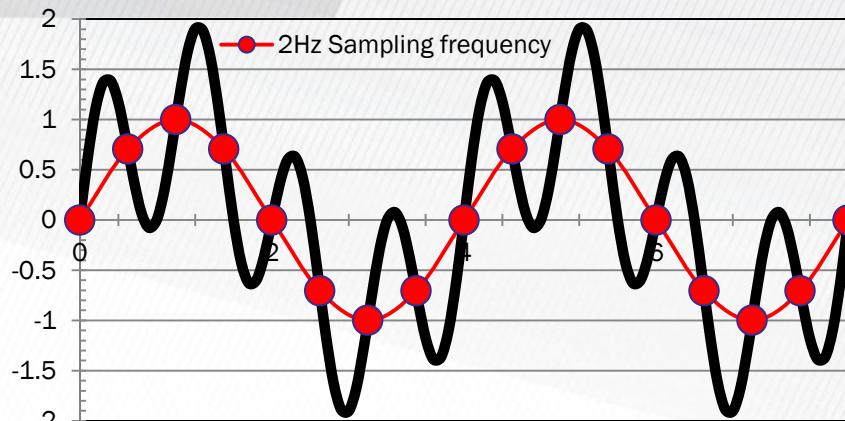
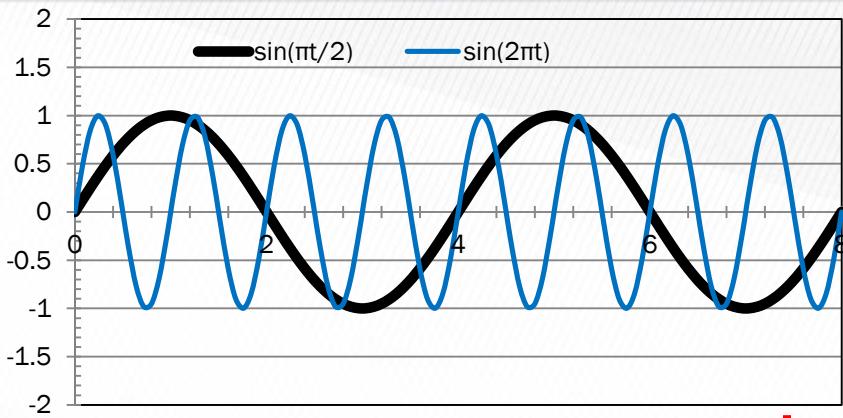
频率反应  
函数



# 4. 测定频率

(Sampling frequency)

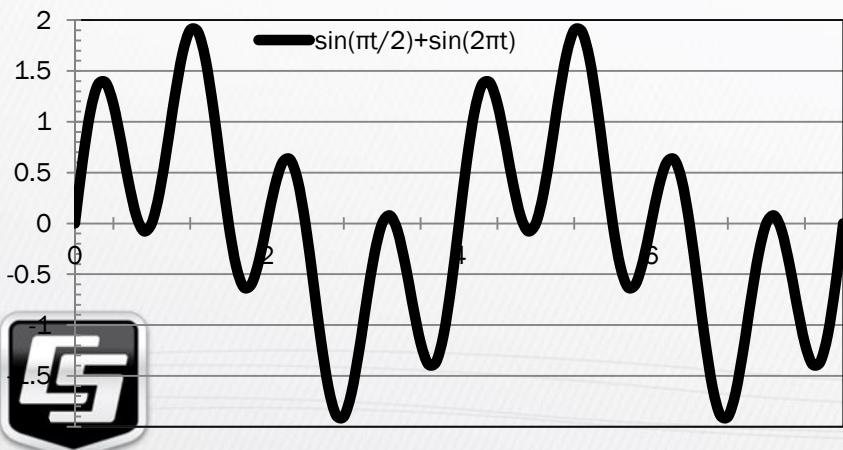
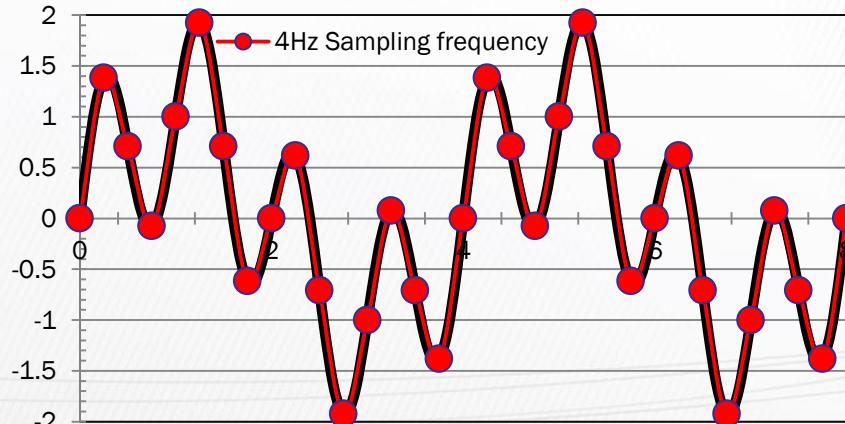
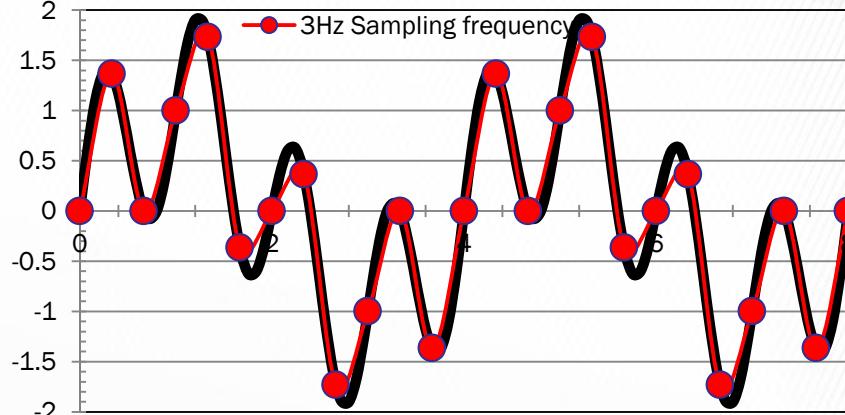




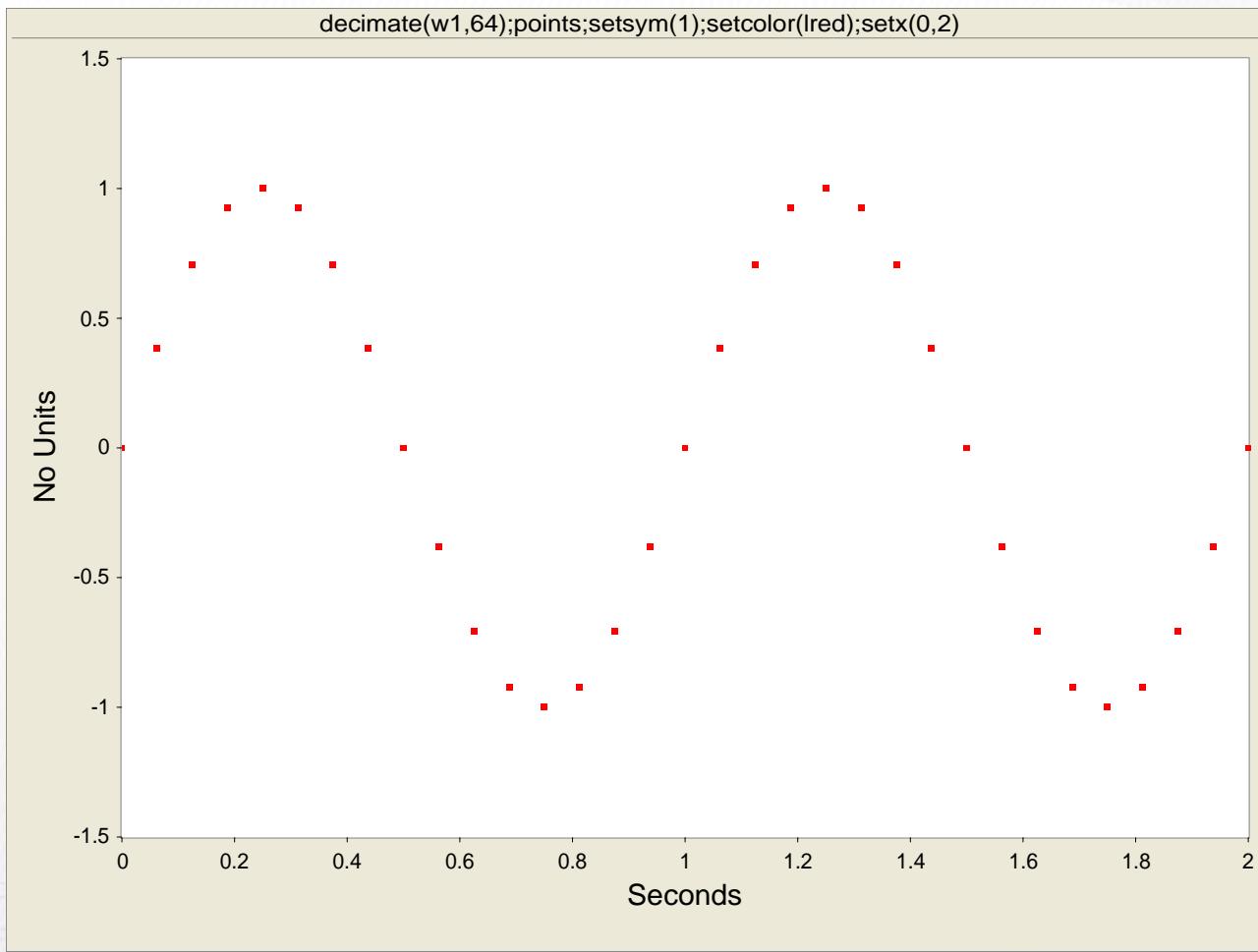
## 测定频率与湍流信号频率

香农定理 (Shannon Theorem)

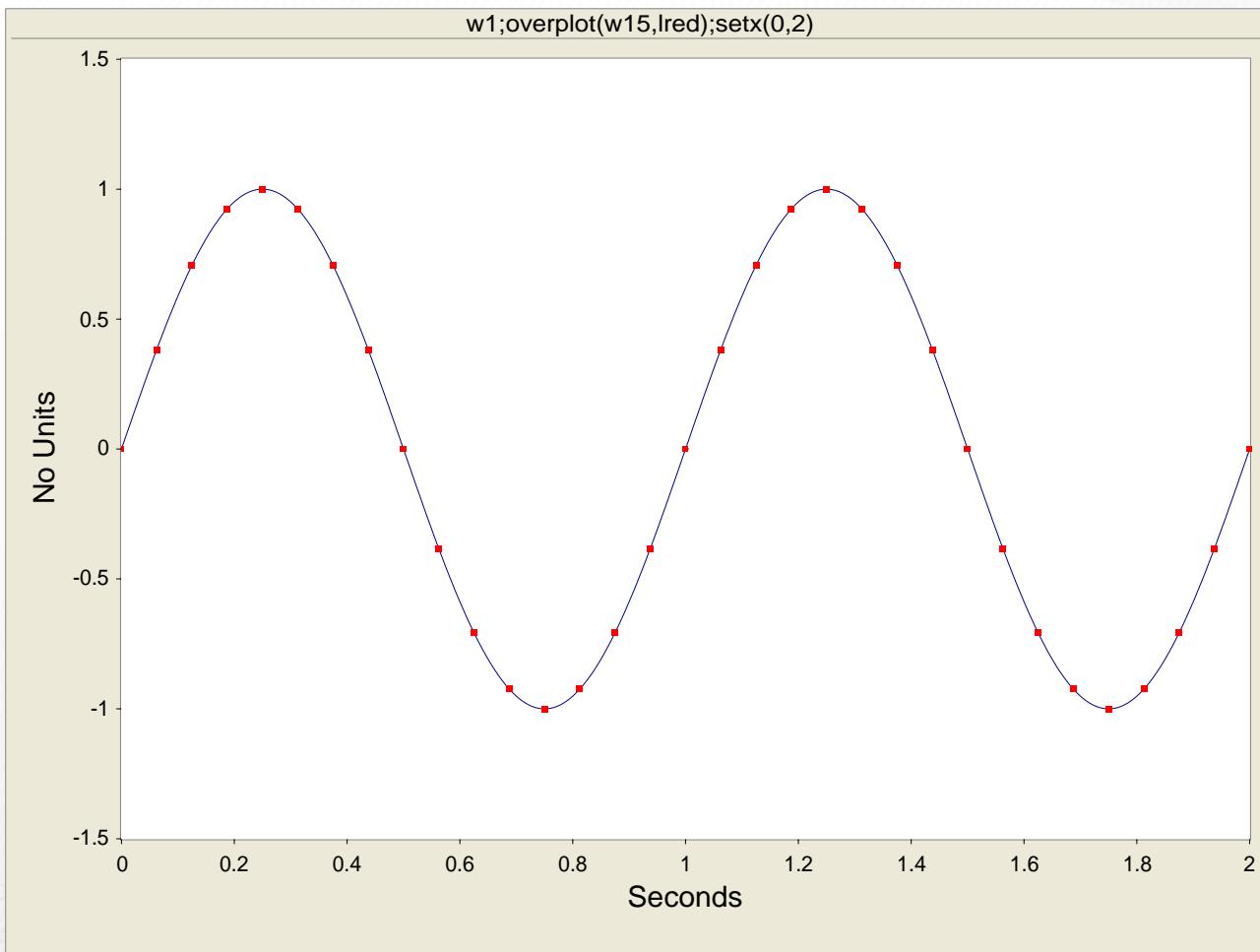
测定频率**最低**应是  
被测信号**最高频率的二倍**。



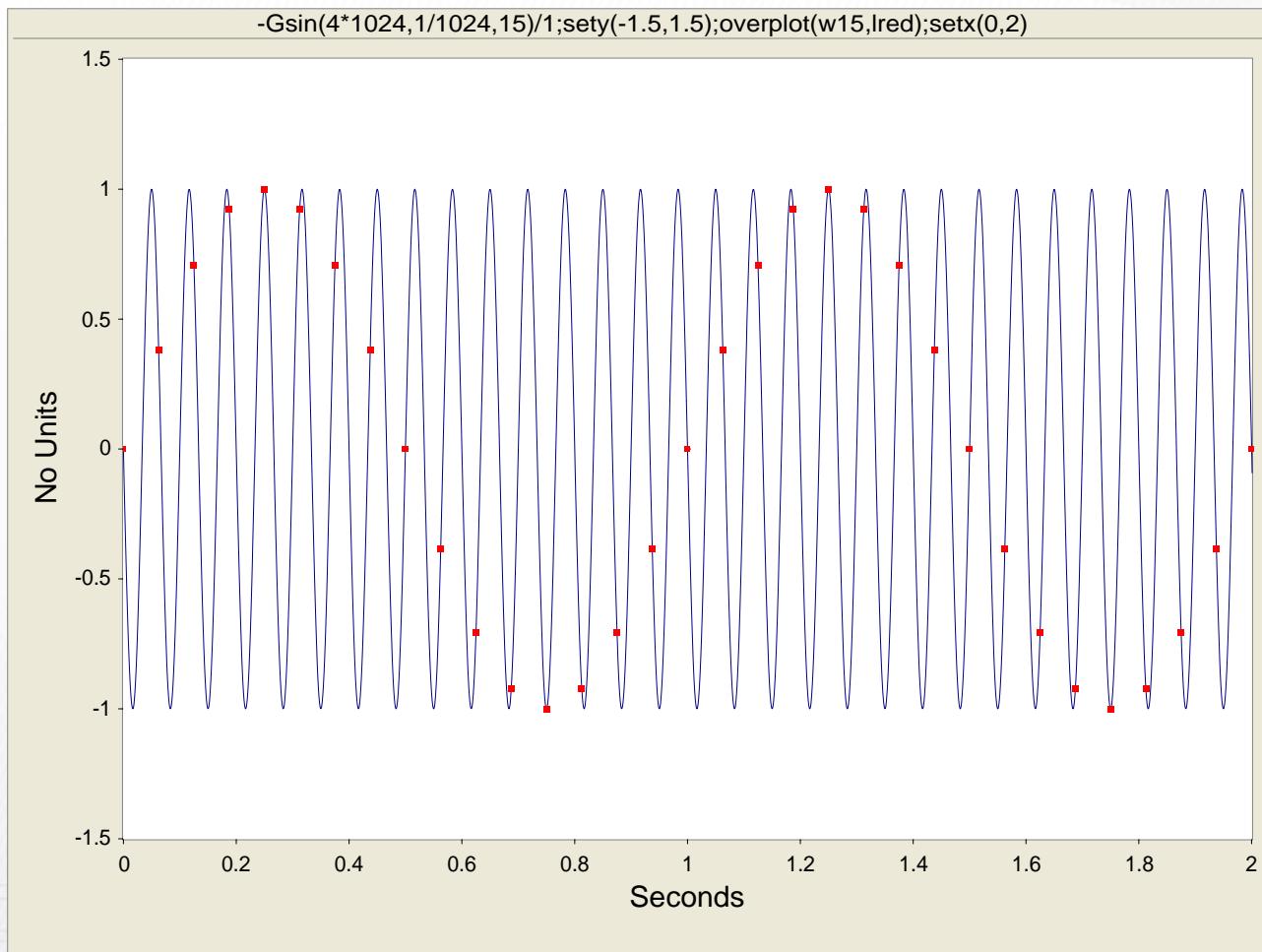
# 非连续性样本



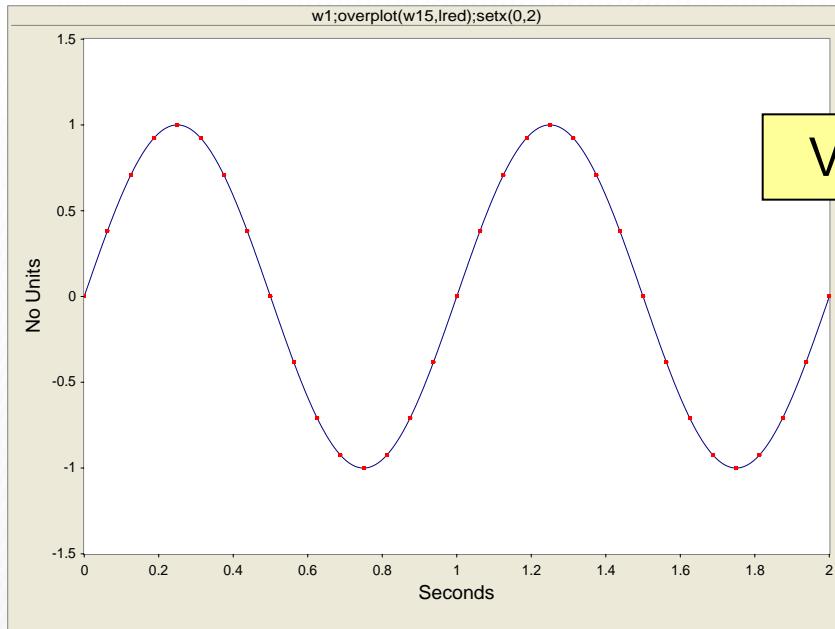
# 原信号?



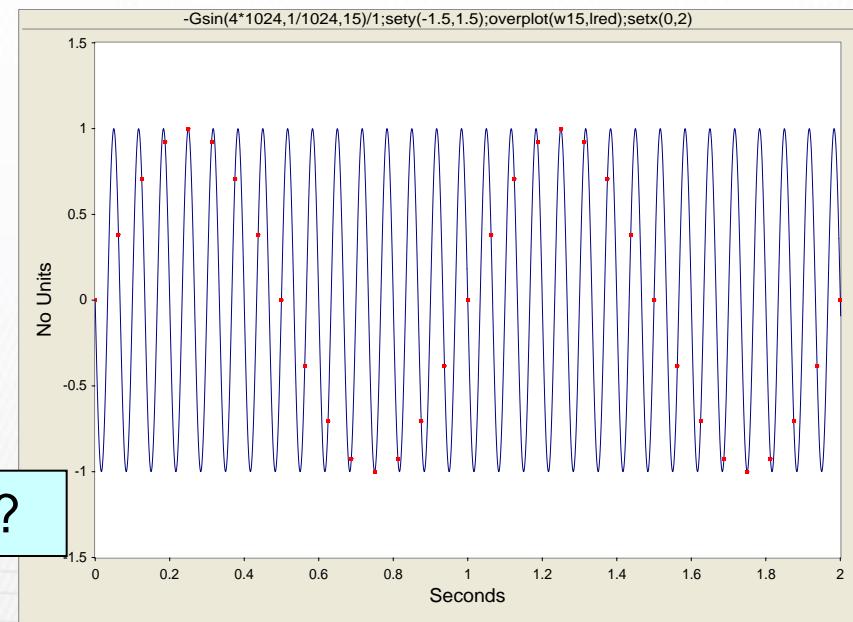
# 另一可能?



# 失真信号的统计描述



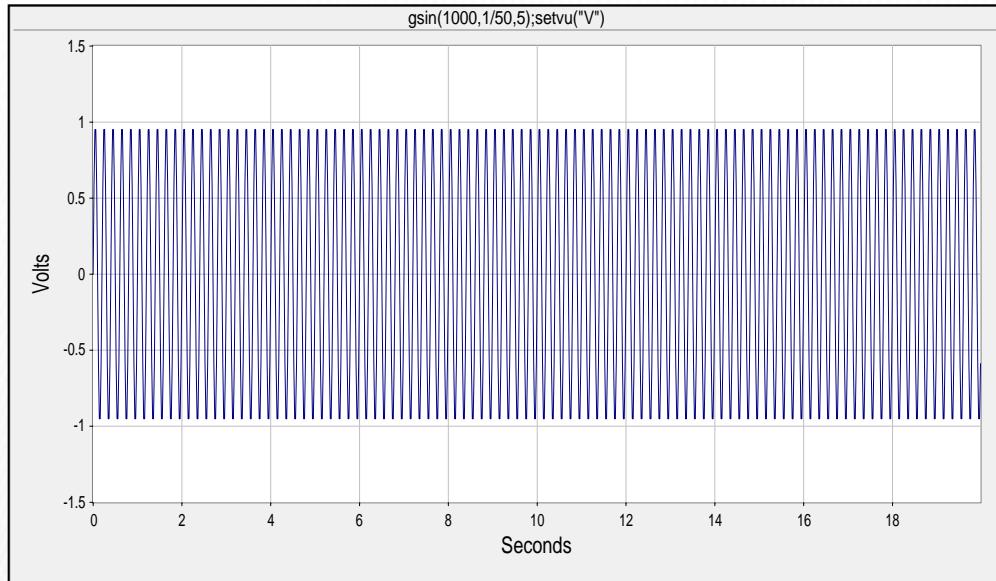
Variance = ???



Variance = ???



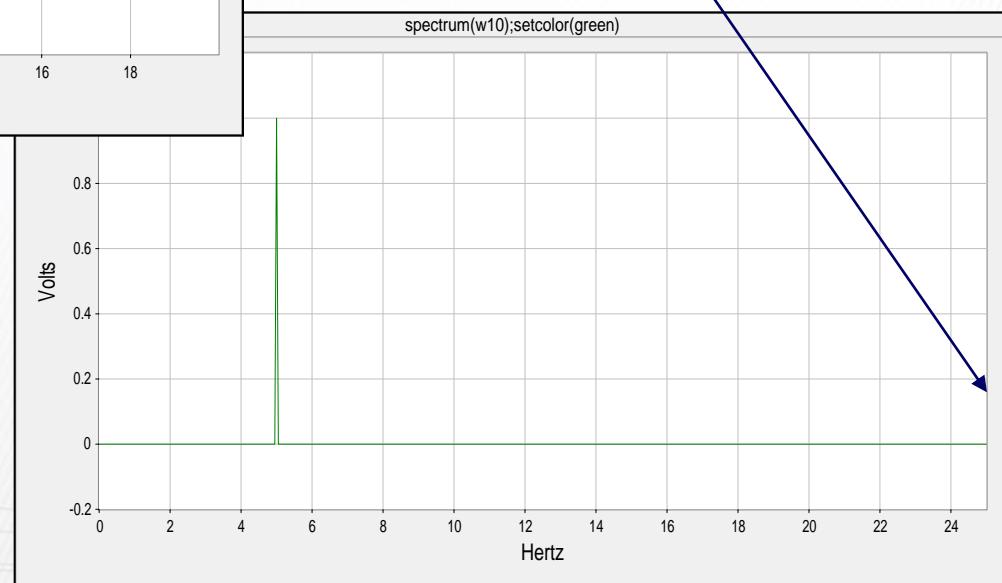
# 样本信号的奈奎思特 (Nyquist) 频率 Sine Waves



5-Hz 频率正玄函数  
50 Hz 采样频率

5-Hz 时间正玄函数  
50 Hz 采样频率

$$\text{Nyquist Frequency} = f_{\text{sample}}/2 = 25 \text{ Hz}$$



# 测定频率( $f_s$ ) 的确定

$$f_s = \frac{z_m n_{max}}{\bar{U}}$$



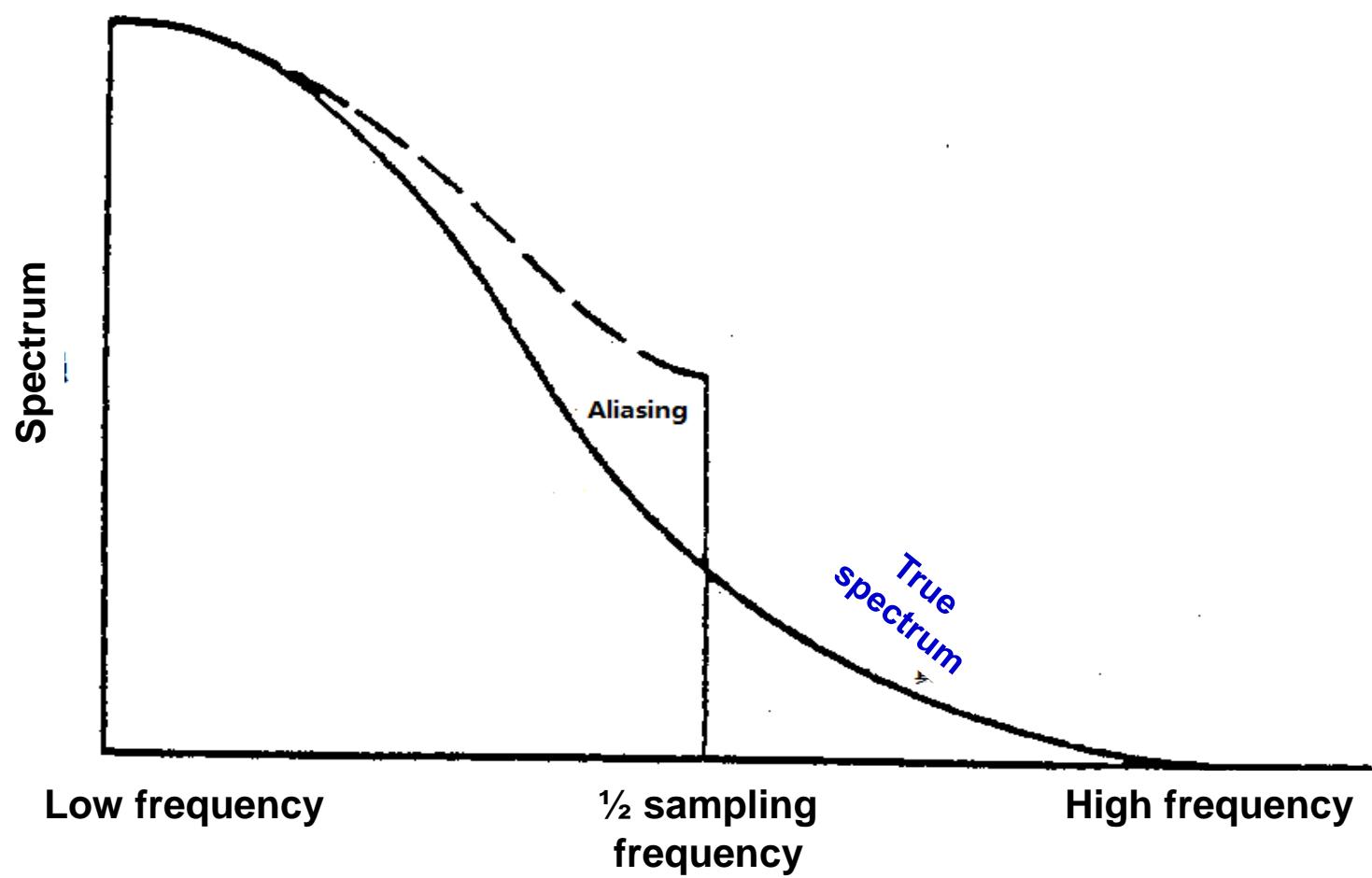
## 4. 高叠（“杂”）低现象 (Aliasing)



失真  
采集的离散时间信号  
(video)



- Aliasing:**
1. 在信号采集过程中，大于  $1/2$  采样频率的信号在样本中不能在其自己频率出现
  2. 然而，这些信号在样本中确出现在小于  $1/2$  采样频率段中。



# 数学理解 aliasing

$$w(t) = \sin 2\pi \left( \frac{p + 0.25}{2 \times 0.005} \right) t$$

If  $p = 1$ , Then  $\frac{1 + 0.25}{2 \times 0.005} = 125$

200 Hz 采样频率 (时间隔 = 0.005 sec)

$$w(t_i) = \sin 2\pi \left( \frac{p + 0.25}{2 \times 0.005} \right) (t_i \times 0.005) = \cos p\pi t_i \sin 0.25\pi t_i$$

↑  
整数

$p$  为奇数 ( $p=1$ , 125 Hz 信号)

$$\begin{aligned} w(t_i) &= (-1)^{t_i} \sin 0.25\pi t_i \\ &= \cos \pi t_i \sin 0.25\pi t_i \\ &= -\sin(2\pi) \times 75 \times (0.005t_i) \end{aligned}$$

200Hz

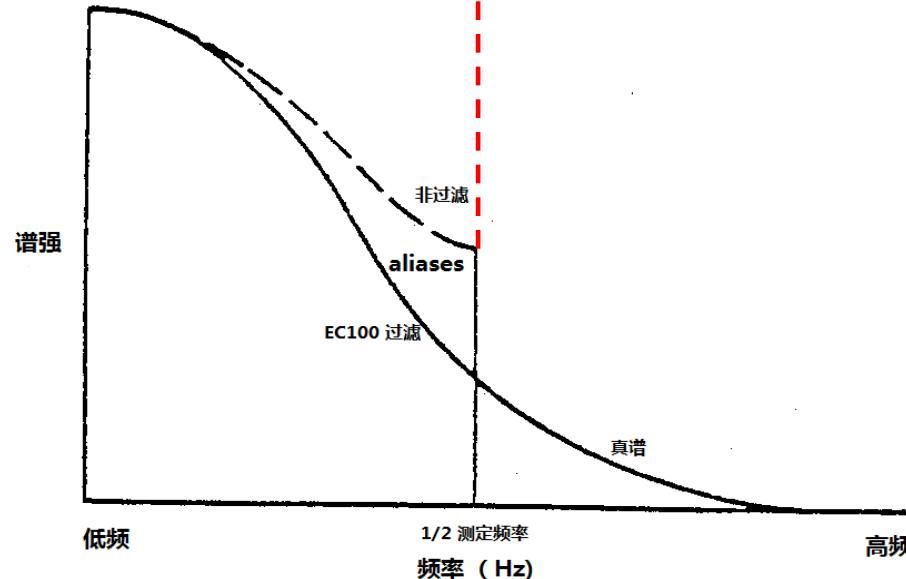
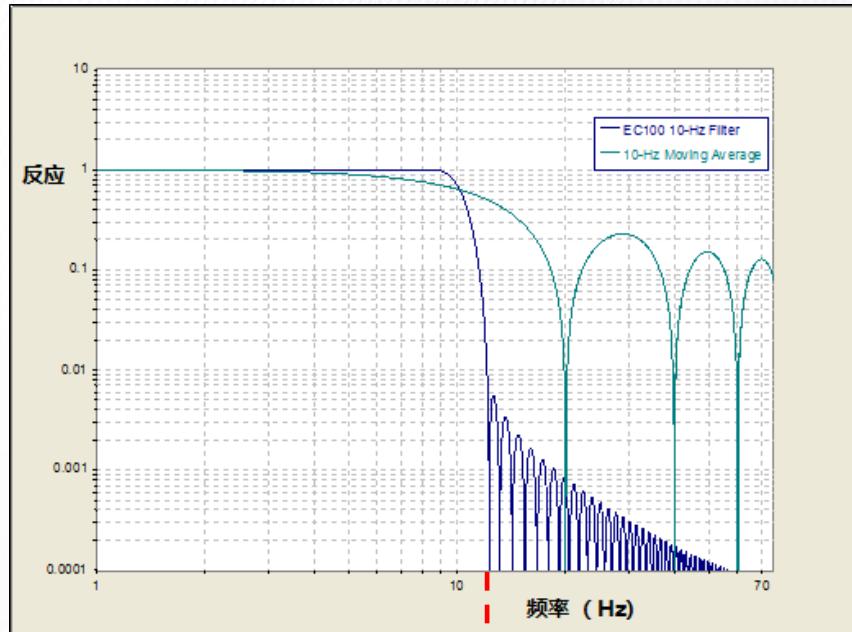
$p$  为偶数 ( $p=2$ , 225 Hz 信号)

$$\begin{aligned} w(t_i) &= \sin 0.25\pi t_i \\ &= \sin(2\pi) \times 25 \times (0.005t_i) \end{aligned}$$

200Hz



## 6. 减少高叠（“杂”）低效应 (Aliases)



# **5. 超声感热通量订正 (SND correction)**

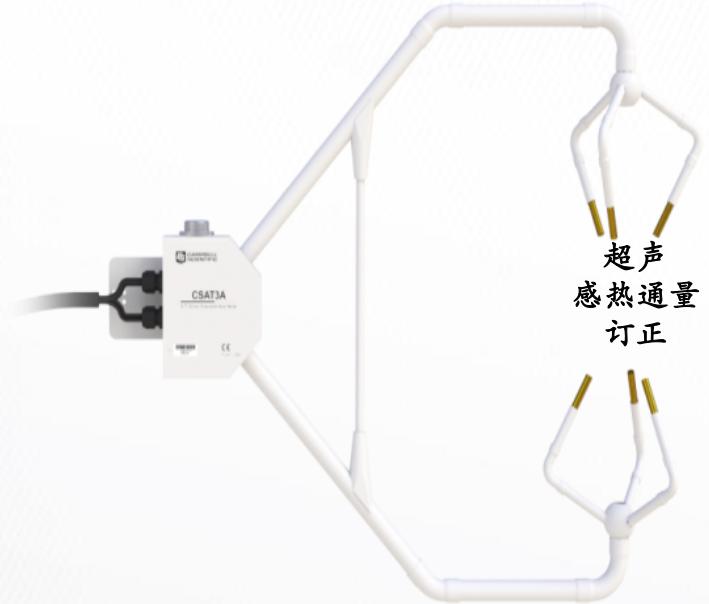


$$c^2 = \gamma \frac{P}{\rho}$$

$$\frac{P}{\rho} = R_d T_v = R_d \frac{T}{\left[1 - (1 - \varepsilon) \frac{e}{P}\right]}$$

$$T_s = \frac{c^2}{\gamma_d R_d}$$





Schotanus et al. (1983)

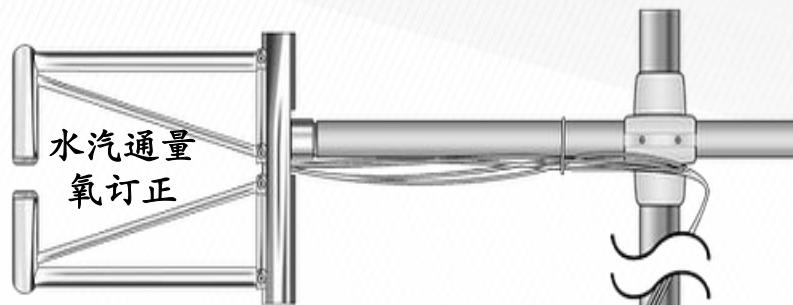
$$T_s = T(1 + 0.514q)$$

$$T'_s = T' \frac{\bar{T}_s}{\bar{T}} + 0.514q' \bar{T}$$

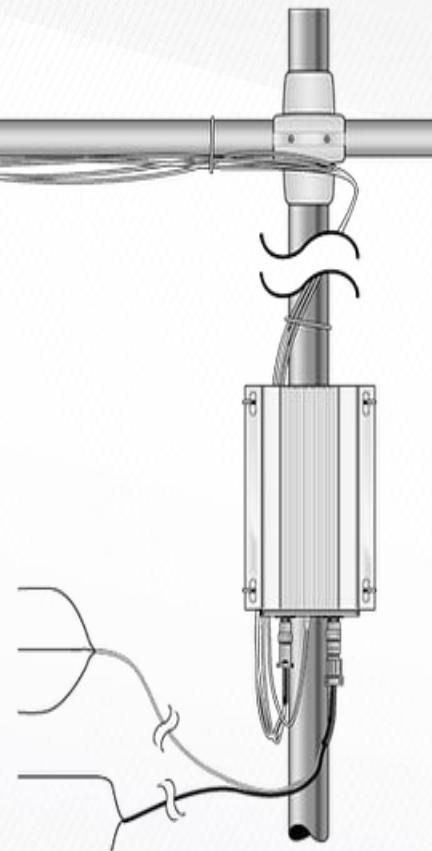


# 6. 氧订正 (Oxygen correction)





Tanner et al. (1993)

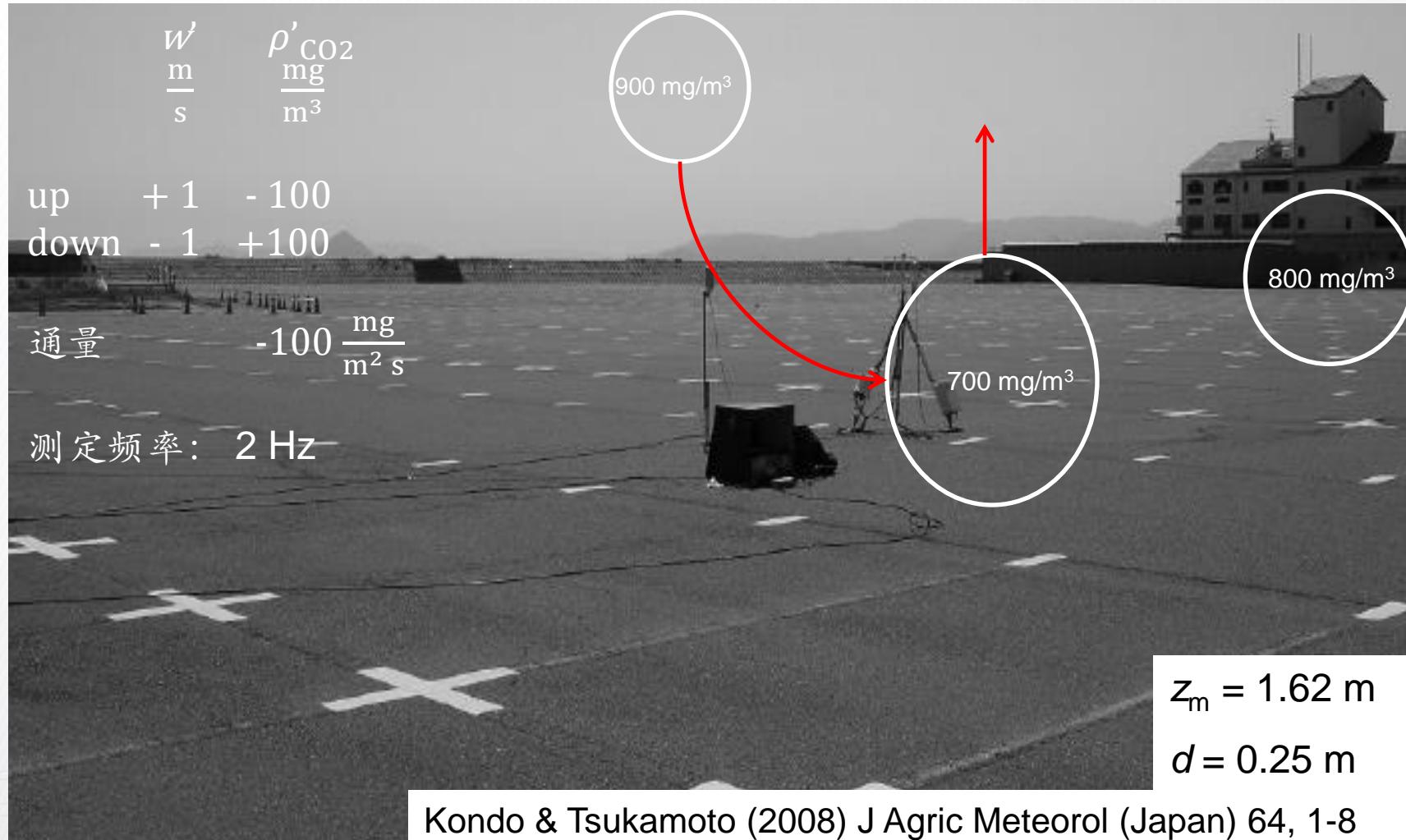


## 7. 订正测定过程中空气密度的变化影响 (WPL correction)



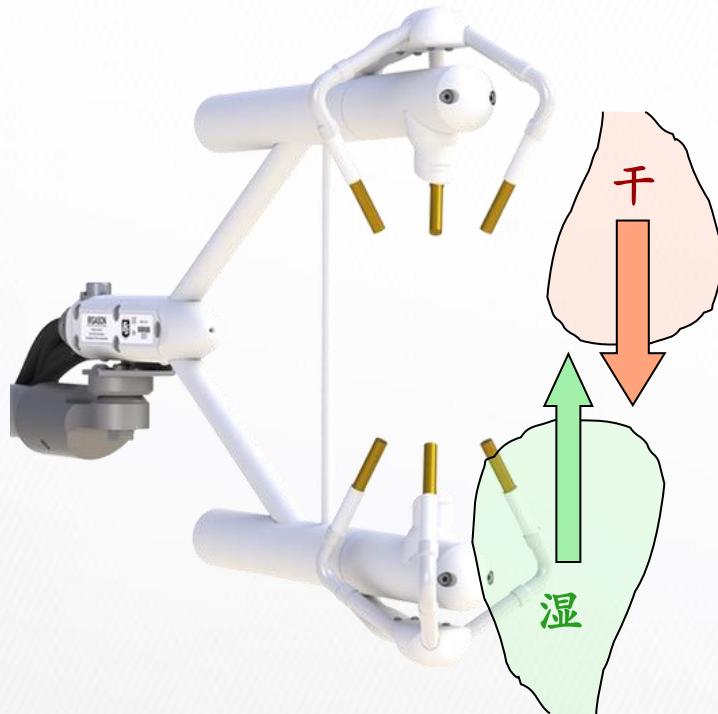
## 空气密度变化对通量测定影响

- 在没有CO<sub>2</sub>交换下垫面，可测得明显的CO<sub>2</sub>负通量



Kondo & Tsukamoto (2008) J Agric Meteorol (Japan) 64, 1-8

# WPL correction 订正空气密度变化所引起的测定误差



$$\bar{W} \neq 0$$

1. 水和CO<sub>2</sub>出入地面
2. 感热通量引起的空气度变化

$$\bar{W} - 0.75 \sim 1.5 \text{ mm/s}$$
$$LE - 200 \sim 600 \text{ W/m}^2$$

CAST 分辨率: 0.25 ~ 2.00 mm/s



# Webb, Pearman & Leuning (1980) 理论

## 稳态, 水平一致的湍流

$$\overline{F}_c = \overline{c_d w' \chi_c} = \overline{w' c'_c} + \overline{\chi_c} \left[ \overline{w' c'_v} + \overline{c} \frac{\overline{w' T'}}{\overline{T}} \right]$$

Raw CO<sub>2</sub> flux   Water vapor flux   Heat flux

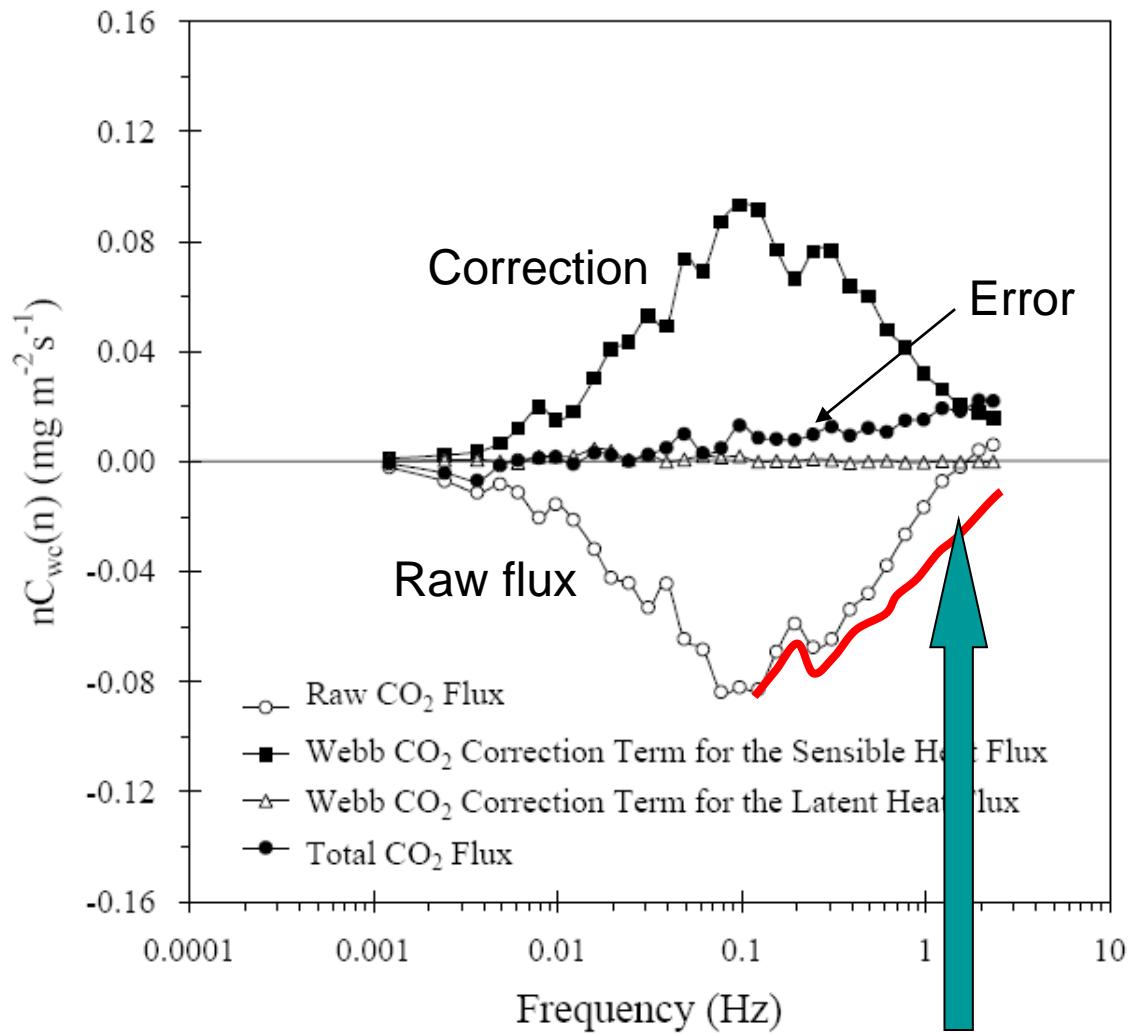
Leuning (2007) showed original WPL still correct

For non-steady state flows



## 协湍流谱

Error due to  
differing  
frequency  
responses for  
cospectra of  
 $wT$  and  $wC_c$



Need to correct for loss of covariance before WPL correction



# 开路湍流通量测定的计算

Correct  $H$ ,  $E$  &  $F_c$  co-spectra first for high & low frequency filtering

$$1) \quad \overline{H} = \overline{\rho c_p w' T'}$$

$$2) \quad \overline{E} = (1 + \overline{\chi_v}) \left[ \overline{w' c_v'} + \frac{\overline{c_v}}{\overline{T}} \frac{\overline{H}}{\overline{\rho c_p}} \right]$$

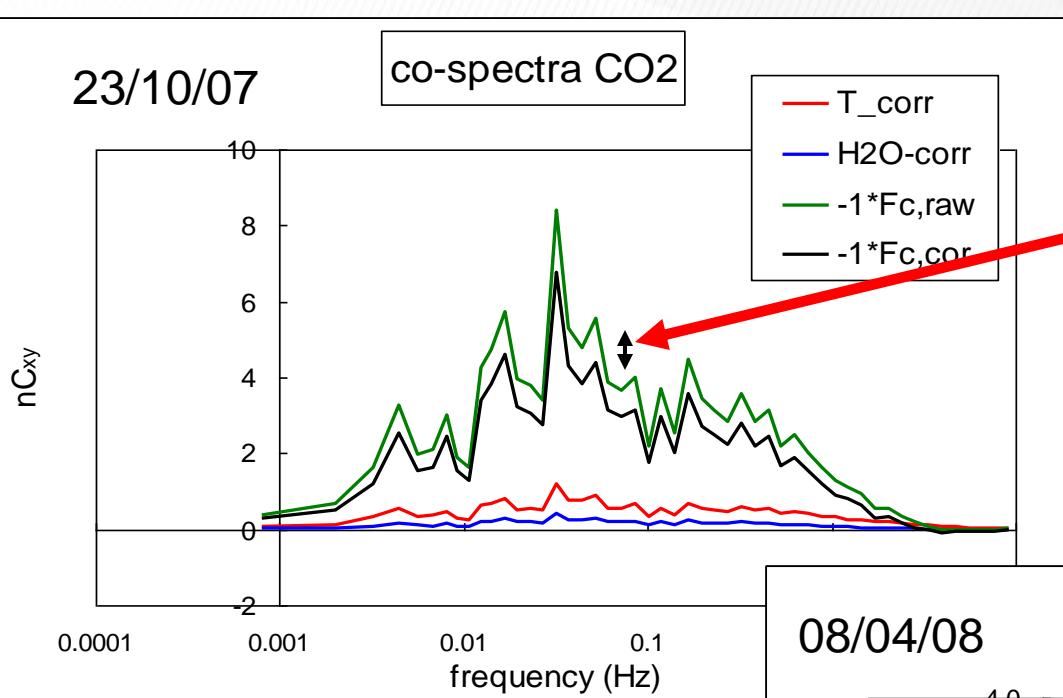
$$3) \quad \overline{F}_c = \overline{w' c_c'} + \overline{c_c} \left[ \frac{\overline{E}}{\overline{c}} + \frac{\overline{H}}{\overline{\rho c_p T}} \right]$$



# 有时WPL 对开路测定订正非常大

23/10/07

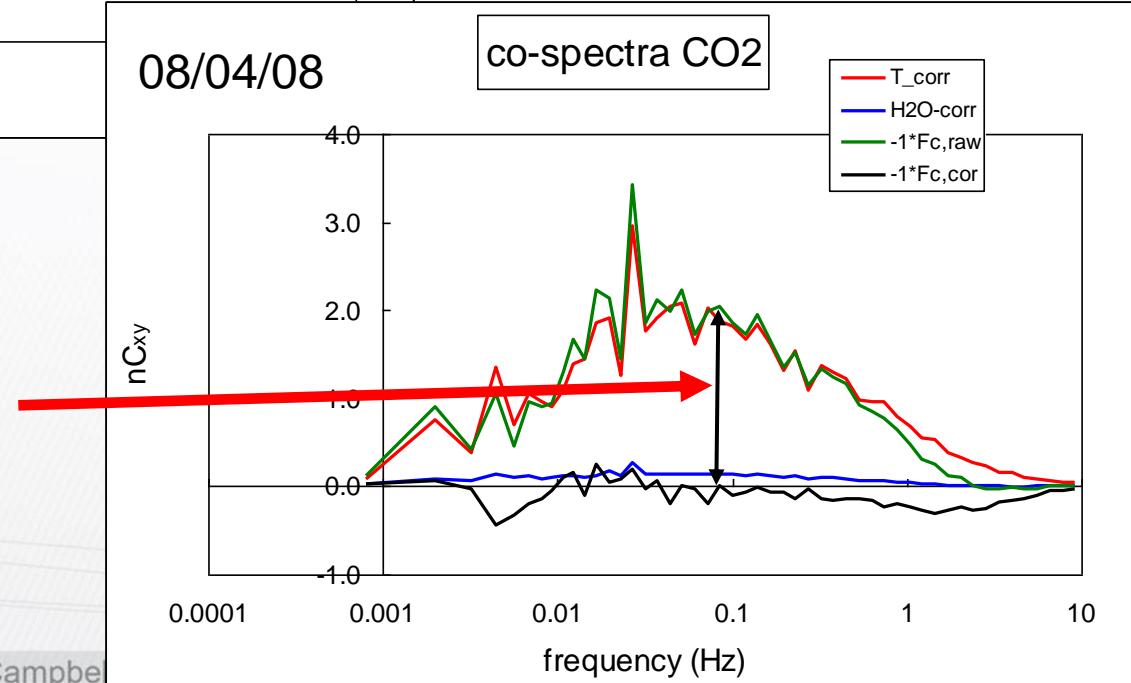
co-spectra CO<sub>2</sub>



小 wT WPL 订正

08/04/08

co-spectra CO<sub>2</sub>



大 wT WPL 订正



## 最新模型

Gu et al./Ag For Meteorol (2012)

净CO<sub>2</sub>通量 ( $N_{co2}$ )

$$N_{co2} = \overline{w' c'_{co2}}|_h + \frac{\overline{c_{co2}}}{\overline{C_d}} \left[ \overline{w' c'_{h2o}} + \bar{c} \frac{\overline{w' T'}}{\bar{T}} \right] h + \int_0^h \frac{\partial \overline{c_{co2}}}{\partial t} dz - \frac{\overline{c_{co2}}}{\overline{C_d}} h \int_0^h \frac{\partial \overline{c_d}}{\partial t} dz$$

↑ 千空气  
密度

↑ 湿空气  
密度

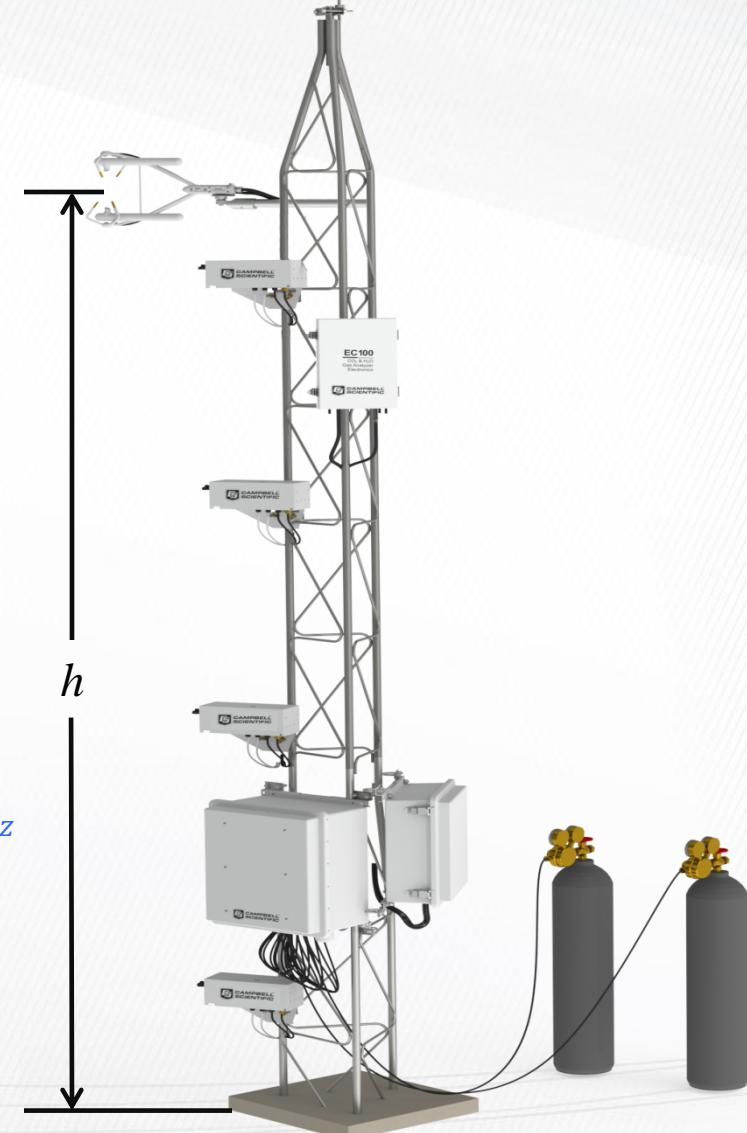
净H<sub>2</sub>O通量 ( $N_{h2o}$ )

$$N_{h2o} = \overline{w' c'_{h2o}}|_h + \frac{\overline{c_{h2o}}}{\overline{C_d}} \left[ \overline{w' c'_{h2o}} + \bar{c} \frac{\overline{w' T'}}{\bar{T}} \right] h + \int_0^h \frac{\partial \overline{c_{h2o}}}{\partial t} dz - \frac{\overline{c_{h2o}}}{\overline{C_d}} h \int_0^h \frac{\partial \overline{c_d}}{\partial t} dz$$



## 最新仪器系统

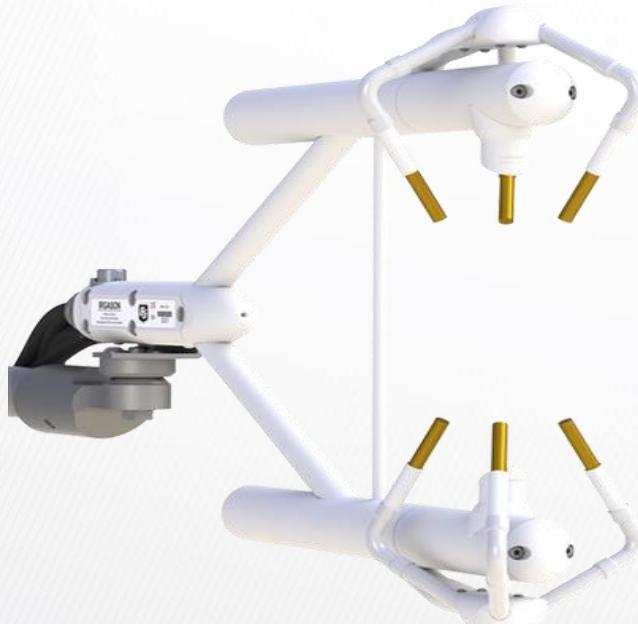
IRGASON and AP200



少假设  
少订正  
少不确定性  
高精度



Fewer assumptions used  
Fewer corrections needed  
Less uncertainty  
Better accuracy



**IRGASON**  
(红外超声碳水热通量集成观测仪)



**AP200**  
(红外大气碳水热纵断面观测系统)



**CPEC200**  
(闭路红外超声碳水热通量观系统)

A close-up photograph of a squirrel's head and front paws as it climbs a tree trunk. The squirrel has reddish-brown fur with dark stripes. A large, white, three-dimensional-style question mark is superimposed on the image, centered behind the squirrel's eye.

# Questions?

?

# 谢谢



Welcome to Campbell Scientific

